

### Peer-to-Peer Networks 03 CAN (Content Addressable Network)

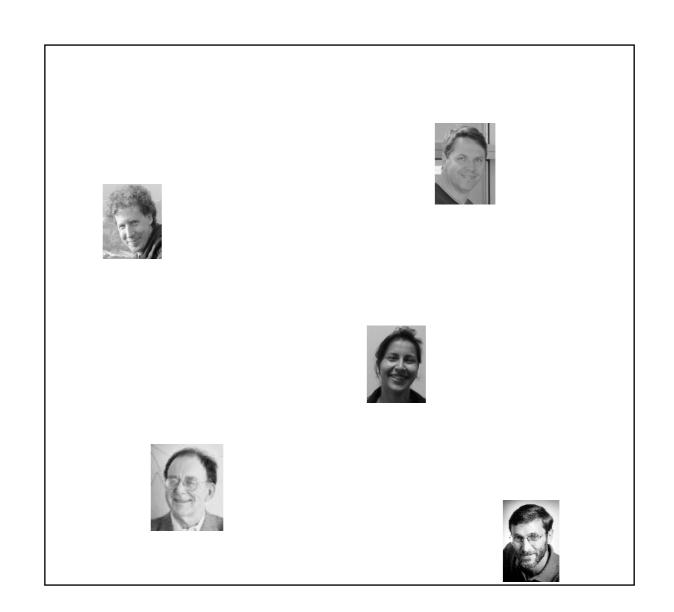
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### CAN Playground

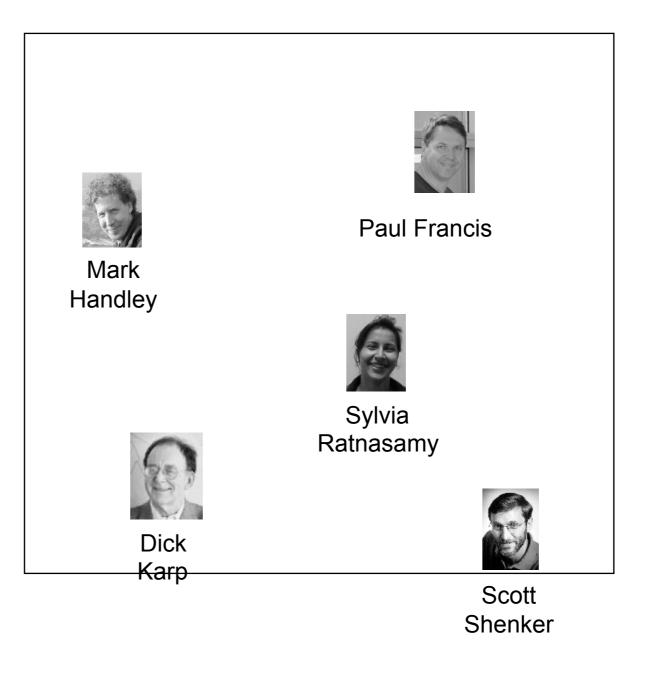
- Index entries are mapped to the square [0,1]<sup>2</sup>
  - using two hash functions to the real numbers
  - according to the search key
- Assumption:
  - hash functions
    behave a like
    a random
    mapping





### CAN Index Entries

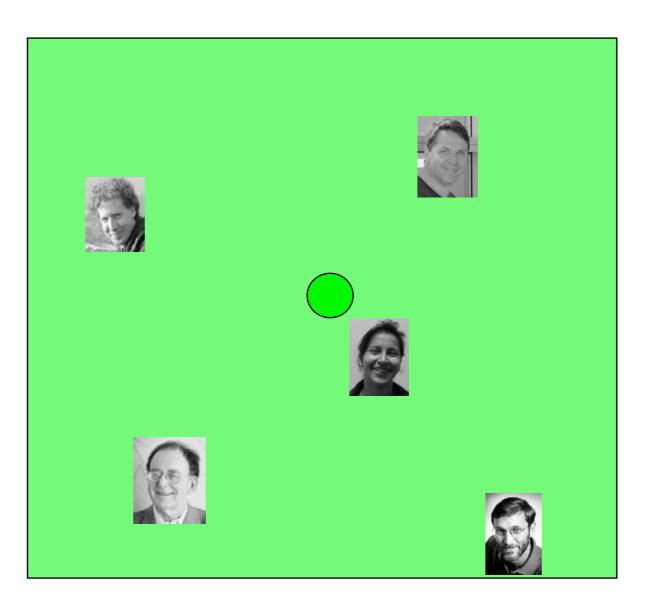
- Index entries are mapped to the square [0,1]2
  - using two hash functions to the real numbers
  - according to the search key
- Assumption:
  - hash functions behave a like a random mapping
- Literature
  - Ratnasamy, S., Francis, P., Handley, M., Karp, R., Shenker, S.: A scalable content-addressable network.
     In: Computer Communication Review. Volume 31., Dept. of Elec. Eng. and Comp. Sci., University of California, Berkeley (2001) 161–172





