



# Peer-to-Peer Networks

## 05 Pastry

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- Antony Rowstron
  - Microsoft Research, Cambridge, GB
- Developed in Cambridge (Microsoft Research)
- Pastry
  - Scalable, decentralized object location and routing for large scale peer-to-peer-network
- PAST
  - A large-scale, persistent peer-to-peer storage utility
- Two names one P2P network
  - PAST is an application for Pastry enabling the full P2P data storage functionality
  - We concentrate on Pastry

- Each peer has a 128-bit ID: nodeID
  - unique and uniformly distributed
  - e.g. use cryptographic function applied to IP-address
- Routing
  - Keys are matched to  $\{0,1\}^{128}$
  - According to a metric messages are distributed to the neighbor next to the target
- Routing table has  $O(2^b(\log n)/b) + \ell$  entries
  - n: number of peers
  - $\ell$ : configuration parameter
  - b: word length
    - typical: b= 4 (base 16),  
 $\ell = 16$
    - message delivery is guaranteed as long as less than  $\ell/2$  neighbored peers fail
- Inserting a peer and finding a key needs  $O((\log n)/b)$  messages

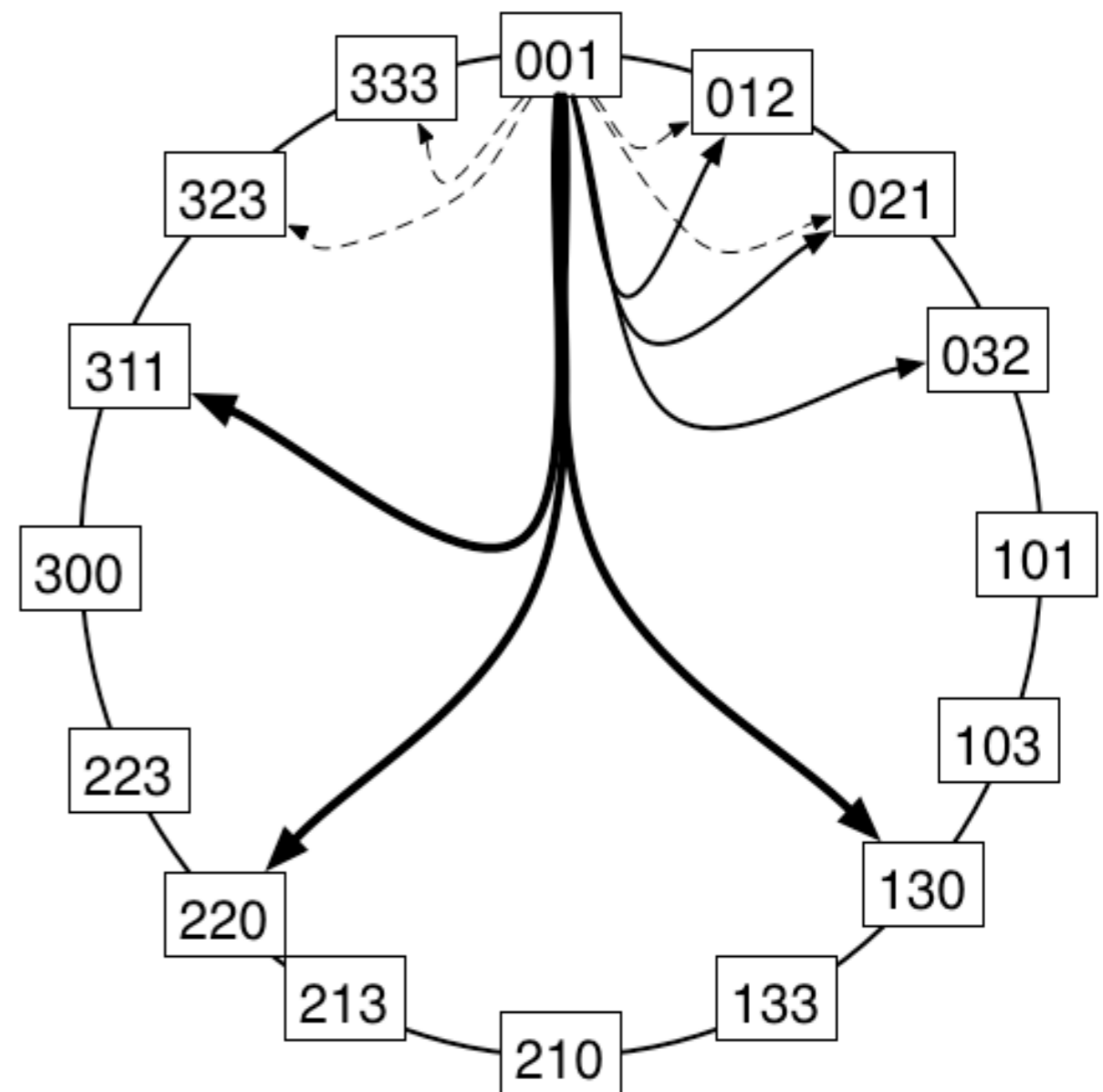
# Routing Table

- NodeID presented in base  $2^b$ 
  - e.g. NodeID: 65A0BA13
- For each prefix  $p$  and letter  $x \in \{0, \dots, 2^b - 1\}$  add an peer of form  $px^*$  to the routing table of NodeID, e.g.
  - $b=4, 2^b=16$
  - 15 entries for  $0^*, 1^*, \dots, F^*$
  - 15 entries for  $60^*, 61^*, \dots, 6F^*$
  - ...
  - if no peer of the form exists, then the entry remains empty
- Choose next neighbor according to a distance metric
  - metric results from the RTT (round trip time)
- In addition choose  $\ell$  neighbors
  - $\ell/2$  with next higher ID
  - $\ell/2$  with next lower ID

