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# Algorithms for Radio Networks

Multicasting with Network Coding  
COPE

University of Freiburg  
Technical Faculty  
Computer Networks and Telematics  
Prof. Christian Schindelhauer



# Multicasting in Ad Hoc Networks

## ► Wu, Chou, Sun-Yuan,

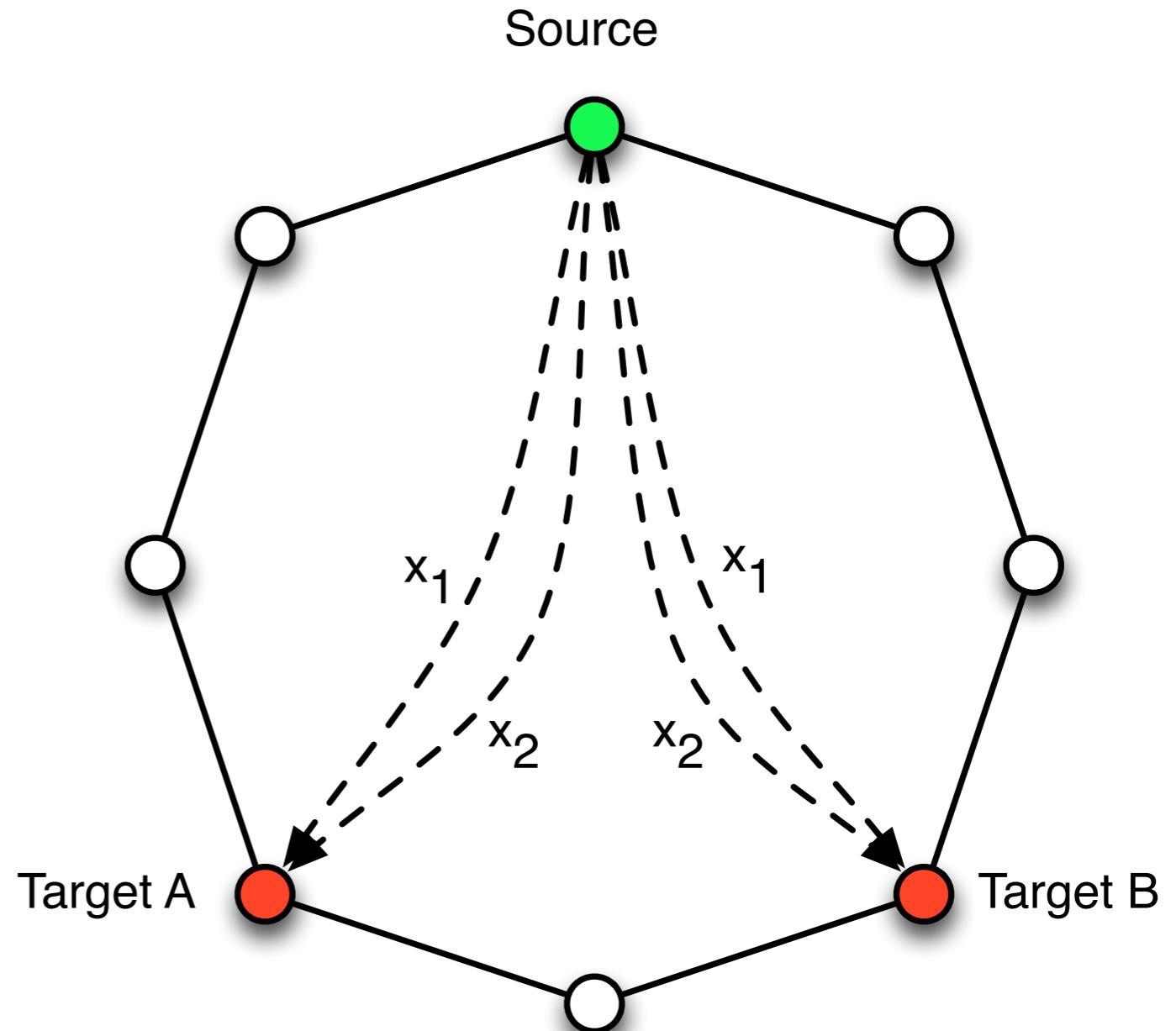
- Minimum-Energy Multicast in Mobile Ad hoc Networks using Network Coding, 2006

## ► Multicast

- Distribute message from one node to a given set of nodes

## ► Cost measure

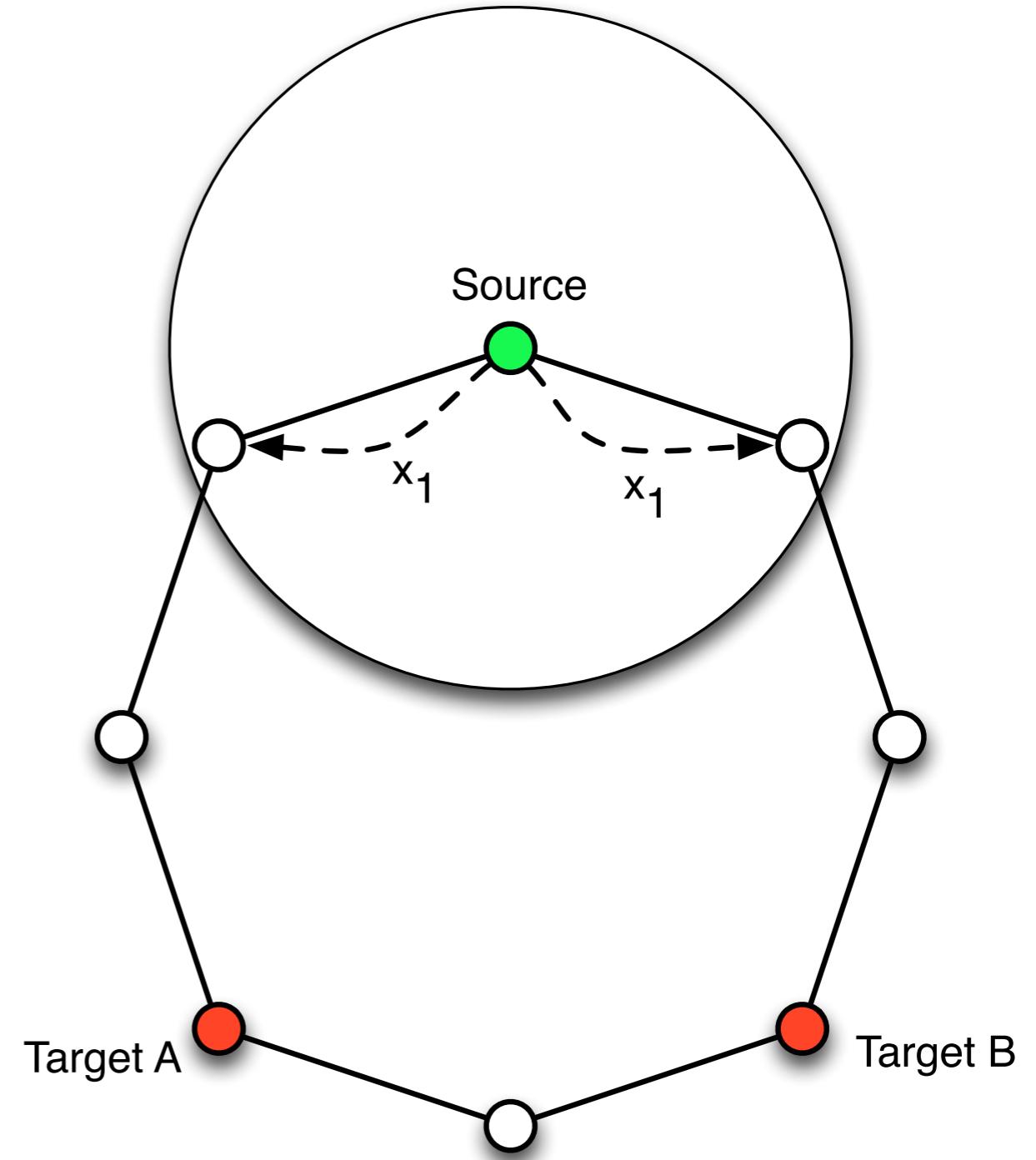
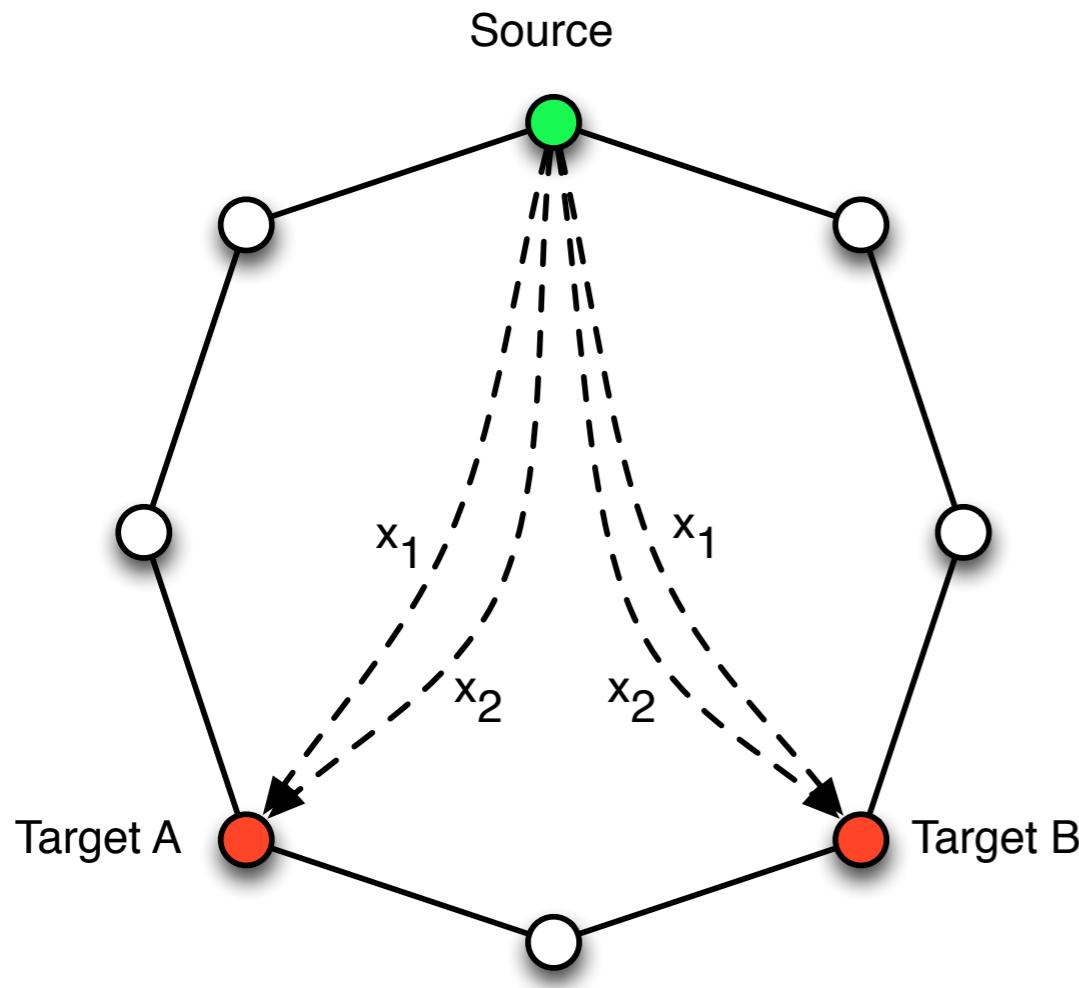
- Each one-hop broadcast costs an energy unit