## First Peer in CAN

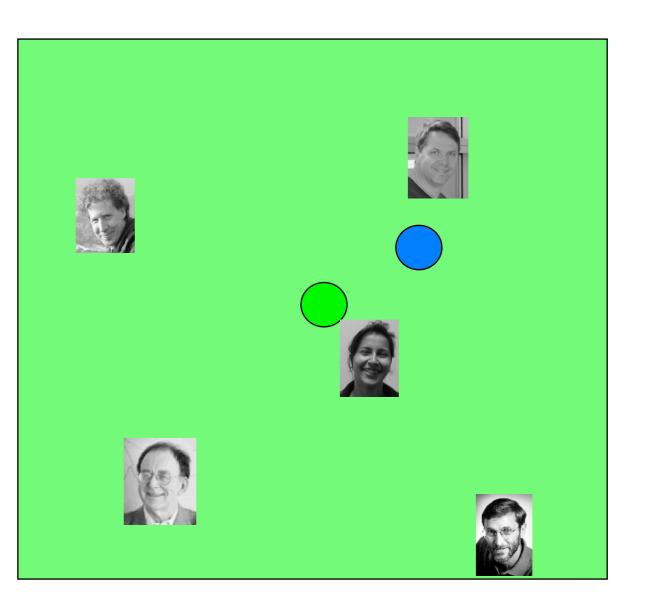
- In the beginning there is one peer owning the whole square
- All data is assigned to the (green) peer





## CAN: The 2nd Peer Arrives

- The new peer chooses a random point in the square
  - or uses a hash function applied to the peers Internet address
- The peer looks up the owner of the point
  - and contacts the owner

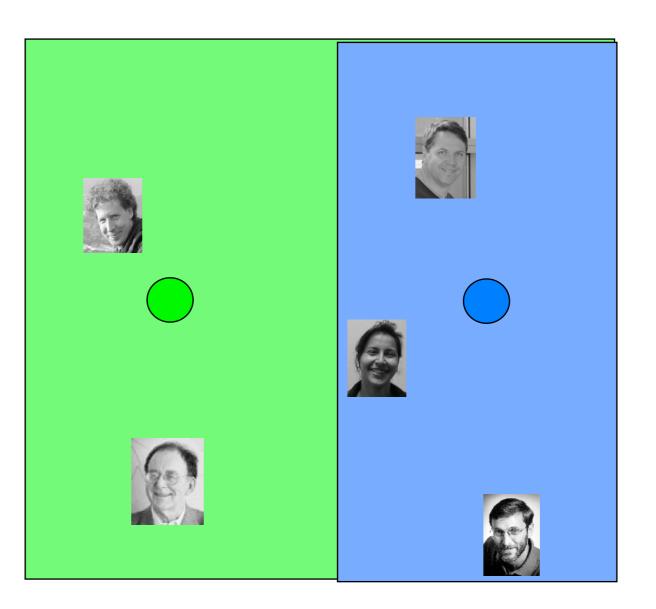


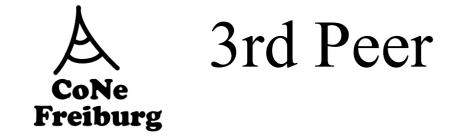
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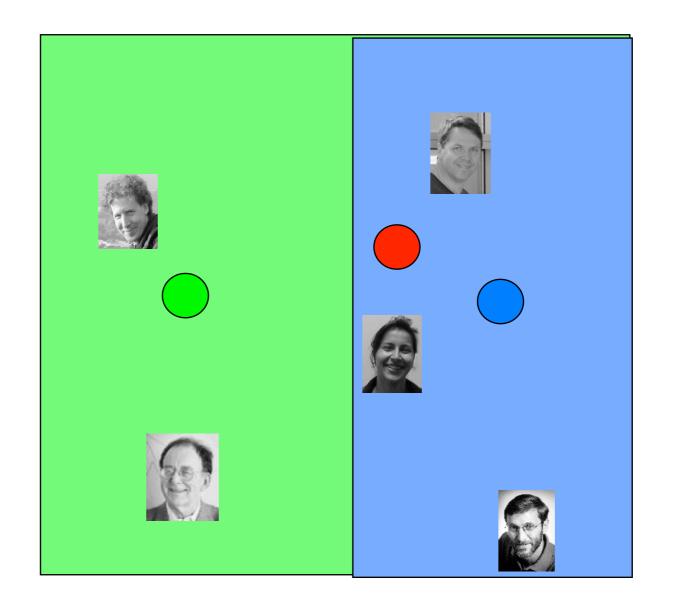


# CAN: 2nd Peer Has Settled Down

- The new peer chooses a random point in the square
  - or uses a hash function applied to the peers Internet address
- The peer looks up the owner of the point
  - and contacts the owner
- The original owner divides his rectangle in the middle and shares the data with the new peer