<i>0</i>	<i>1</i>	<i>2</i>	<i>3</i>	<i>4</i>	<i>5</i>		<i>7</i>	<i>8</i>	<i>9</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>e</i>	<i>f</i>	
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<i>6</i>	<i>6</i>	<i>6</i>	<i>6</i>	<i>6</i>	<i>6</i>	<i>6</i>	<i>6</i>	<i>6</i>	<i>6</i>		<i>6</i>	<i>6</i>	<i>6</i>	<i>6</i>	<i>6</i>	
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<i>a</i>		<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	<i>a</i>	
<i>0</i>		<i>2</i>	<i>3</i>	<i>4</i>	<i>5</i>	<i>6</i>	<i>7</i>	<i>8</i>	<i>9</i>	<i>a</i>	<i>b</i>	<i>c</i>	<i>d</i>	<i>e</i>	<i>f</i>	
<i>x</i>		<i>x</i>	<i>x</i>	<i>x</i>	<i>x</i>	<i>x</i>	<i>x</i>	<i>x</i>	<i>x</i>	<i>x</i>	<i>x</i>	<i>x</i>	<i>x</i>	<i>x</i>	<i>x</i>	

# Routing Table

- Example  $b=2$
- Routing Table
  - For each prefix  $p$  and letter  $x \in \{0, \dots, 2^b - 1\}$  add an peer of form  $px^*$  to the routing table of NodeID
- In addition choose  $\ell$  neighbors
  - $\ell/2$  with next higher ID
  - $\ell/2$  with next lower ID
- Observation
  - The leaf-set alone can be used to find a target
- Theorem
  - With high probability there are at most  $O(2^b (\log n)/b)$  entries in each routing table



# Routing Table

- Theorem

- With high probability there are at most  $O(2^{(1+\epsilon)(\log n)/b})$  entries in each routing table

- Proof

- The probability that a peer gets the same m-digit prefix is  $2^{-bm}$
- The probability that a m-digit prefix is unused is

$$(1 - 2^{-bm})^n \leq e^{-n/2^{bm}}$$

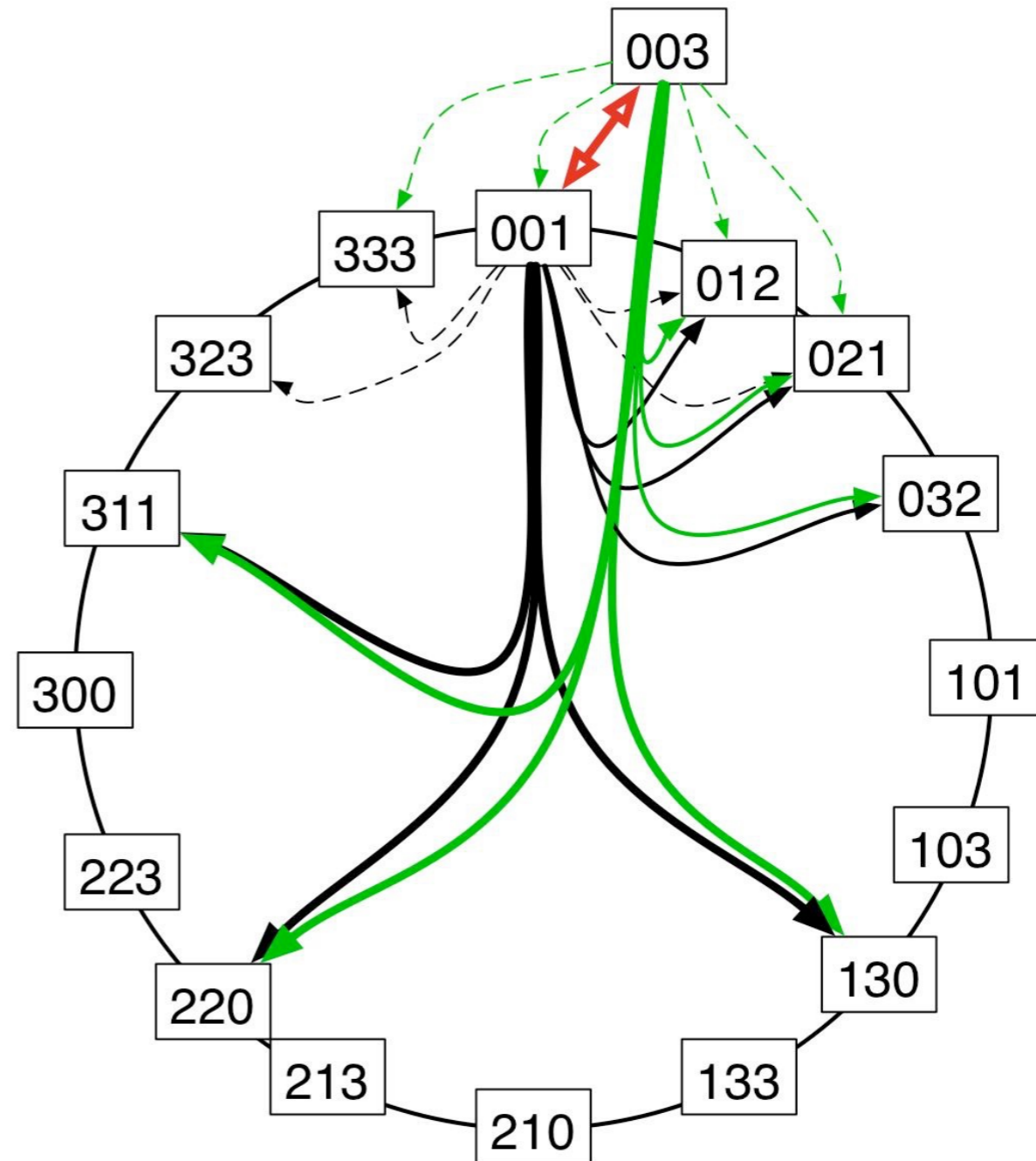
- For  $m = c(\log n)/b$  we get

$$e^{-n/2^{bm}} \leq e^{-n/2^{c \log n}} \leq e^{-n/n^c} \leq e^{-n^{c-1}}$$

- With (extremely) high probability there is no peer with the same prefix of length  $(1+\epsilon)(\log n)/b$
- Hence we have  $(1+\epsilon)(\log n)/b$  rows with  $2^\epsilon - 1$  entries each