# Beispiel

► **Traditionally,**

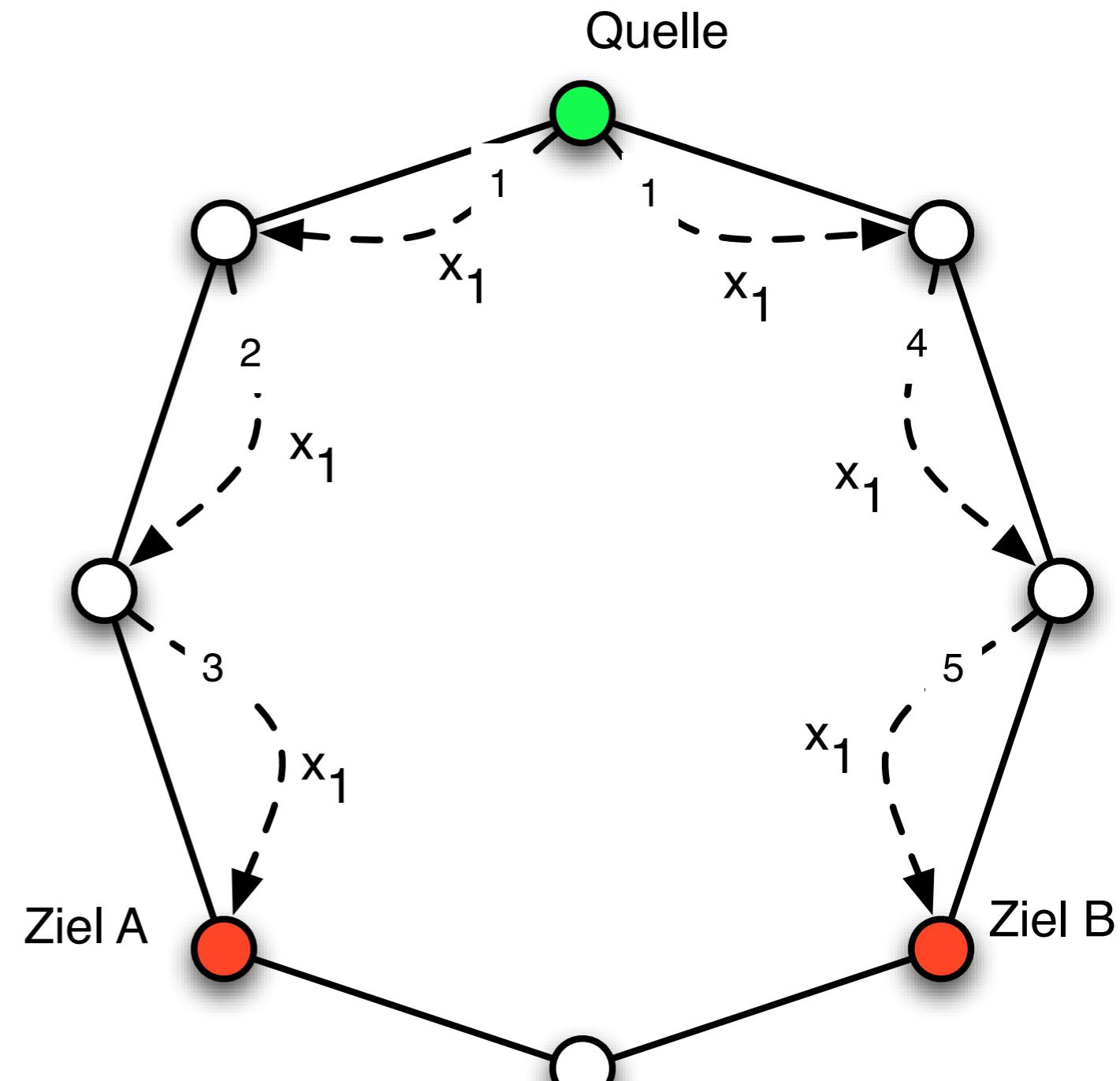
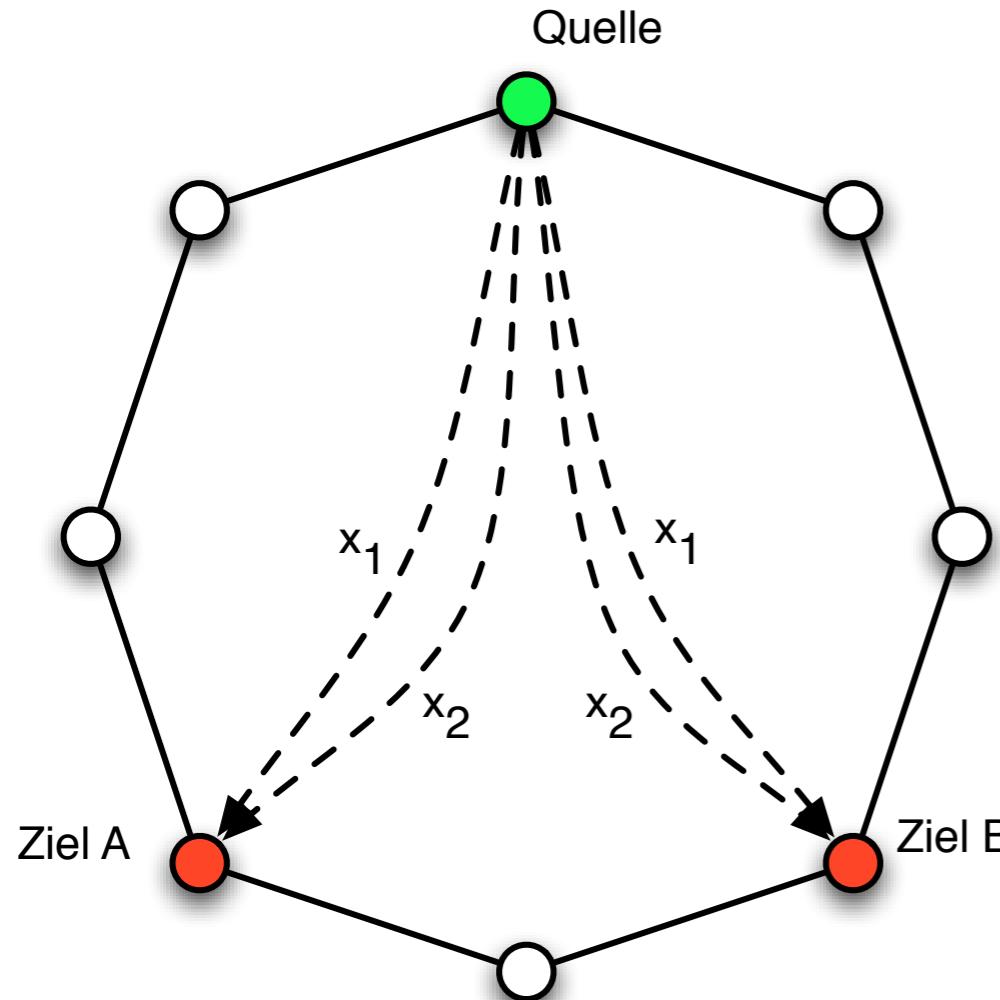
- it costs 5 energy units for a multicast message