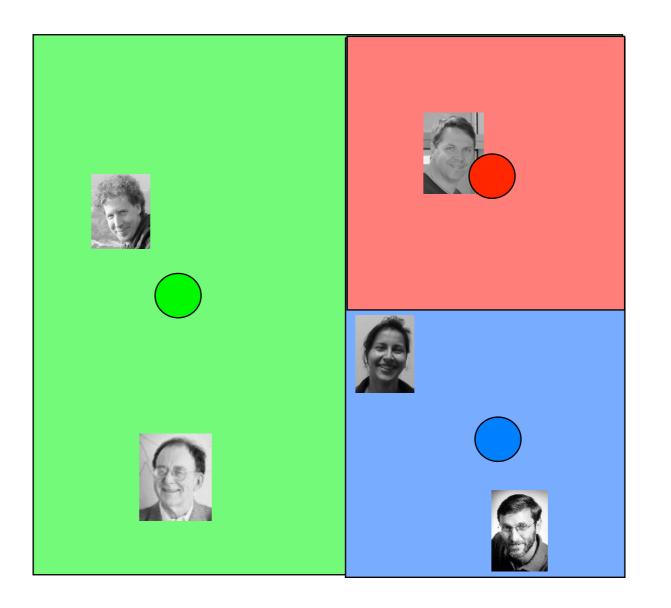






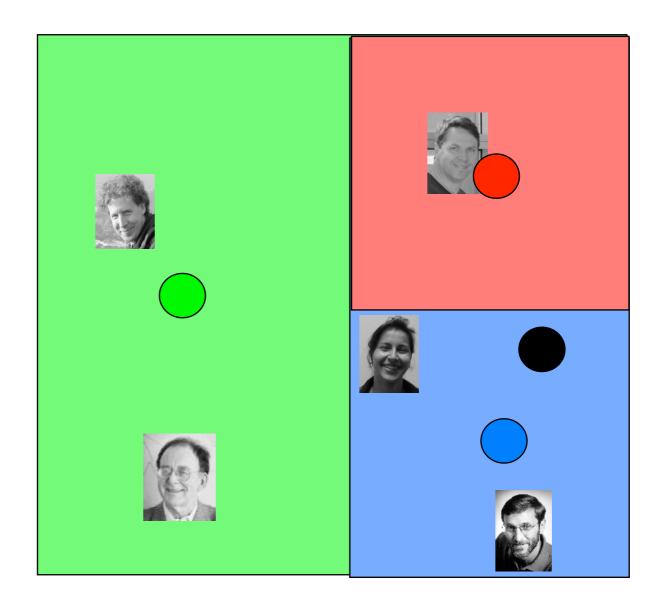


### CAN: 3rd Peer



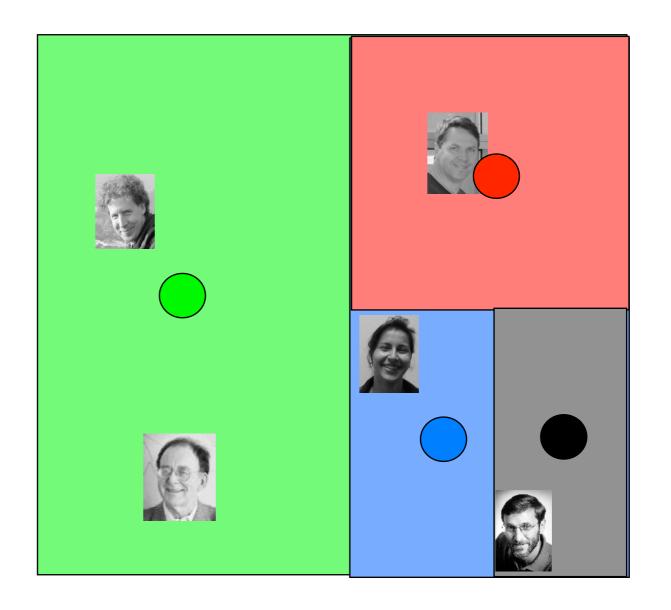


### CAN: 4th Peer





## CAN: 4th Peer Added

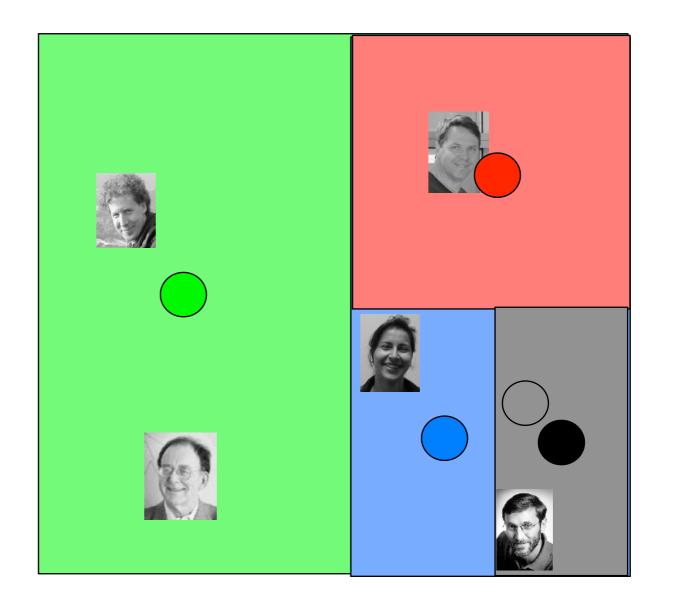




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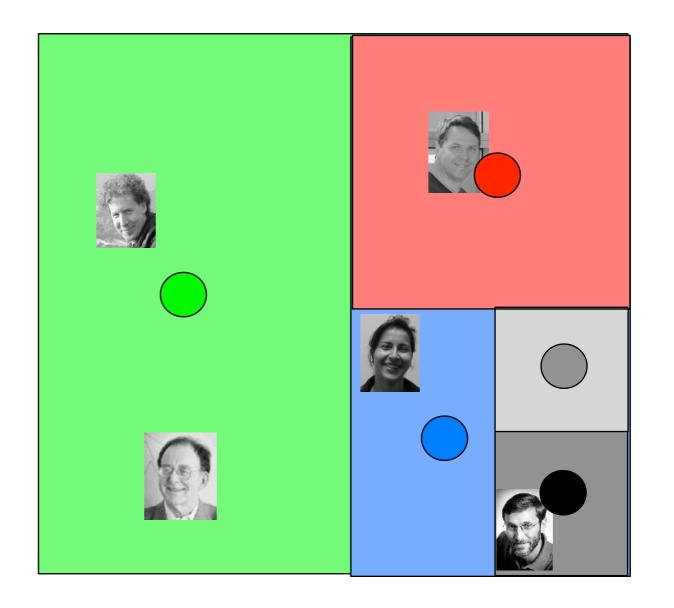


## CAN: 5th Peer





## CAN: All Peers Added



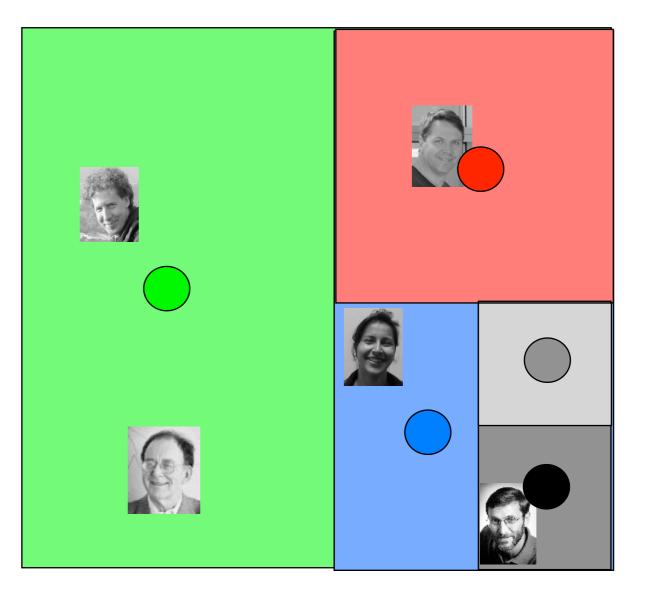




# On the Size of a Peer's Area

- R(p): rectangle of peer p
- A(p): area of the R(p)