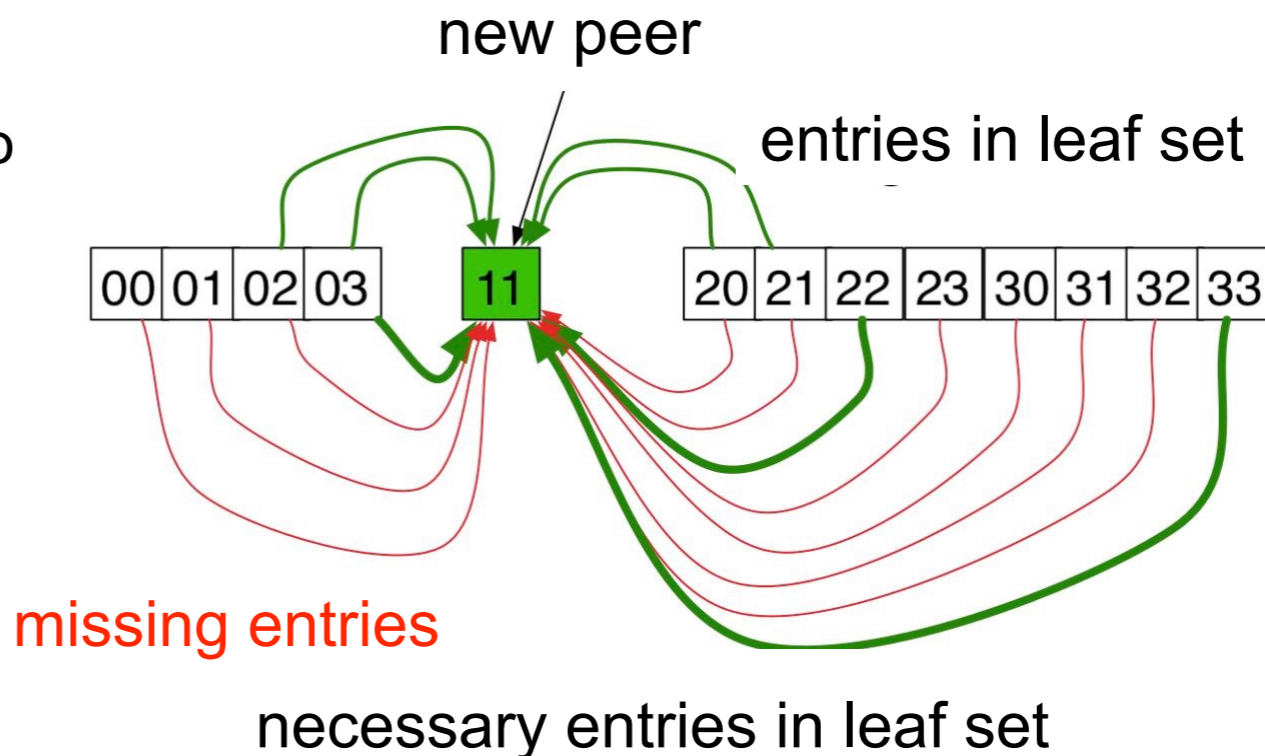
0	1	2	3	4	5		7	8	9	a	b	c	d	e	f
x	x	x	x	x	x		x	x	x	x	x	x	x	x	x
<hr/>															
6	6	6	6	6		6	6	6	6	6	6	6	6	6	6
0	1	2	3	4		6	7	8	9	a	b	c	d	e	f
x	x	x	x	x		x	x	x	x	x	x	x	x	x	x
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6	6	6	6	6	6	6	6	6	6		6	6	6	6	6
5	5	5	5	5	5	5	5	5	5		5	5	5	5	5
0	1	2	3	4	5	6	7	8	9		b	c	d	e	f
x	x	x	x	x	x	x	x	x	x		x	x	x	x	x
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6		6	6	6	6	6	6	6	6	6	6	6	6	6	6
5		5	5	5	5	5	5	5	5	5	5	5	5	5	5
a		a	a	a	a	a	a	a	a	a	a	a	a	a	a
0		2	3	4	5	6	7	8	9	a	b	c	d	e	f
x		x	x	x	x	x	x	x	x	x	x	x	x	x	x

- New node  $x$  sends message to the node  $z$  with the longest common prefix  $p$
- $x$  receives
  - routing table of  $z$
  - leaf set of  $z$
- $z$  updates leaf-set
- $x$  informs  $\ell$ -leaf set
- $x$  informs peers in routing table
  - with same prefix  $p$  (if  $\ell/2 < 2^b$ )
- Number of messages for adding a peer
  - $\ell$  messages to the leaf-set
  - expected  $(2^b - \ell/2)$  messages to nodes with common prefix
  - one message to  $z$  with answer