# Example

► Traditionally,

- it costs 5 energy units for a multicast message



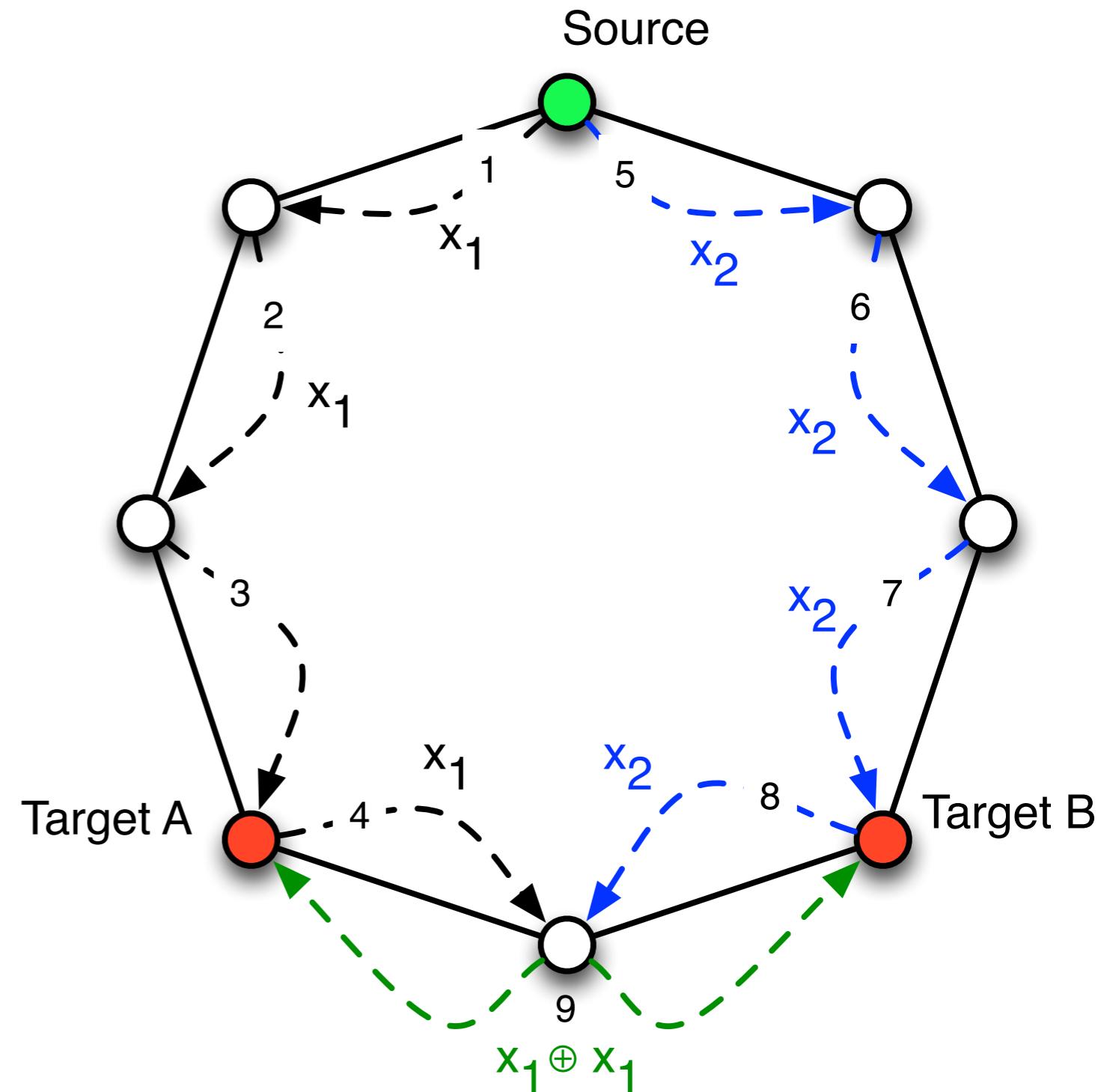
# Example

## ► Network coding

- 9 energy units for 2 messages
- Average of 4.5

## ► Without network coding

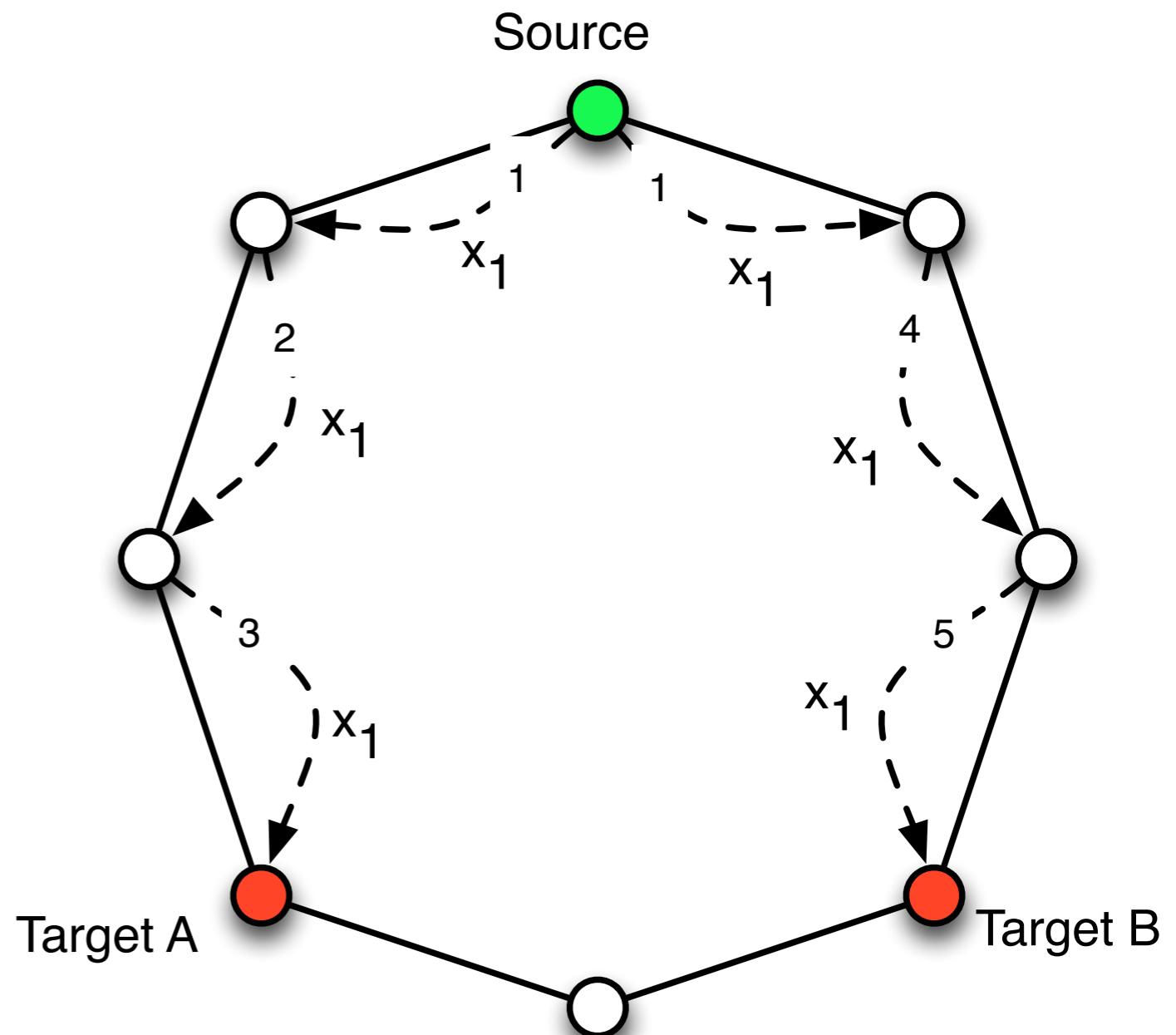
- 5 units for one multicast message



# Multicasting in Ad Hoc Networks

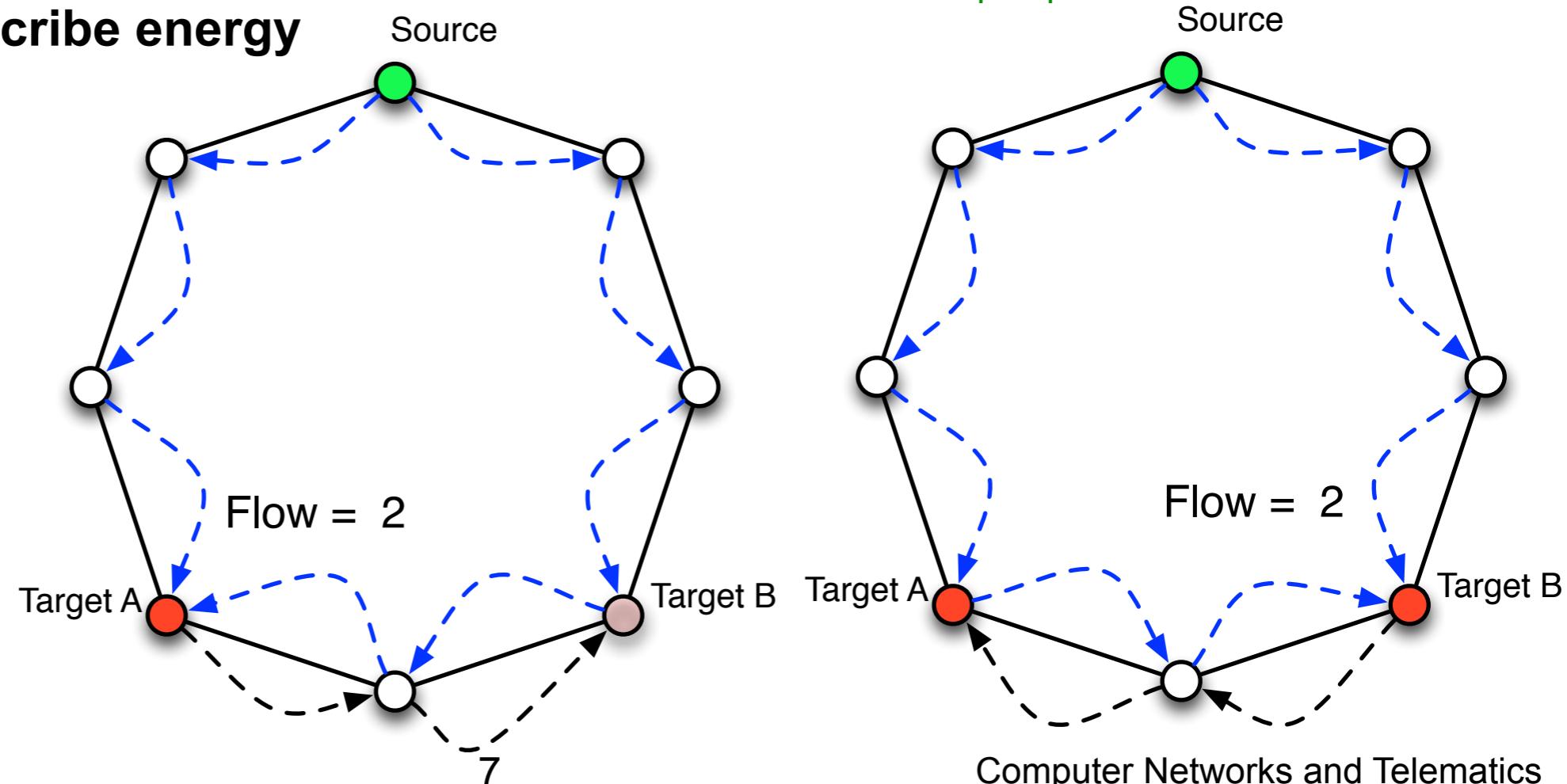
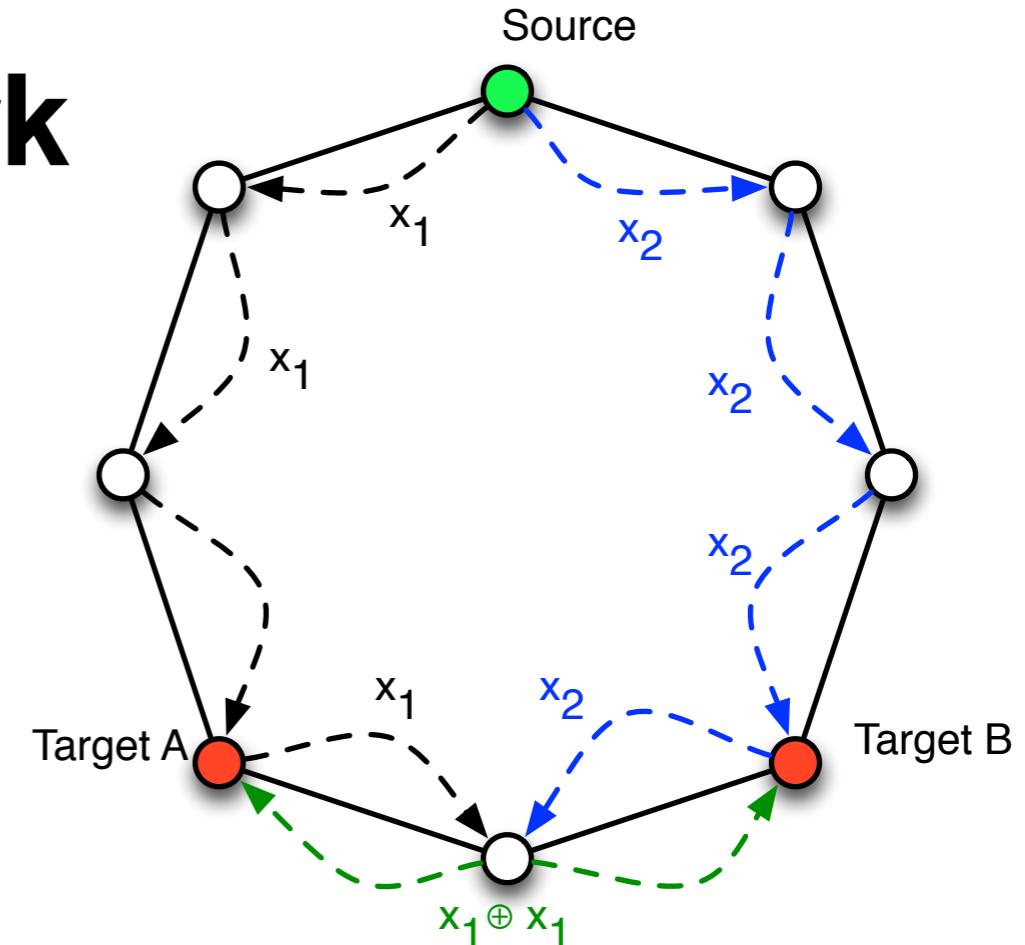
- ▶ **Solution of the minimal energy multicasting problem without network coding is NP-hard**

- Less than constant factor approximation is NP-hard
- Requires calculation of the discrete Steiner tree



# Condition for Network Coding

- ▶ **Messages allow flow of the size of the desired number of messages**
  - from the sources to each individual sink
- ▶ **If such flows are guaranteed, network coding can be applied**
- ▶ **Size of the flows describe energy consumption**