- n: number of peers
- area of playground square: 1
- Lemma
  - For all peers we have  $E[A(p)] = \frac{1}{n}$
- Lemma
  - Let P<sub>R,n</sub> denote the probability that no peers falls into an area R. Then we have

 $P_{R,n} \le e^{-n\operatorname{Vol}(R)}$ 



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#### An Area Not being Hit

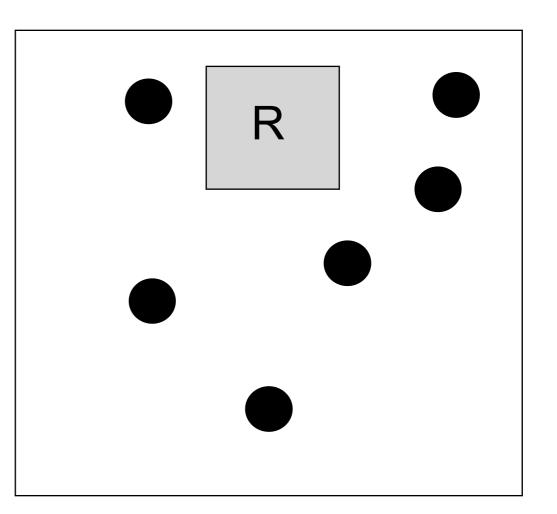
#### Lemma

- Let  $P_{R,n}$  denote the probability that no peers falls into an area R. Then  $P_{R,n} \leq e^{-n\operatorname{Vol}(R)}$ 