# When the Entry-Operation Errs

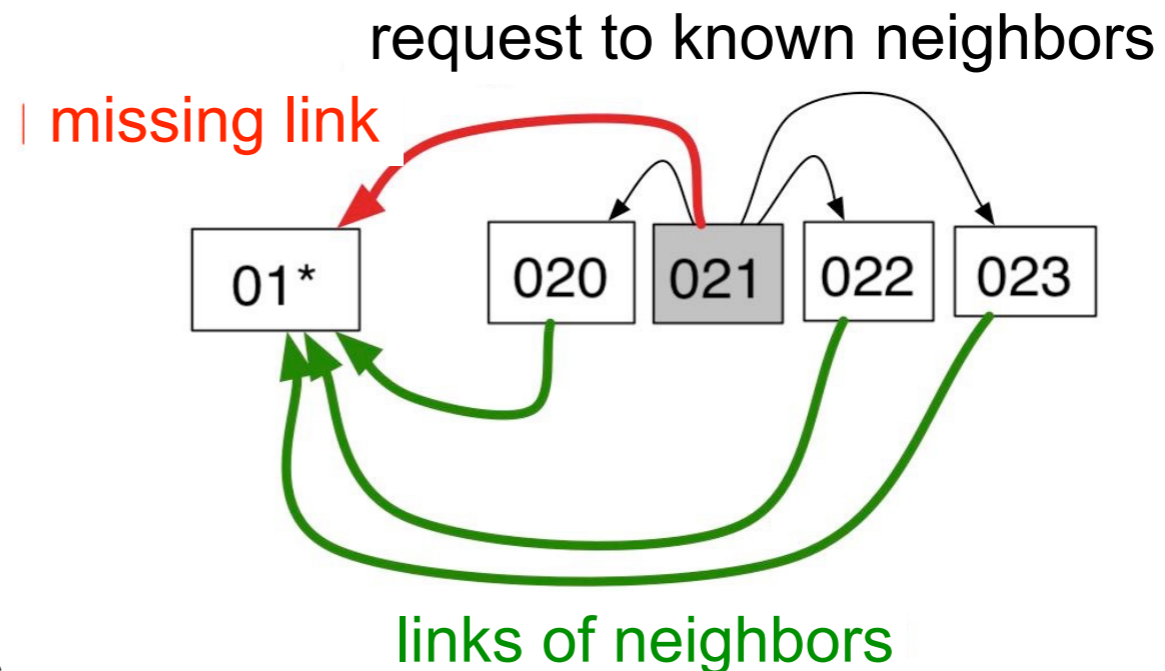
- Inheriting the next neighbor routing table does not allow work perfectly
- Example
  - If no peer with 1\* exists then all other peers have to point to the new node
  - Inserting 11
  - 03 knows from its routing table
    - 22,33
    - 00,01,02
  - 02 knows from the leaf-set
    - 01,02,20,21
- 11 cannot add all necessary links to the routing tables