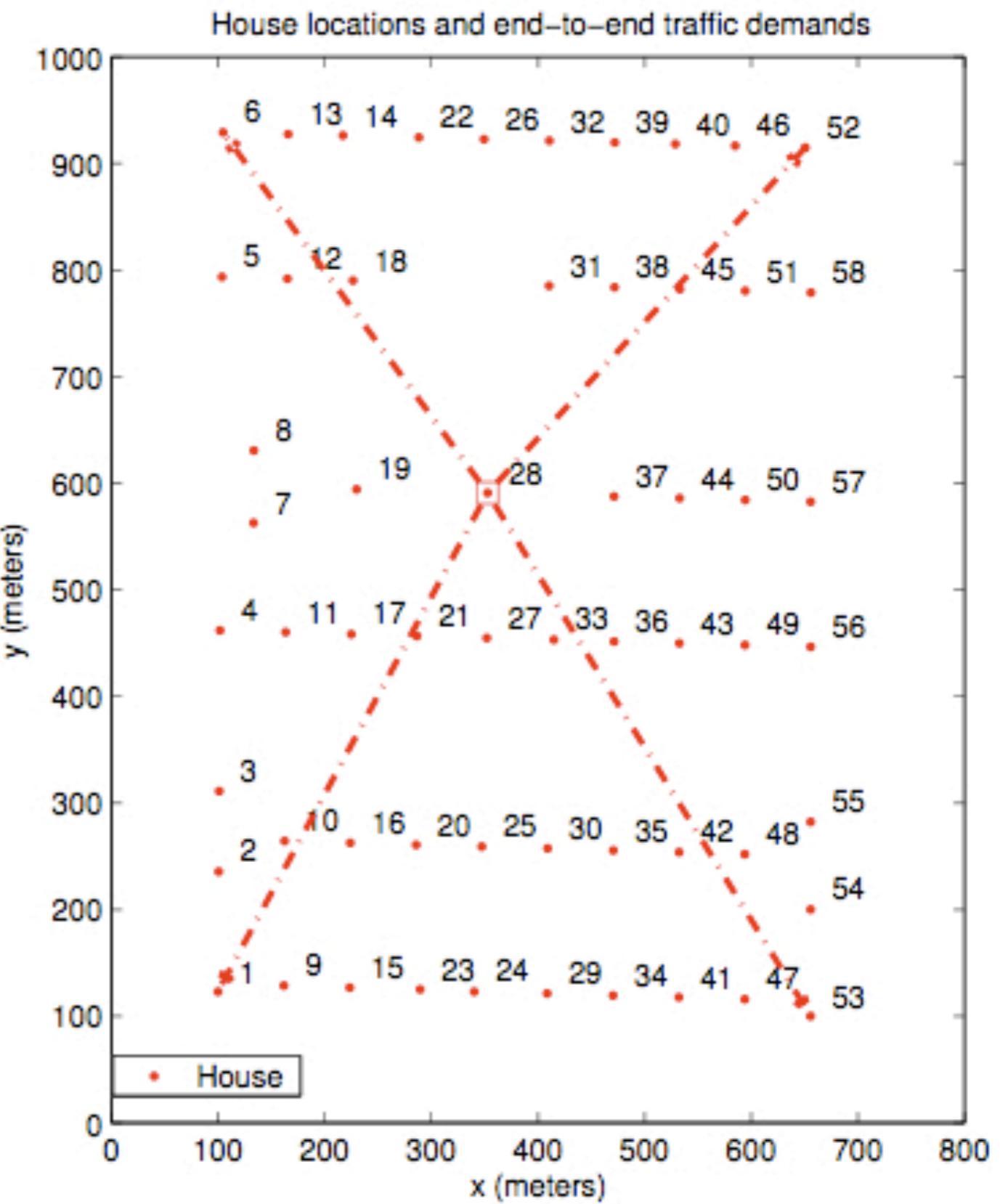


# Computational Complexity

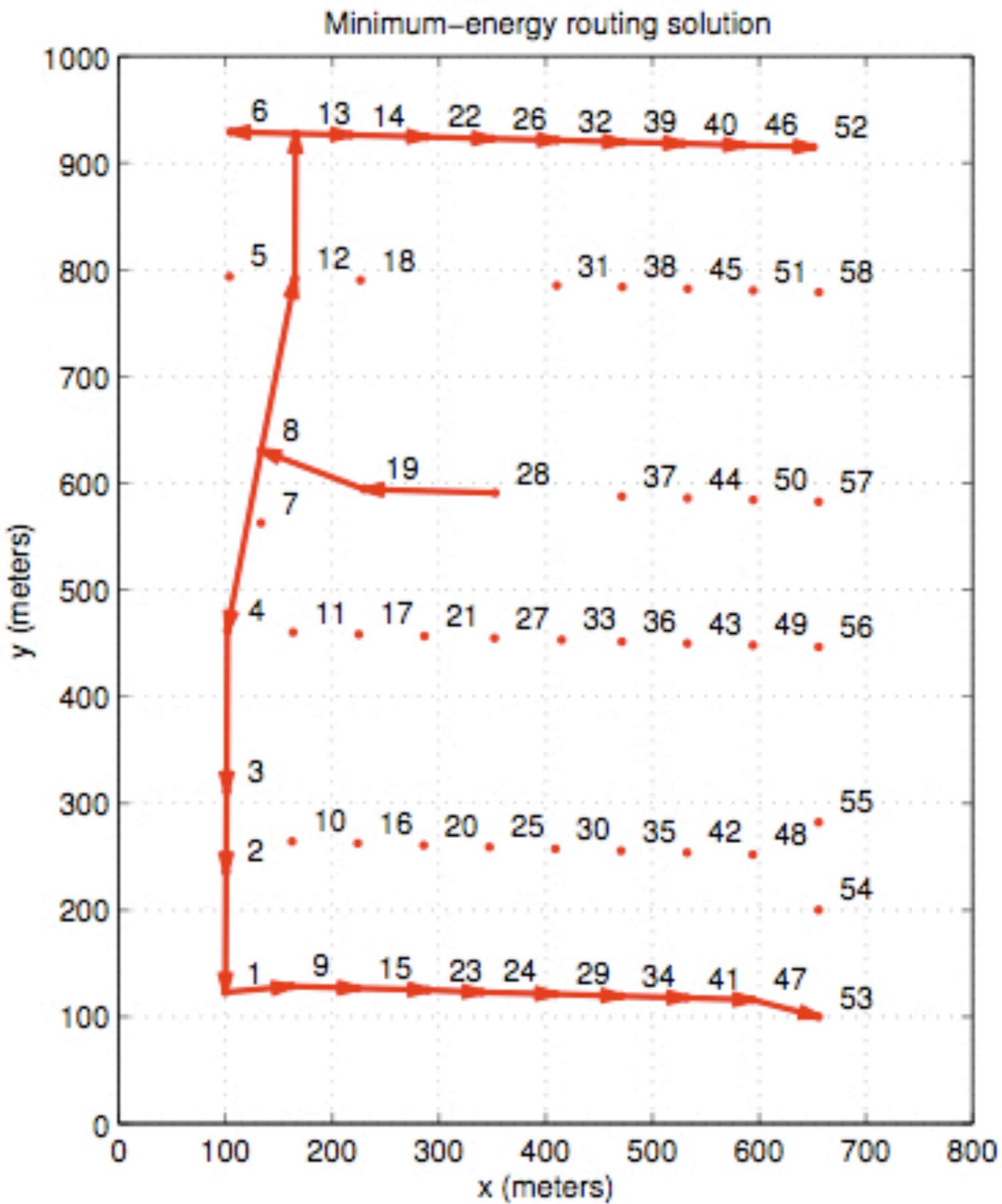
- ▶ **Algorithm**
  - Collect all available link information
  - Formulate as linear program
  - Approximation of the solution
- ▶ **With the help of network coding, the maximum throughput can be approximated arbitrarily well in polynomial time**

# Example Demand

Wu, Chou, Sun-Yuan,  
Minimum-Energy Multicast in Mobile Ad hoc  
Networks using Network Coding, 2006



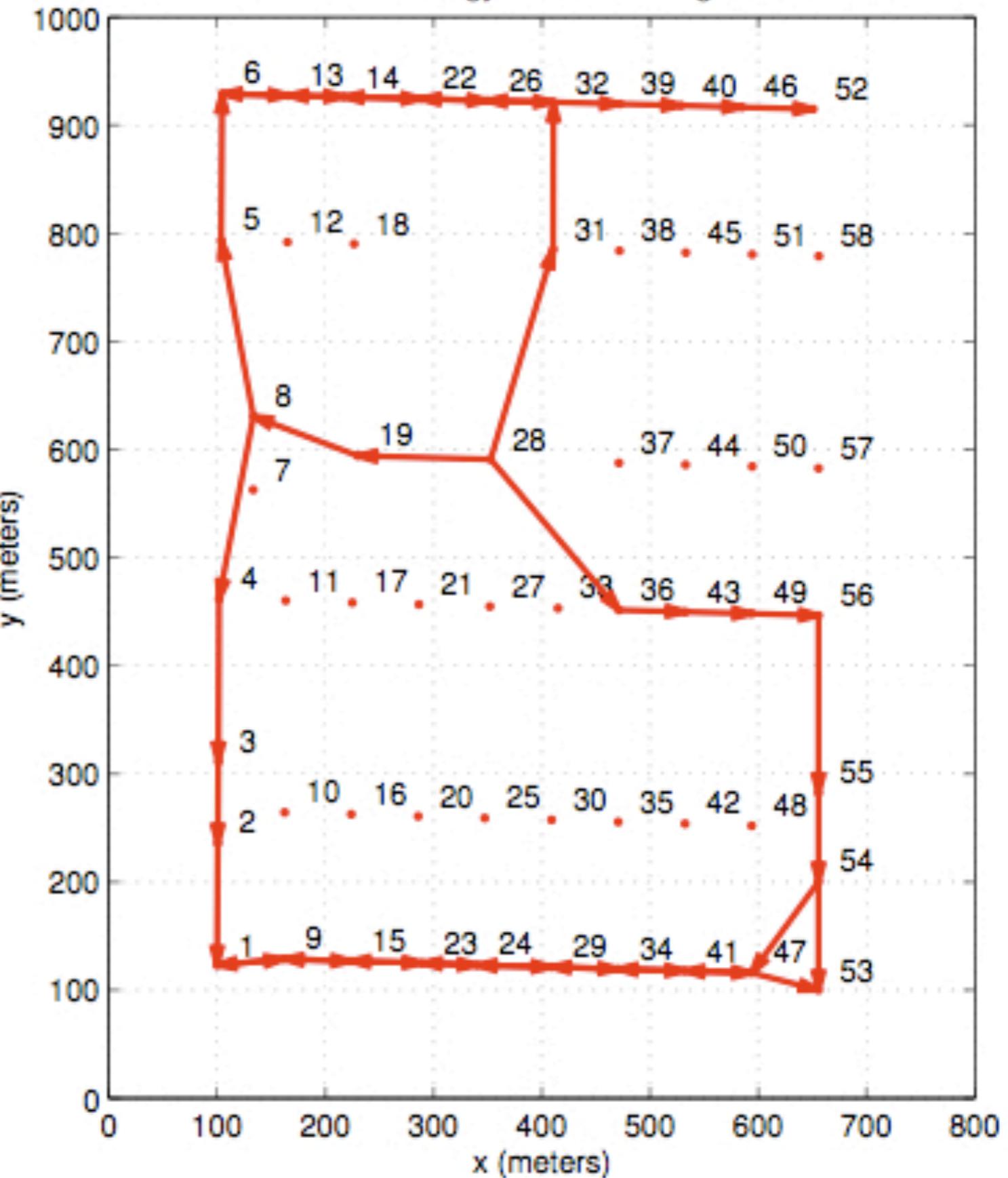
# Example Multicasting with minimal Energy



Wu, Chou, Sun-Yuan,  
Minimum-Energy Multicast in Mobile Ad hoc  
Networks using Network Coding, 2006

# Multicasting with Network Coding

Minimum-energy network coding solution



Wu, Chou, Sun-Yuan,  
Minimum-Energy Multicast in Mobile Ad hoc  
Networks using Network Coding, 2006

# Discussion

- ▶ **Options**
  - Energy model can customized
- ▶ **Limitations**
  - Network coding is not described
  - Central algorithm
  - Any change in the communication requires recalculation

# Xors in the Air

- ▶ **Katti, Hu, Katabi, Médard, Crowcroft**
  - XORs in the Air: Practical Wireless Network Coding
- ▶ **Problem**
  - Maximize throughput in ad-hoc network
  - Multihop messages cause interference
- ▶ **Solution**
  - Uses only XORs of multiple messages
  - Local, opportunistic algorithm