Proof

- Let x=Vol(R)
- The probability that a peer does not fall into R is 1 x
- The probability that n peers do not fall into R is  $(1-x)^n$
- So, the probability is bounded by m > 1 :  $\left(1 - \frac{1}{m}\right)^m \le \frac{1}{e}$
- because

$$(1-x)^n = ((1-x)^{\frac{1}{x}})^{nx} \le e^{-nx}$$





# How Fair Are the Data Balanced

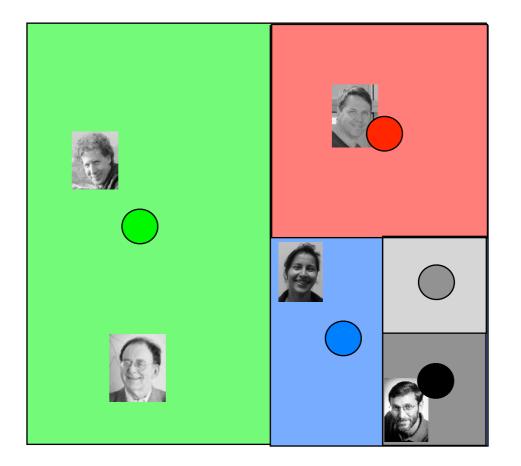
- Lemma
  - With probability n<sup>-c</sup> a rectangle of size (c ln n)/n is not further divided
- Proof
  - Let  $P_{R,n}$  denote the probability that no peers falls into an area R. Then we have

 $P_{R,n} \le e^{-n\operatorname{Vol}(R)}$ 

- Every peer receives at most c (ln n) m/n elements
  - if all m elements are stored equally distributed over the area
- While the average peer stores m/n elements

 $P_{R,n} \le e^{-n\frac{c\ln n}{n}} = e^{-c\ln n} = n^{-c}$ 

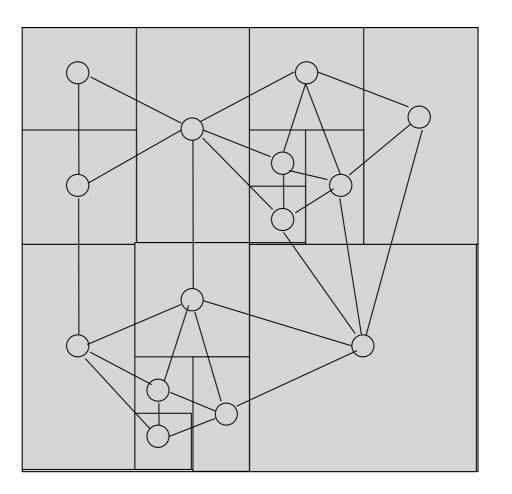
 So, the number of data stored on a peer is bounded by c (ln n) times the average amount





## Network Structure of CAN

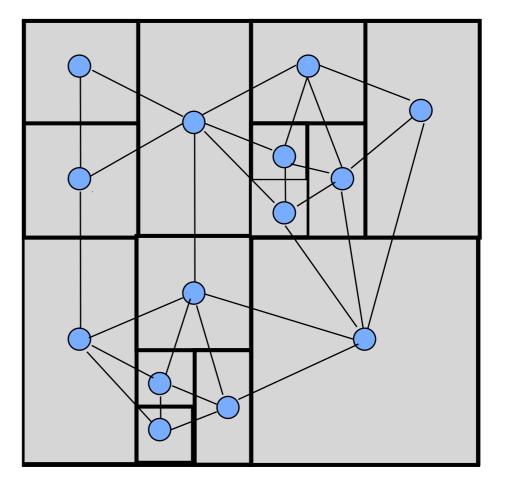
- Let d be the dimension of the square, cube, hyper-cube
  - 1: line
  - 2: square
  - 3: cube
  - 4: ...
- Peers connect
  - if the areas of peers share a (d-1)-dimensional area
  - e.g. for d=2 if the rectangles touch by more than a point





## Lookup in CAN

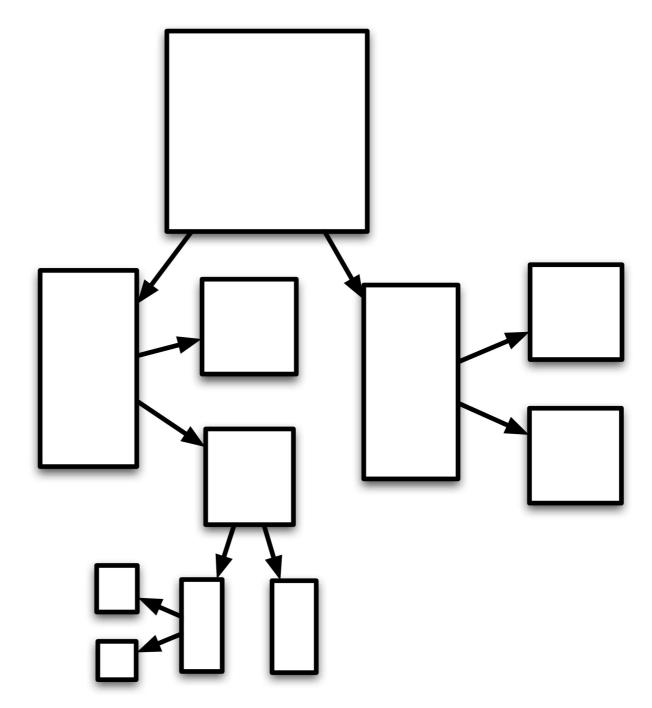
- Compute the position of the index using the hash function on the key value
- Forward lookup to the neighbored peer which is closer to the index
- Expected number of hops for CAN in d dimensions:
  - $O(n^{1/d})$
- Average degree of a node
  - -O(d)