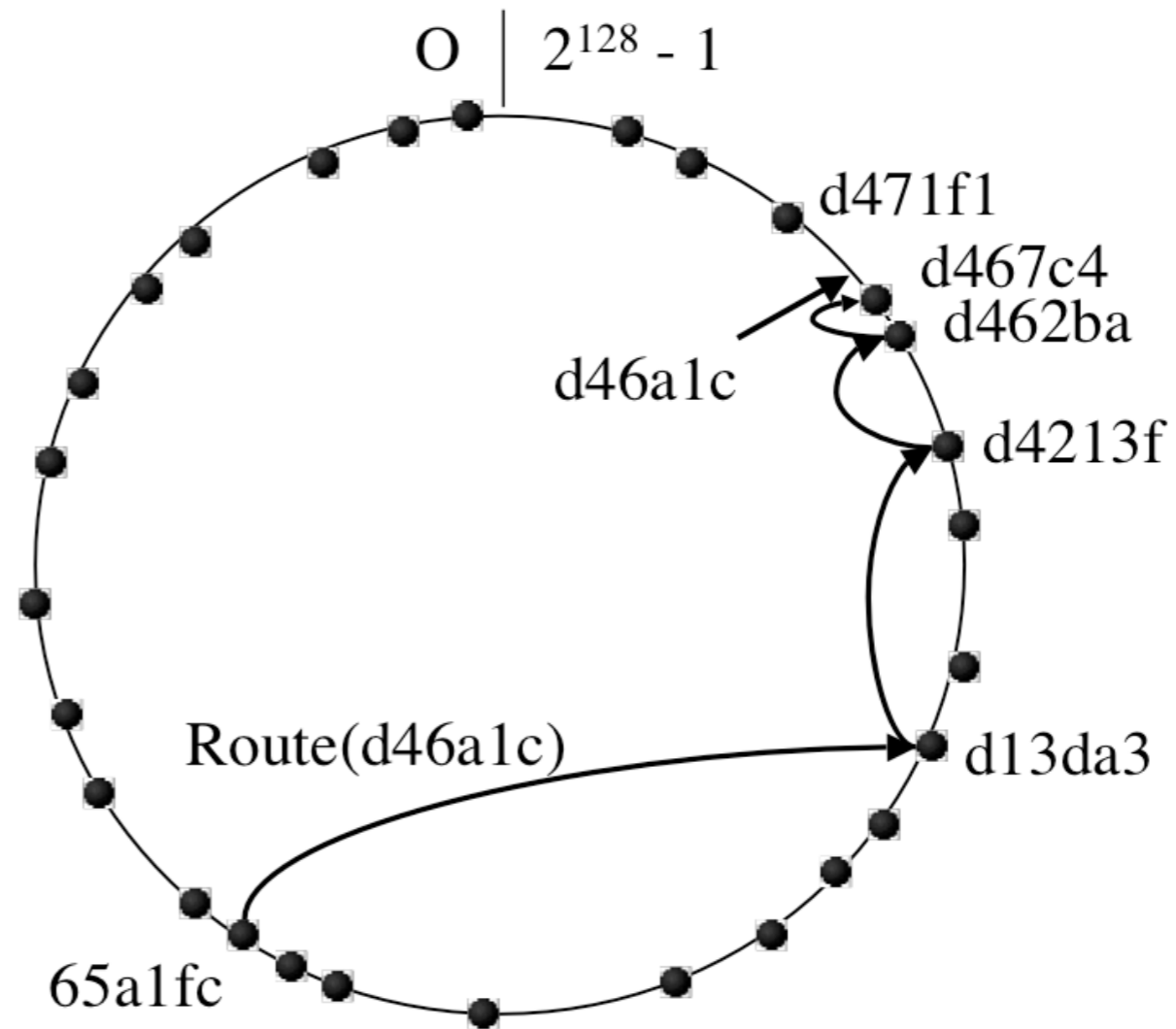


# Missing Entries in the Routing Table

- Assume the entry  $R_{ij}$  is missing at peer D
  - j-th row and i-th column of the routing table
- This is noticed if message of a peer with such a prefix is received
- This may also happen if a peer leaves the network
- Contact peers in the same row
  - if they know a peer this address is copied
- If this fails then perform routing to the missing link



- Compute the target ID using the hash function
- If the address is within the  $\ell$ -leaf set
  - the message is sent directly
  - or it discovers that the target is missing
- Else use the address in the routing table to forward the message
- If this fails take best fit from all addresses



# Lookup in Detail

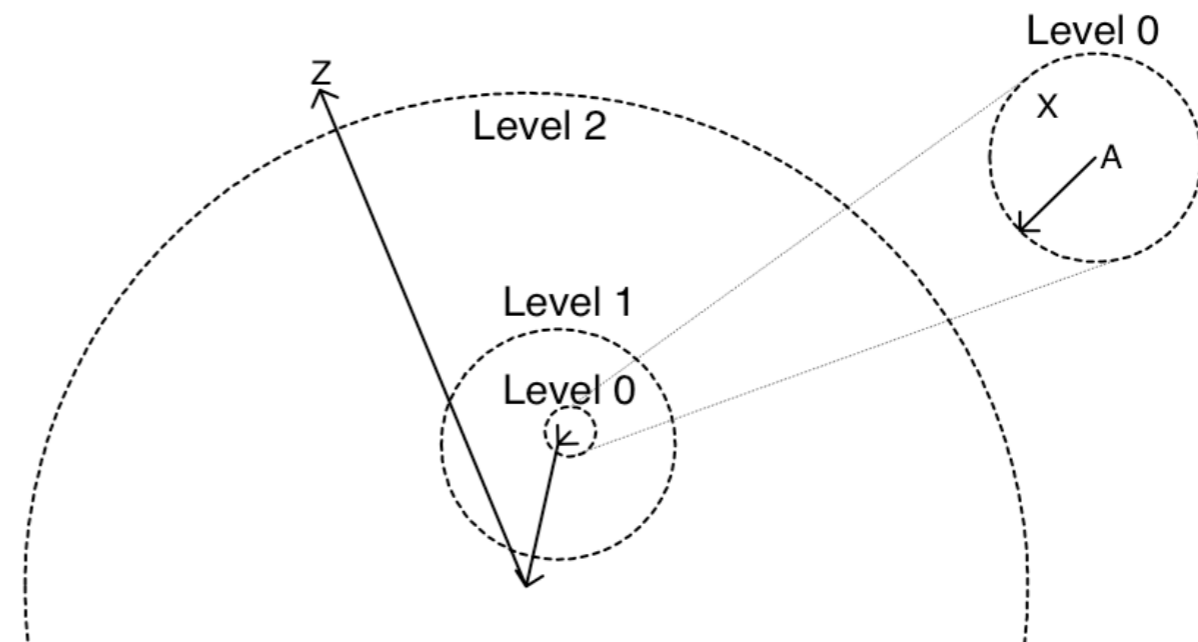
- L:  $\ell$ -leafset
  - R: routing table
  - M: nodes in the vicinity of D (according to RTT)
  - D: key
  - A: nodeID of current peer
  - $R_i^j$ : j-th row and i-th column of the routing table
  - $L_i$ : numbering of the leaf set
  - $D_i$ : i-th digit of key D
  - $shl(A)$ : length of the largest common prefix of A and D (shared header length)
- (1) if ( $L_{-\lfloor |L|/2 \rfloor} \leq D \leq L_{\lfloor |L|/2 \rfloor}$ ) {
  - (2)     // D is within range of our leaf set
  - (3)     forward to  $L_i$ , s.th.  $|D - L_i|$  is minimal;
  - (4) } else {
  - (5)     // use the routing table
  - (6)     Let  $l = shl(D, A)$ ;
  - (7)     if ( $R_l^{D_l} \neq null$ ) {
  - (8)         forward to  $R_l^{D_l}$ ;
  - (9)     }
  - (10)  else {
  - (11)     // rare case
  - (12)     forward to  $T \in L \cup R \cup M$ , s.th.
  - (13)          $shl(T, D) \geq l$ ,
  - (14)          $|T - D| < |A - D|$
  - (15)  }
  - (16) }

- If the Routing-Table is correct
  - routing needs  $O((\log n)/b)$  messages
- As long as the leaf-set is correct
  - routing needs  $O(n/l)$  messages
  - unrealistic worst case since even damaged routing tables allow dramatic speedup
- Routing does not use the real distances
  - M is used only if errors in the routing table occur
  - using locality improvements are possible
- Thus, Pastry uses heuristics for improving the lookup time
  - these are applied to the last, most expensive, hops