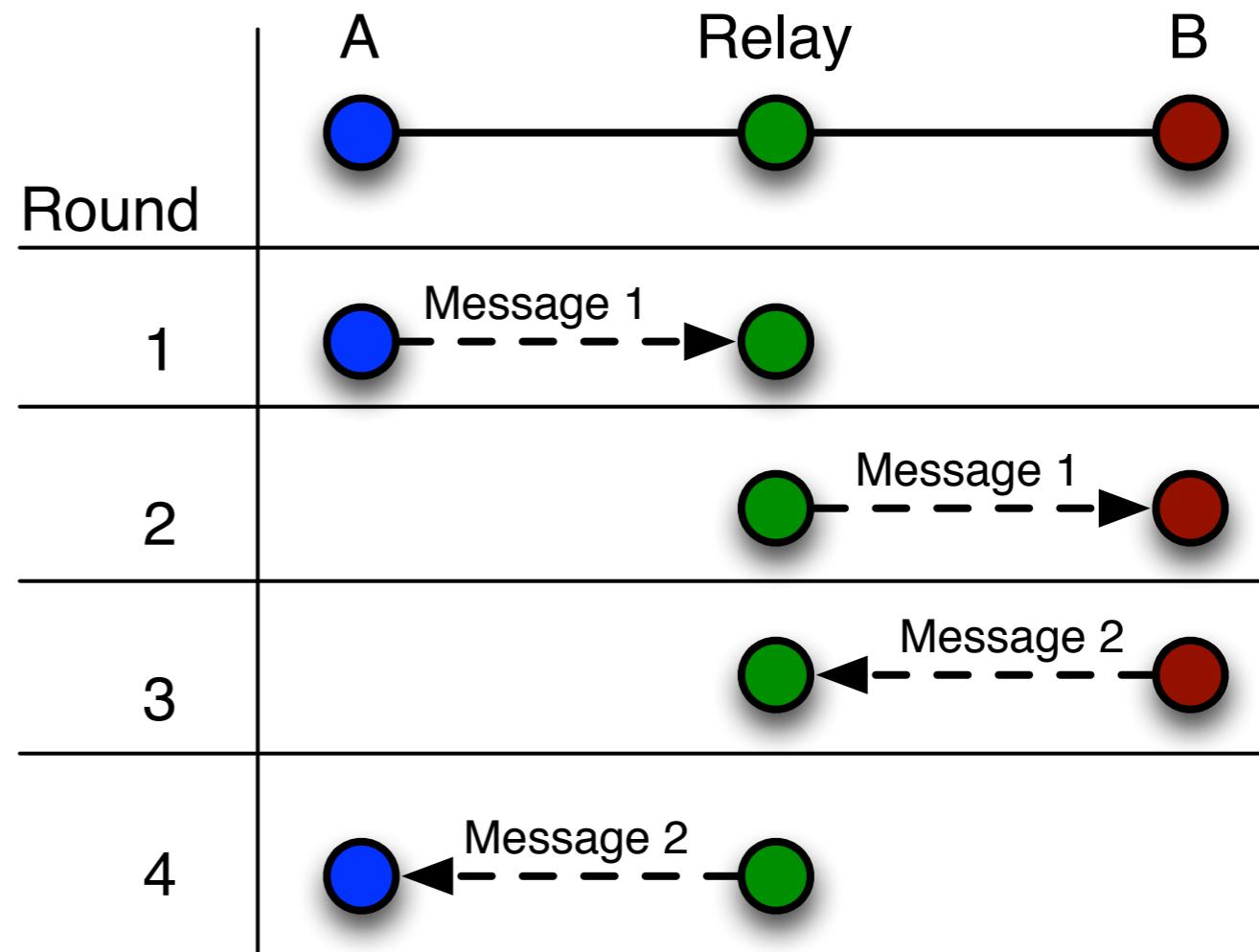
# Xors in the Air

## ► Problem

- Multihop messages cause interferences

## ► Example

- Traditional: 4 messages to send
  - a message from A to B
  - and a message from B to A



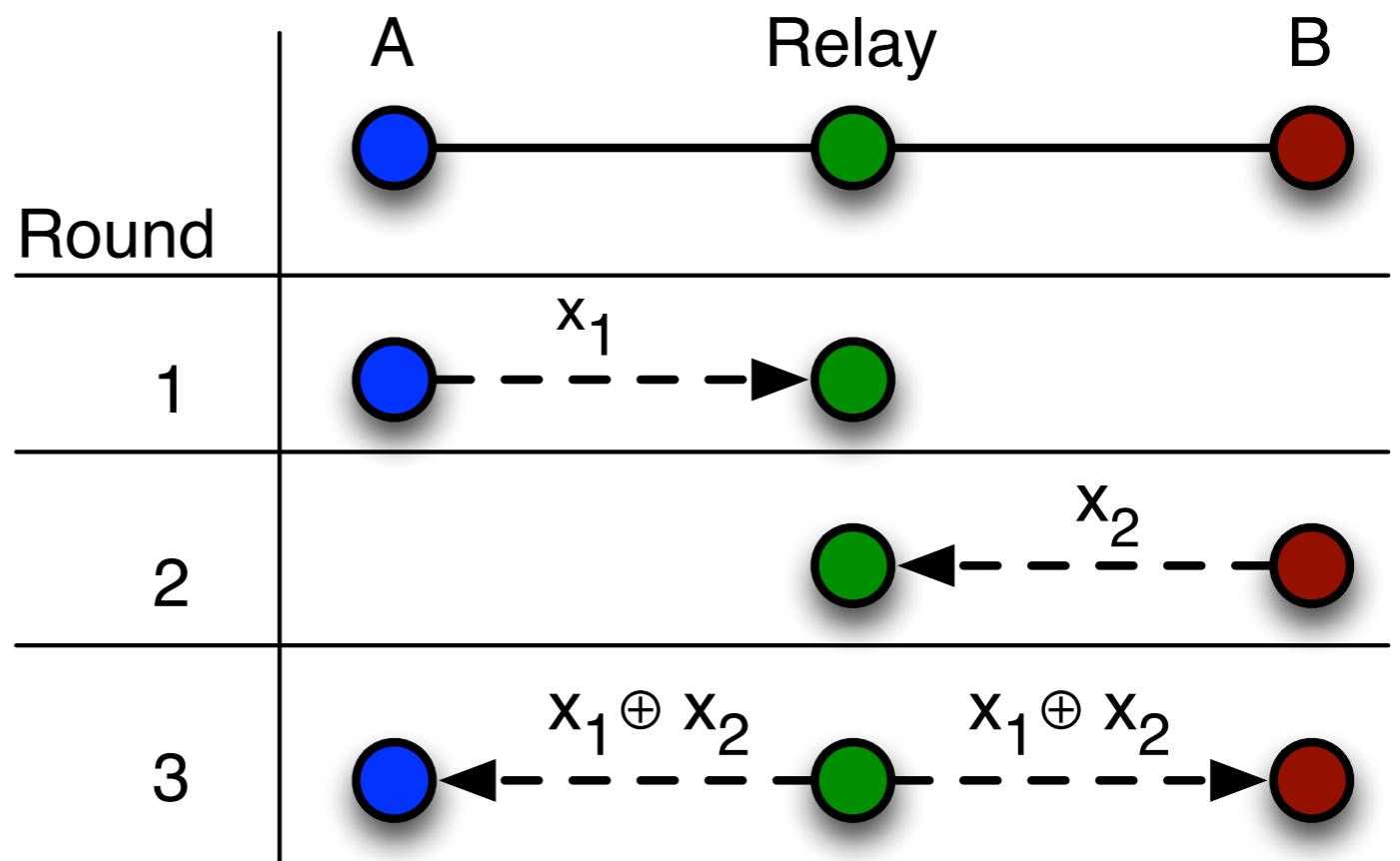
# Xors in the Air

## ► Problem

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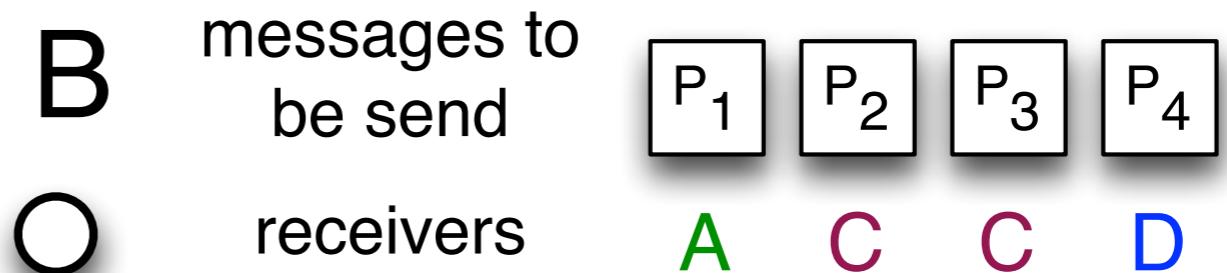
- Traditional: 4 messages to send
  - a message from A to B
  - and a message from B to A
- Network Coding
  - 3 messages suffice