# Insertions in CAN = Random Tree

- Random Tree
  - new leaves are inserted randomly
  - if node is internal then flip coin to forward to left or right sub-tree
  - if node is leaf then insert two leafs to this node
- Depth of Tree
  - in the expectation: O(log n)
  - Depth O(log n) with high probability, i.e. 1-n<sup>-c</sup>
- Observation
  - CAN inserts new peers like leafs in a random tree

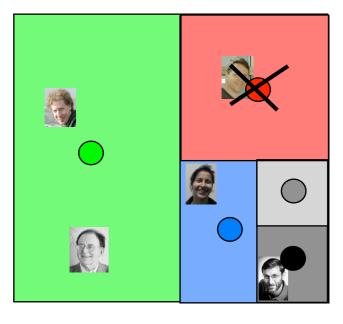


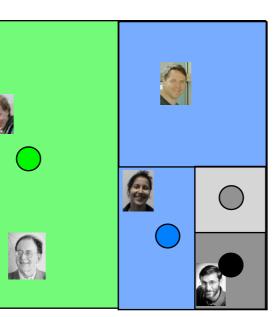
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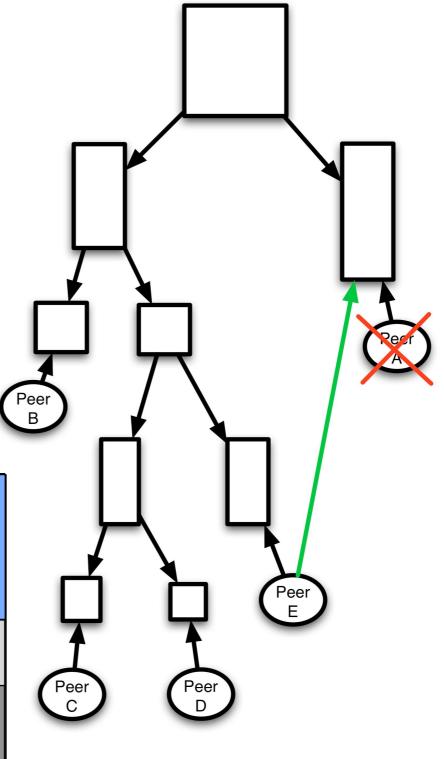


## Leaving Peers in CAN

- If a peer leafs
  - he does not announce it
- Neighbors continue testing on the neighborhood
  - to find out whether peer has left
  - the first neighboir who finds a missing neighbor takes over the area of the missing peer
- Peers can be responsible for many rectangles
- Repeated insertions and deletions of peers leed to fragmentation



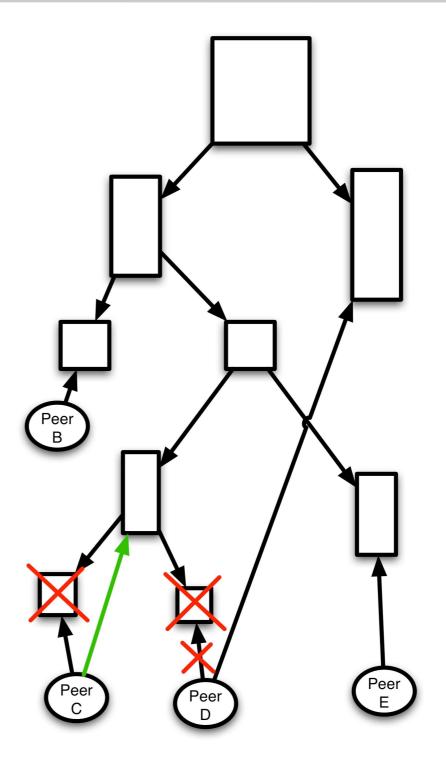






# Defragmentation — The Simple Case

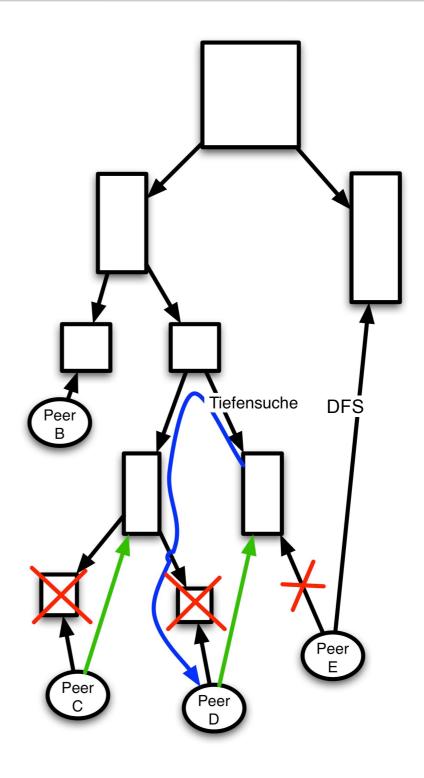
- To heal fragmented areas
  - from time to to time areas are freshly assigned
- Every peer with at least two zones
  - erases smalles zone
  - finds replacement peer for this zone
- Ist case: neighboring zone is undivided
  - both peers are leafs in the random tree
  - transfer zone to the neighbor