- Leaf-set peers are not near, e.g.
  - New Zealand, California, India, ...
- TCP protocol measures latency
  - latencies (RTT) can define a metric
  - this forms the foundation for finding the nearest peers
- All methods of Pastry are based on heuristics
  - i.e. no rigorous (mathematical) proof of efficiency
- Assumption: metric is Euclidean

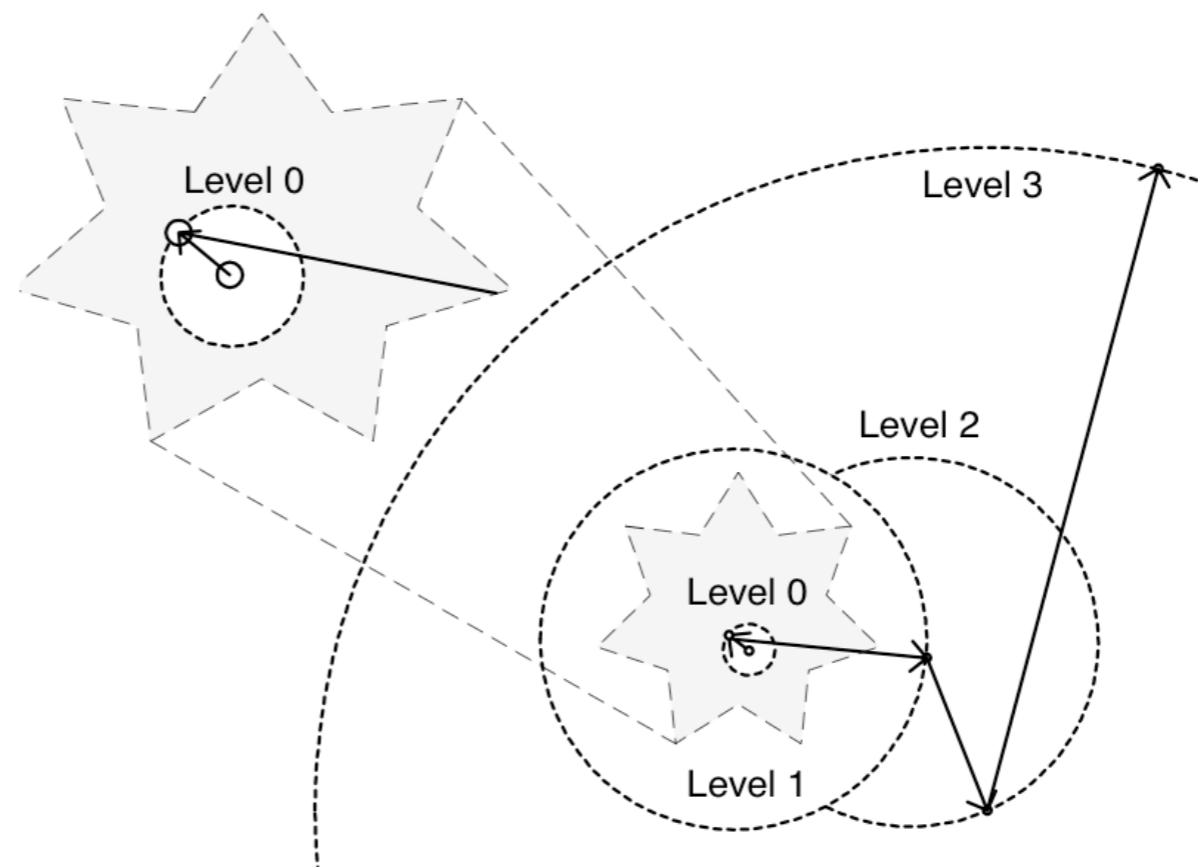
# Locality in the Routing Table

- Assumption
  - When a peer is inserted the peers contacts a near peer
  - All peers have optimized routing tables
- But:
  - The first contact is not necessary near according to the node-ID
- 1st step
  - Copy entries of the first row of the routing table of P
    - good approximation because of the triangle inequality (metric)
- 2nd step
  - Contact fitting peer  $p'$  of  $p$  with the same first letter
  - Again the entries are relatively close
- Repeat these steps until all entries are updated



# Locality in the Routing Table

- In the best case
  - each entry in the routing table is optimal w.r.t. distance metric
  - this does not lead to the shortest path
- There is hope for short lookup times
  - with the length of the common prefix the latency metric grows exponentially
  - the last hops are the most expensive ones
  - here the leaf-set entries help