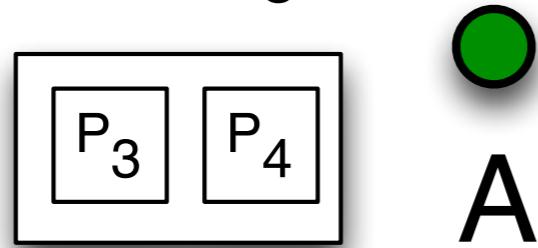
# Coding Opportunistically COPE

- ▶ **Consider of multiple communication paths**
  - Opportunistic coding of messages by Xor
- ▶ **Utilization of the broadcast medium**
  - listening to the channel
  - all (even foreign) messages are buffered
  - buffered messages are used for decoding
- ▶ **Context messages**
  - announcement of level of knowledge
  - neighbors can generate code adapted to the receiver's knowledge
- ▶ **Guess the level of knowledge of neighbors**

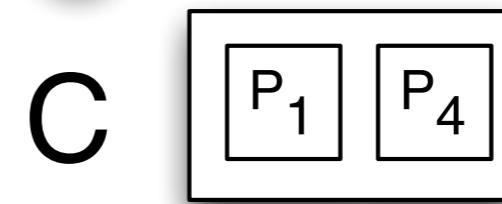
# Opportunistic Coding



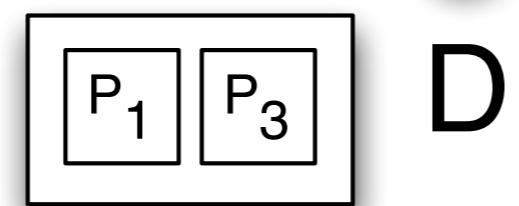
known messages



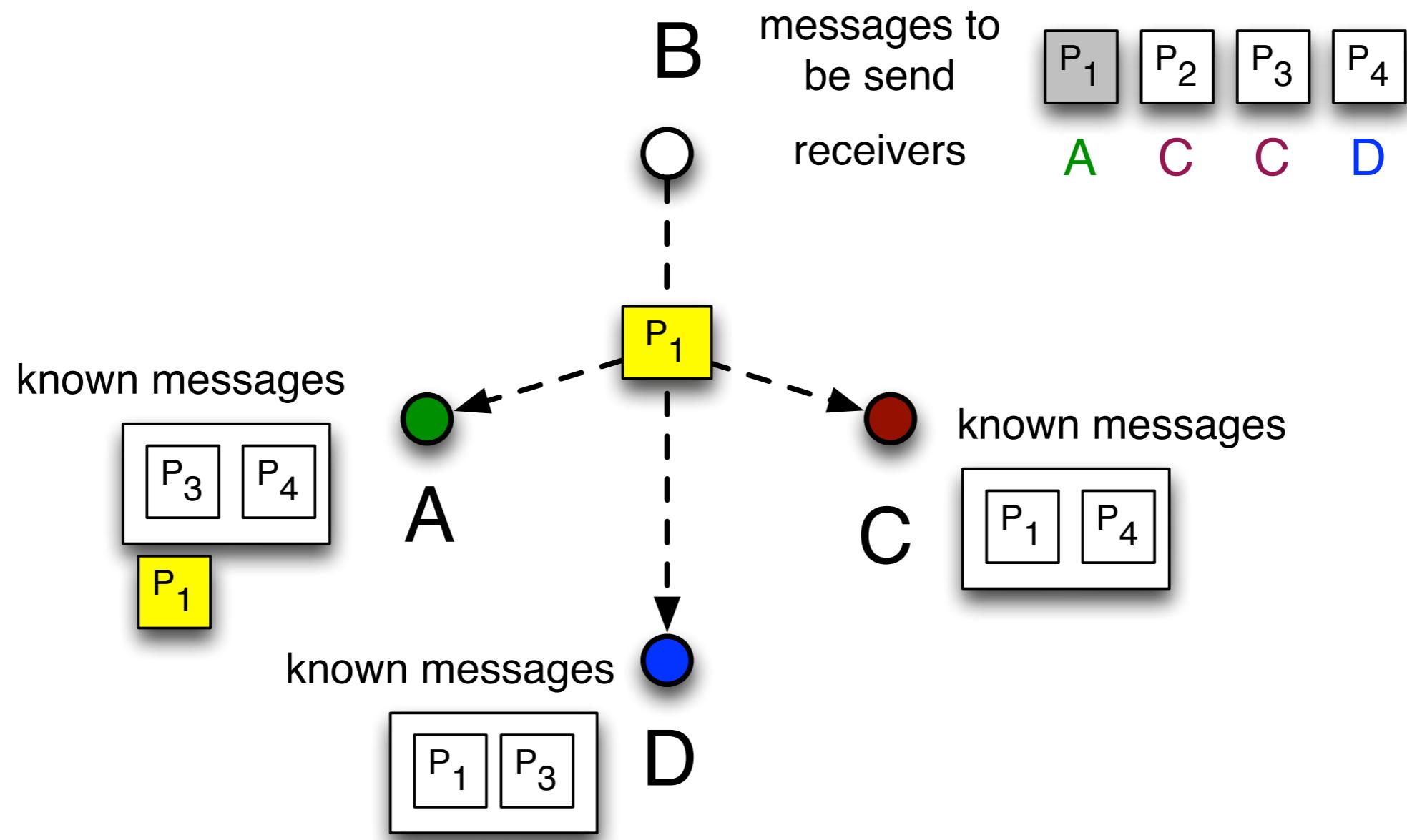
known messages



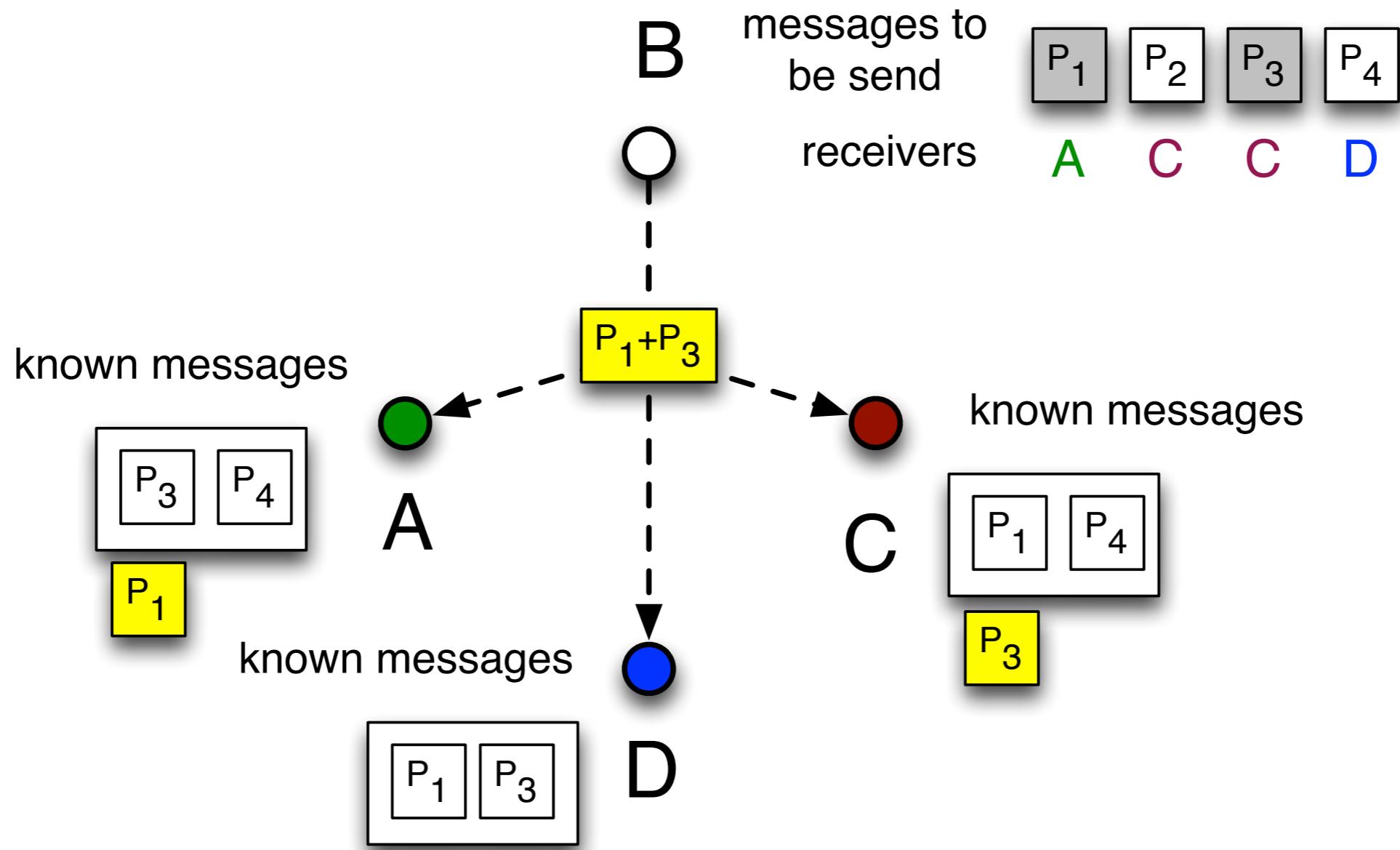
known messages



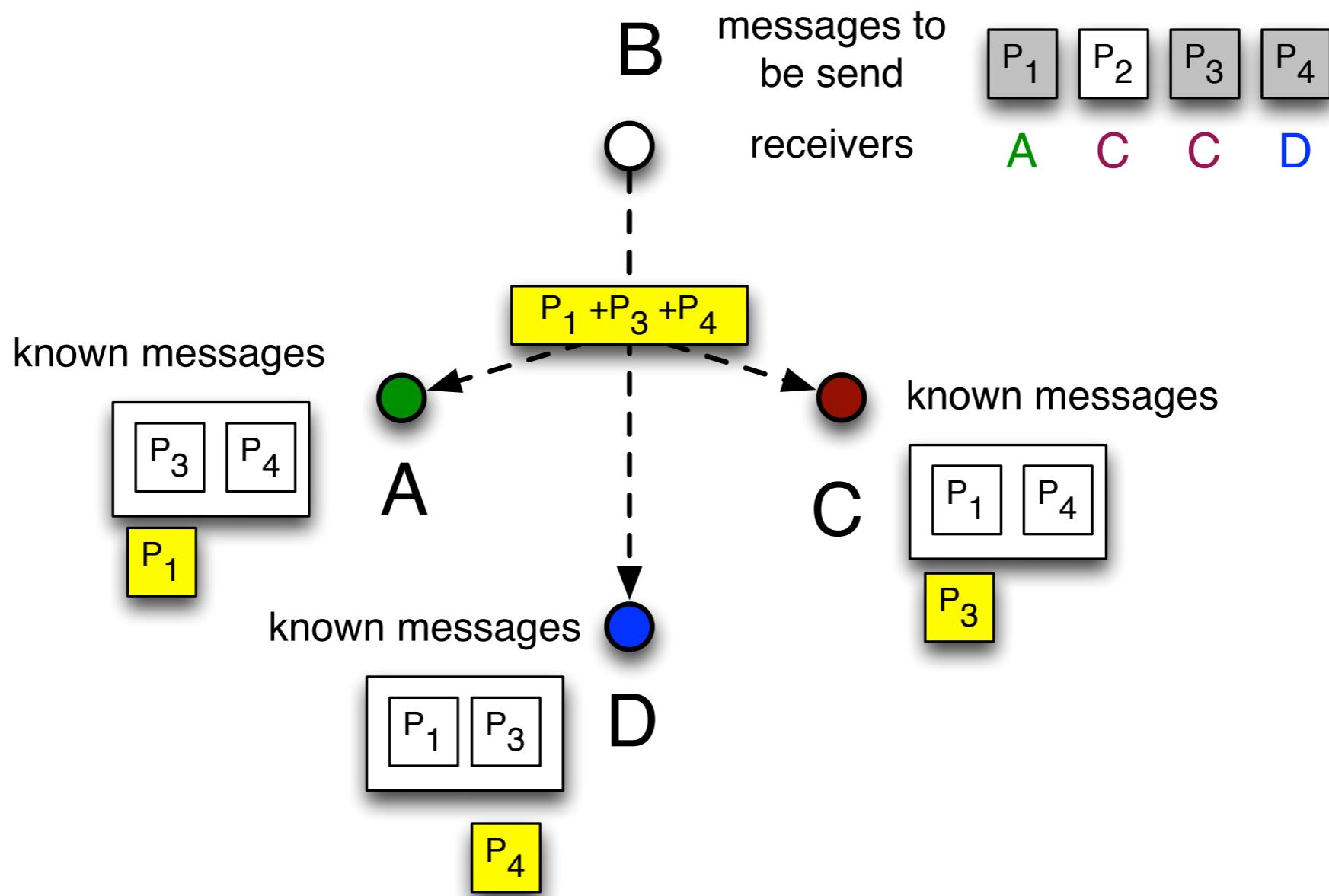
# Opportunistic Coding



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# Coding Gain

**3-chain**



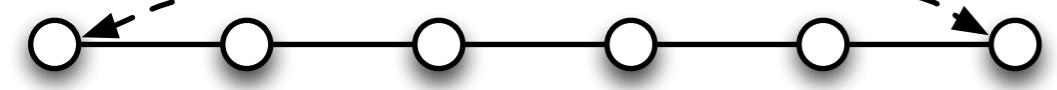
X