# Defragmentation — The Difficult Case

- Every peer with at least two zones
  - erases smalles zone
  - finds replacement peer for this zone
- 2nd case: neighboring zone is further divided
  - Perform DFS (depth first search) in neighbor tree until two neighbored leafs are found
  - Transfer the zone to one leaf which gives up his zone
  - Choose the other leaf to receive the latter zone



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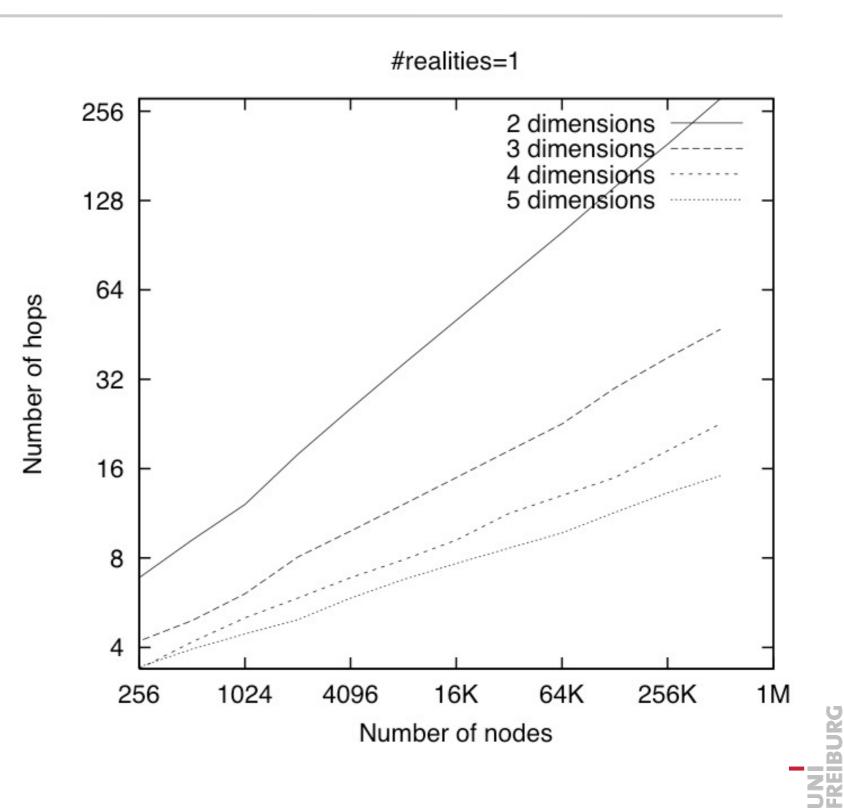
# Improvements for CAN

- More dimensions
- Multiples realities
- Distance metric for routing
- Overloading of zones
- Multiple hasing
- Topology adapted network construction
- Fairer partitioning
- Caching, replication and hot-spot management



### Higher Dimensions

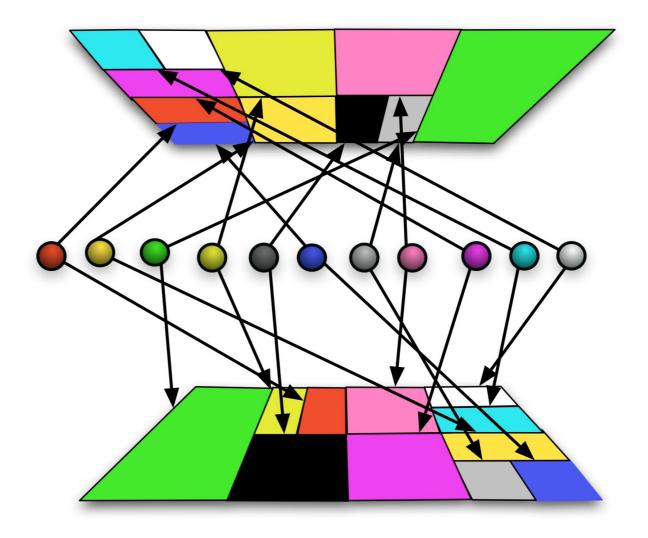
- Let d be the dimension of the square, cube, hypercube
  - 1: line
  - 2: square
  - 3: cube
  - 4: ...
- The expected path length is O(n<sup>1/d</sup>)
- Average number of neighbors O(d)