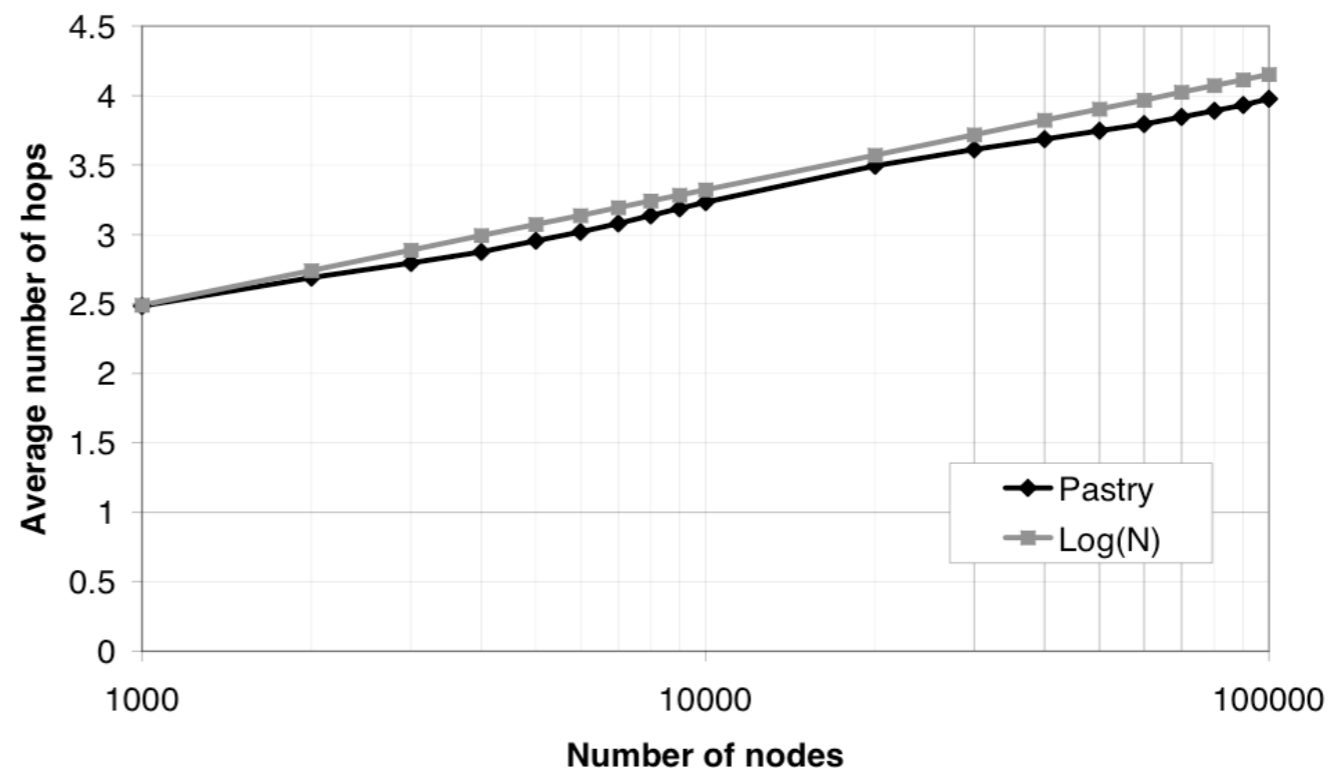
# Localization of Near Nodes

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- Node-ID metric and latency metric are not compatible
- If data is replicated on  $k$  peers then peers with similar Node-ID might be missed
- Here, a heuristic is used
- Experiments validate this approach



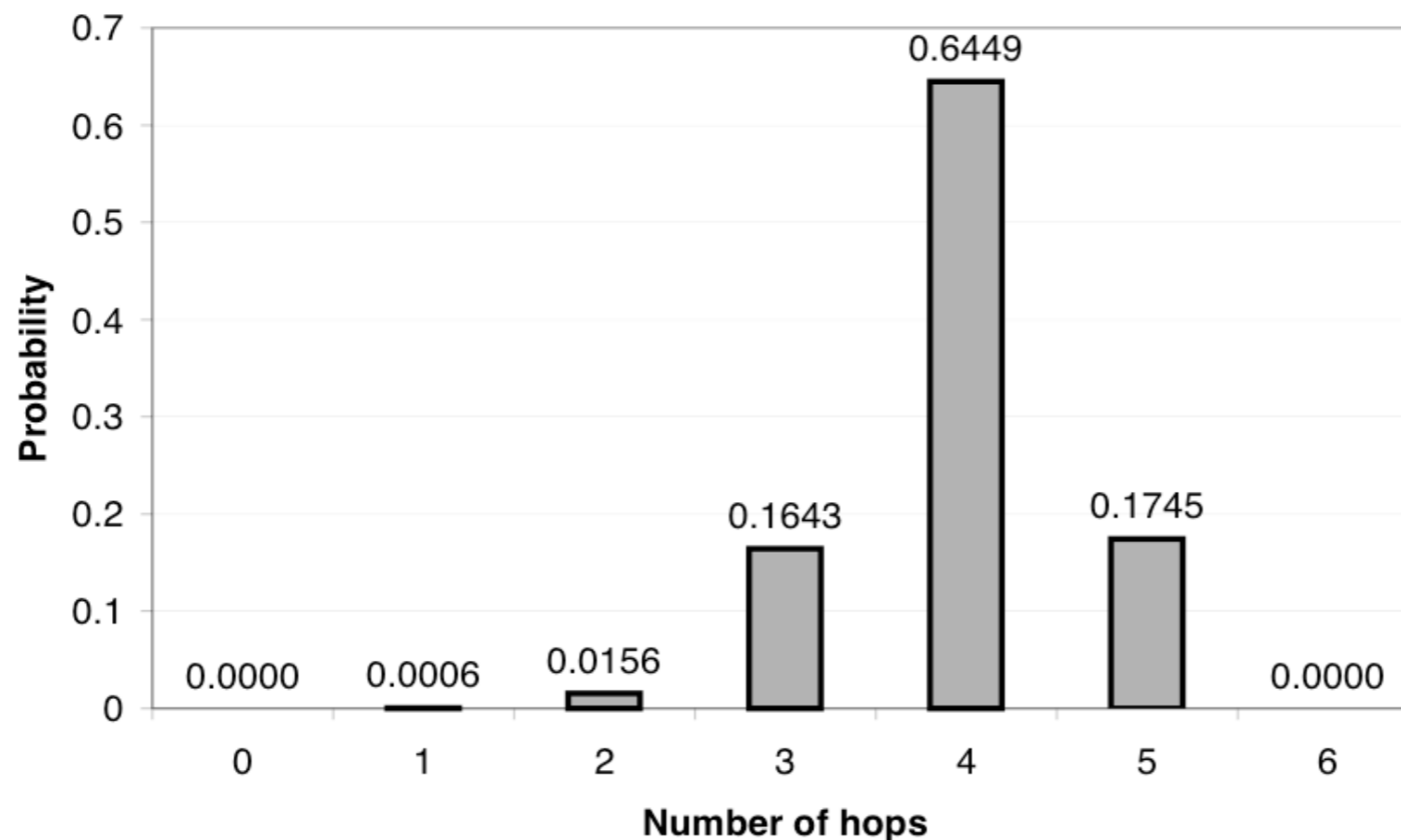
- Parameter  $b=4$ ,  
 $l=16$ ,  $M=32$
- In this experiment  
the hop distance  
grows  
logarithmically with  
the number of  
nodes
- The analysis  
predicts  $O(\log n)$
- Fits well