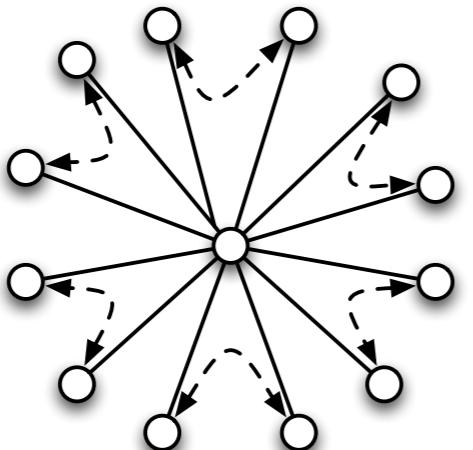
**Cross**



**Infinite Chain**

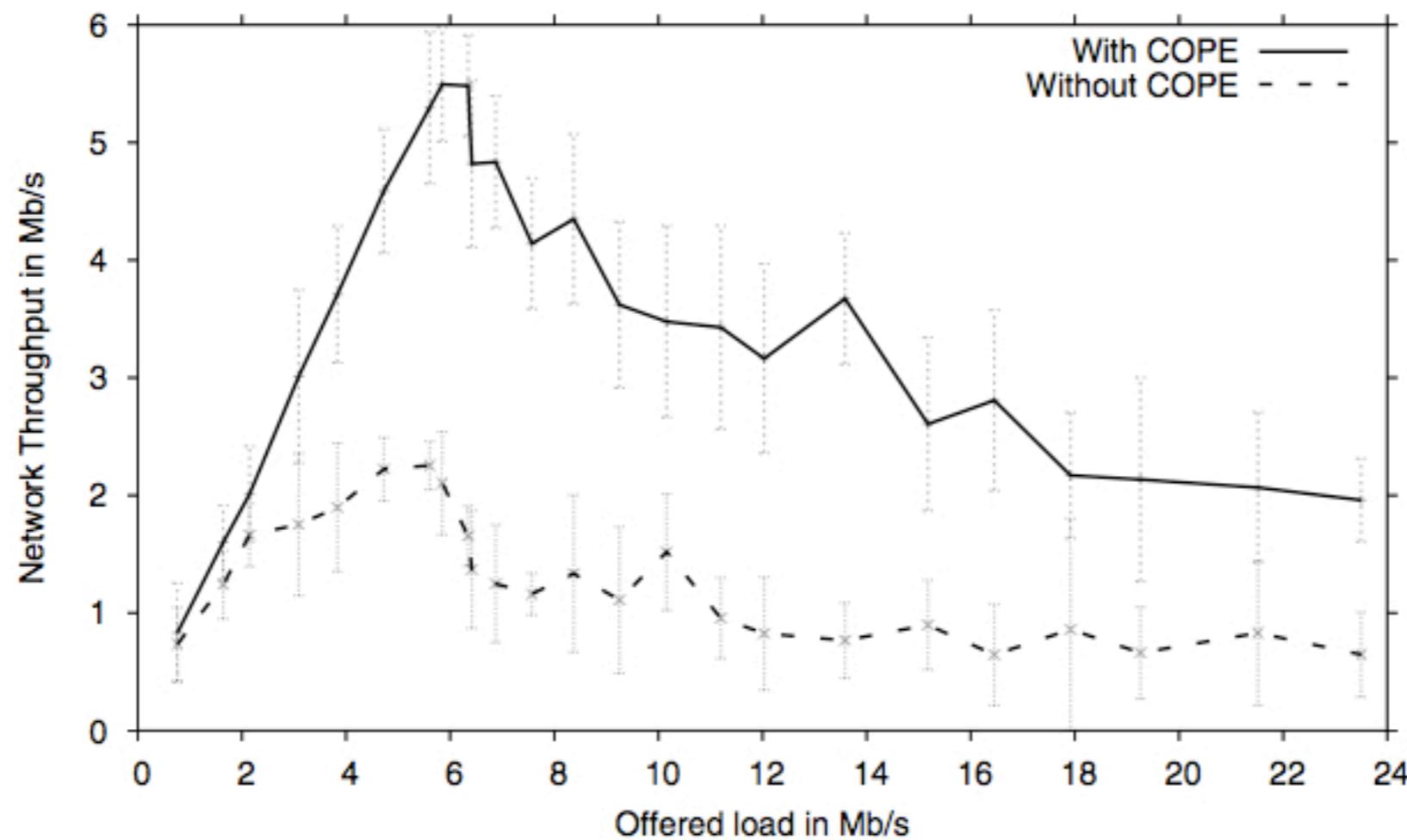


**Infinite Wheel**



Topology	Coding Gain
3-chain	1,333...
X	1,333...
Cross	1,666...
Infinite Chain	2
Infinite Wheel	2

# Summary Network Coding



**Figure 12**—COPE can provide a several-fold (3-4x) increase in the throughput of wireless Ad hoc networks. Results are for UDP flows with randomly picked source-destination pairs, Poisson arrivals, and heavy-tail size distribution.

Wu, Chou, Sun-Yuan, Minimum-Energy Multicast in Mobile Ad hoc Networks using Network Coding, 2006

# Network Coding

## ► **Benefit**

- Network throughput can be increased
  - COPE
- Reduction of energy consumption
- Higher robustness, small error rate
- Applications in peer-to-peer networks, wireless sensor networks

## ► **Problems**

- complex encoding
- sometimes high computational cost
- difficult organization



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