### More Realities

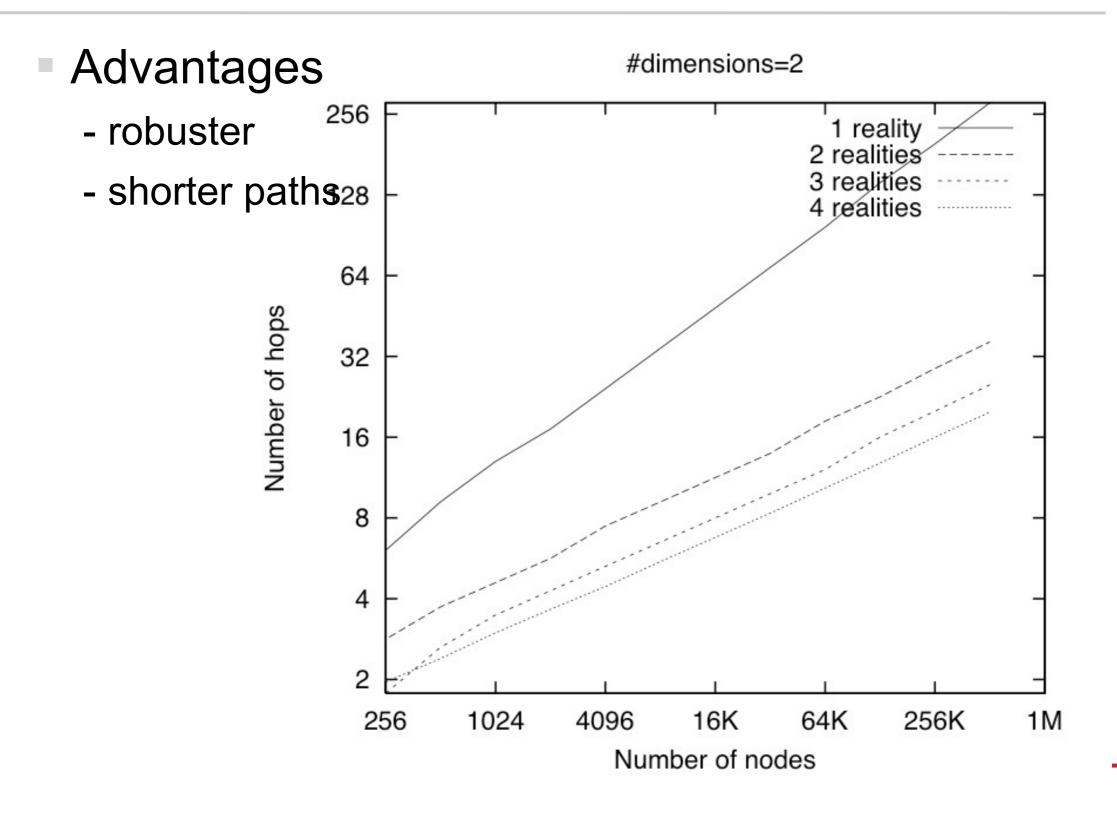
- Build simultanously r CANs with the same peers
- Each CAN is called a *reality*
- For lookup
  - greedily jump between realities
  - choose reality with the closest distance to the target
- Advantanges
  - robuster network
  - faster search



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### More Realities

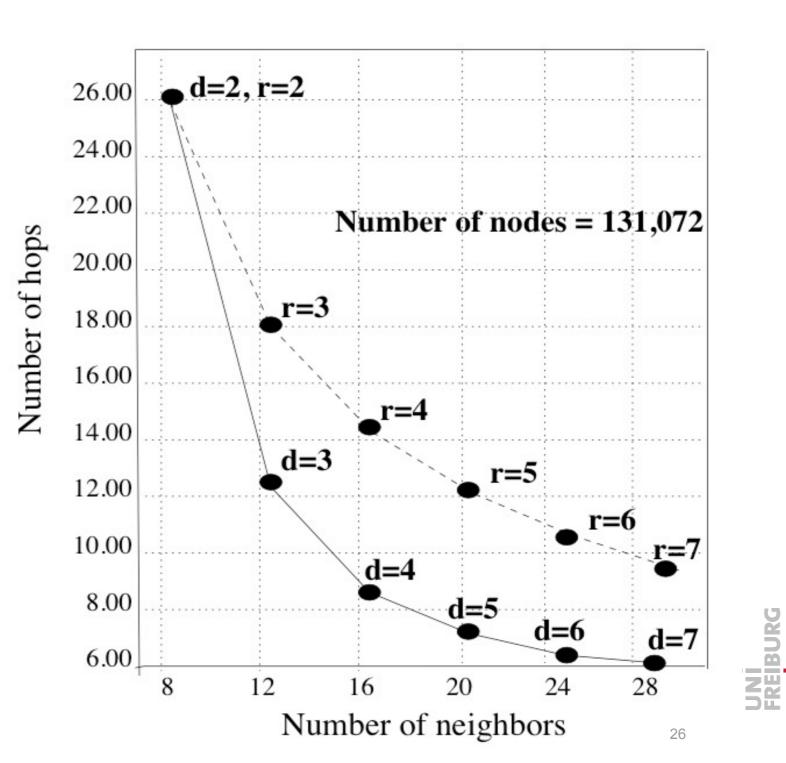




- Dimensionens reduce the lookup path length more effciently
- Realities
  produce more
  robust networks

increasing dimensions, #realities=2

increasing realities, #dimensions=2





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