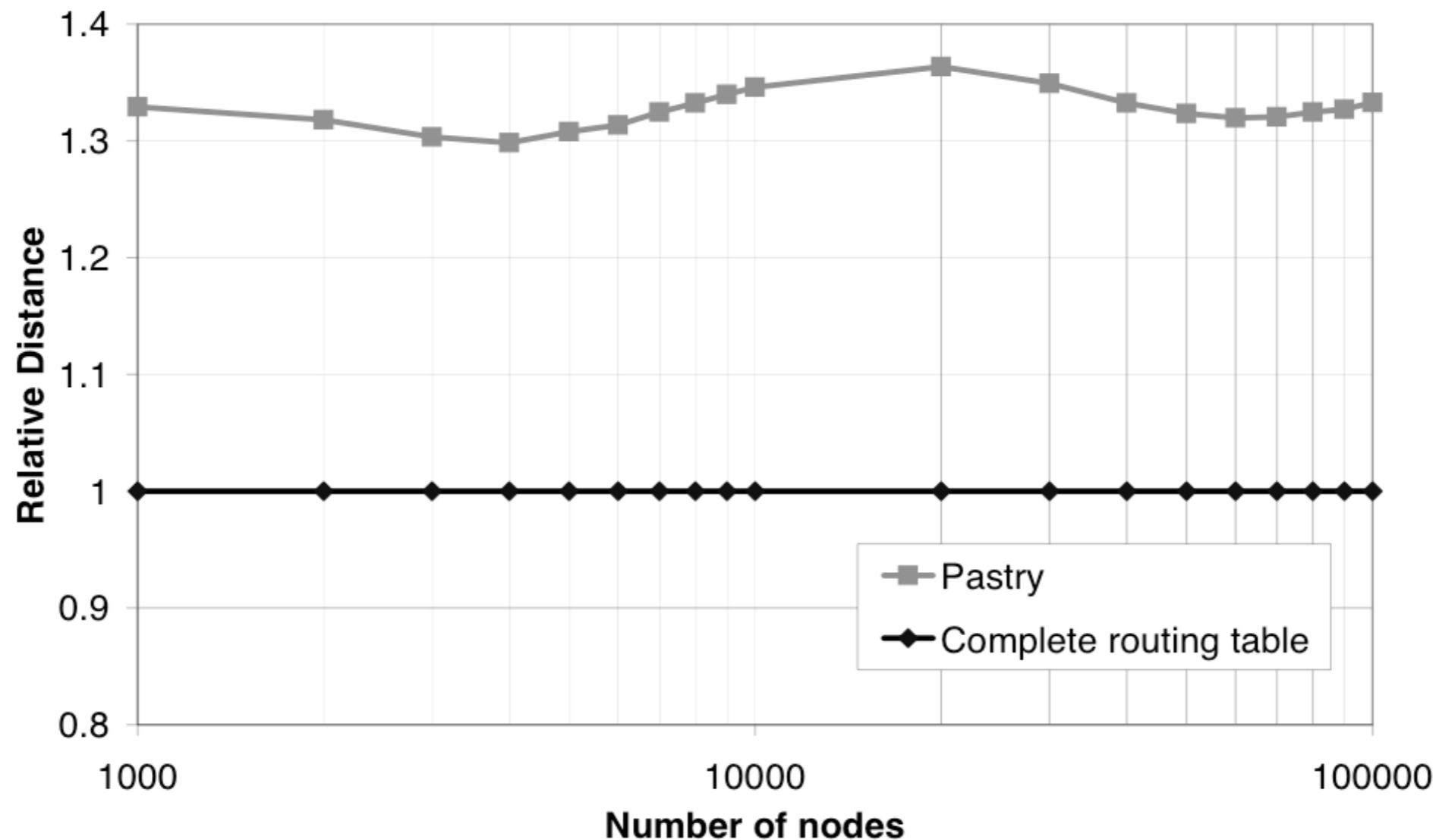
# Experimental Results

## Distribution of Hops

- Parameter  $b=4$ ,  $l=16$ ,  $M=32$ ,  $n = 100,000$
- Result
  - deviation from the expected hop distance is extremely small
- Analysis predicts difference with extremely small probability
  - fits well



- Parameter  $b=4$ ,  $l=16$ ,  $M=3$
- Compared to the shortest path astonishingly small
  - seems to be constant



# Interpreting the Experiments

- Experiments were performed in a well-behaving simulation environment
- With  $b=4$ ,  $L=16$  the number of links is quite large
  - The factor  $2^b/b = 4$  influences the experiment
  - Example  $n= 100\ 000$ 
    - $2^b/b \log n = 4 \log n > 60$  links in routing table
    - In addition we have 16 links in the leaf-set and 32 in M
- Compared to other protocols like Chord the degree is rather large
- Assumption of Euclidean metric is rather arbitrary



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