



# Peer-to-Peer Networks

## 14 Security

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# Cuckoo Hashing for Security

- Awerbuch, Scheideler, Towards Scalable and Robust Overlay Networks
- Problem:
  - Rejoin attacks
- Solution:
  - Chord network combined with
  - Cuckoo Hashing
  - Majority condition:
    - honest peers in the neighborhood are in the majority
  - Data is stored with  $O(\log n)$  copies

# Cuckoo Hashing

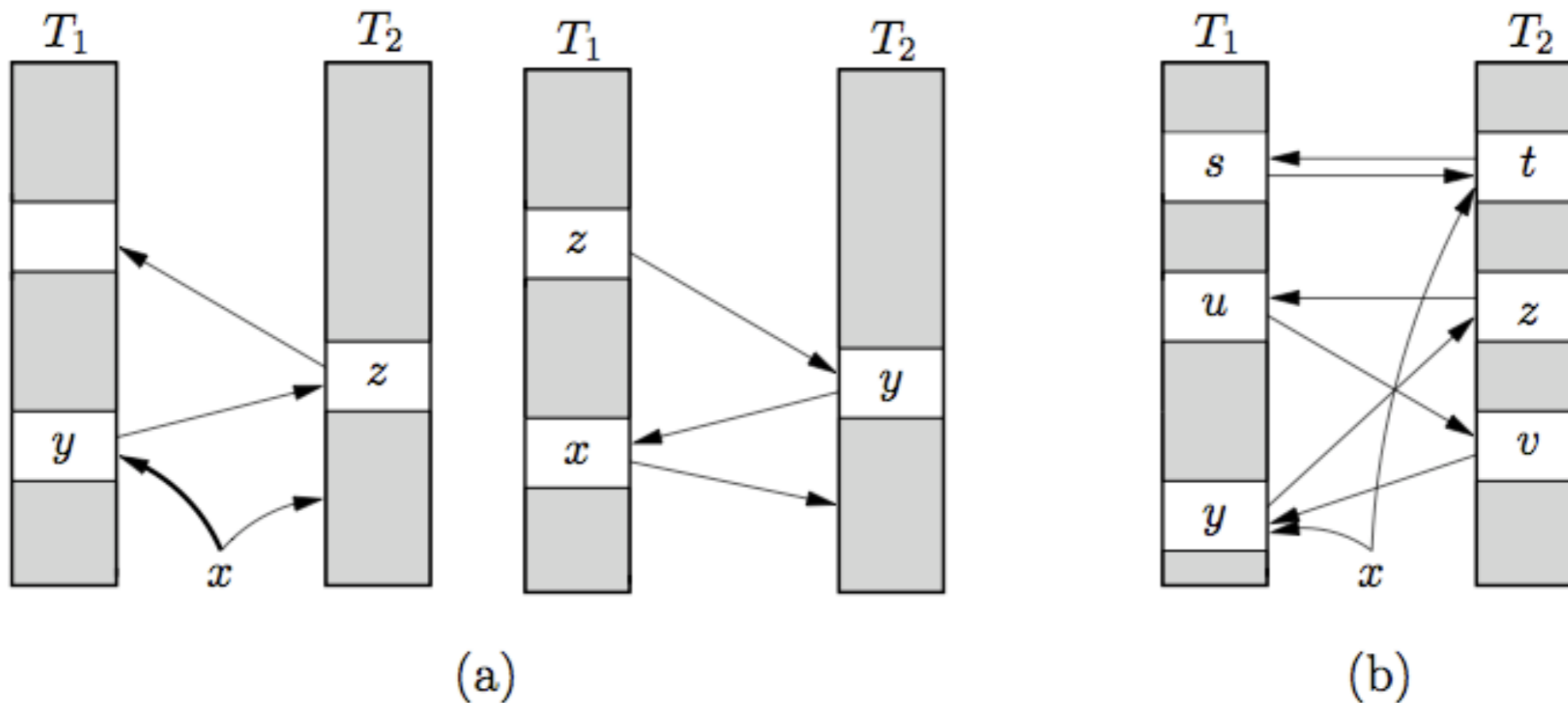


Fig. 1. Examples of CUCKOO HASHING insertion. Arrows show possibilities for moving keys. (a) Key  $x$  is successfully inserted by moving keys  $y$  and  $z$  from one table to the other. (b) Key  $x$  cannot be accommodated and a rehash is necessary.

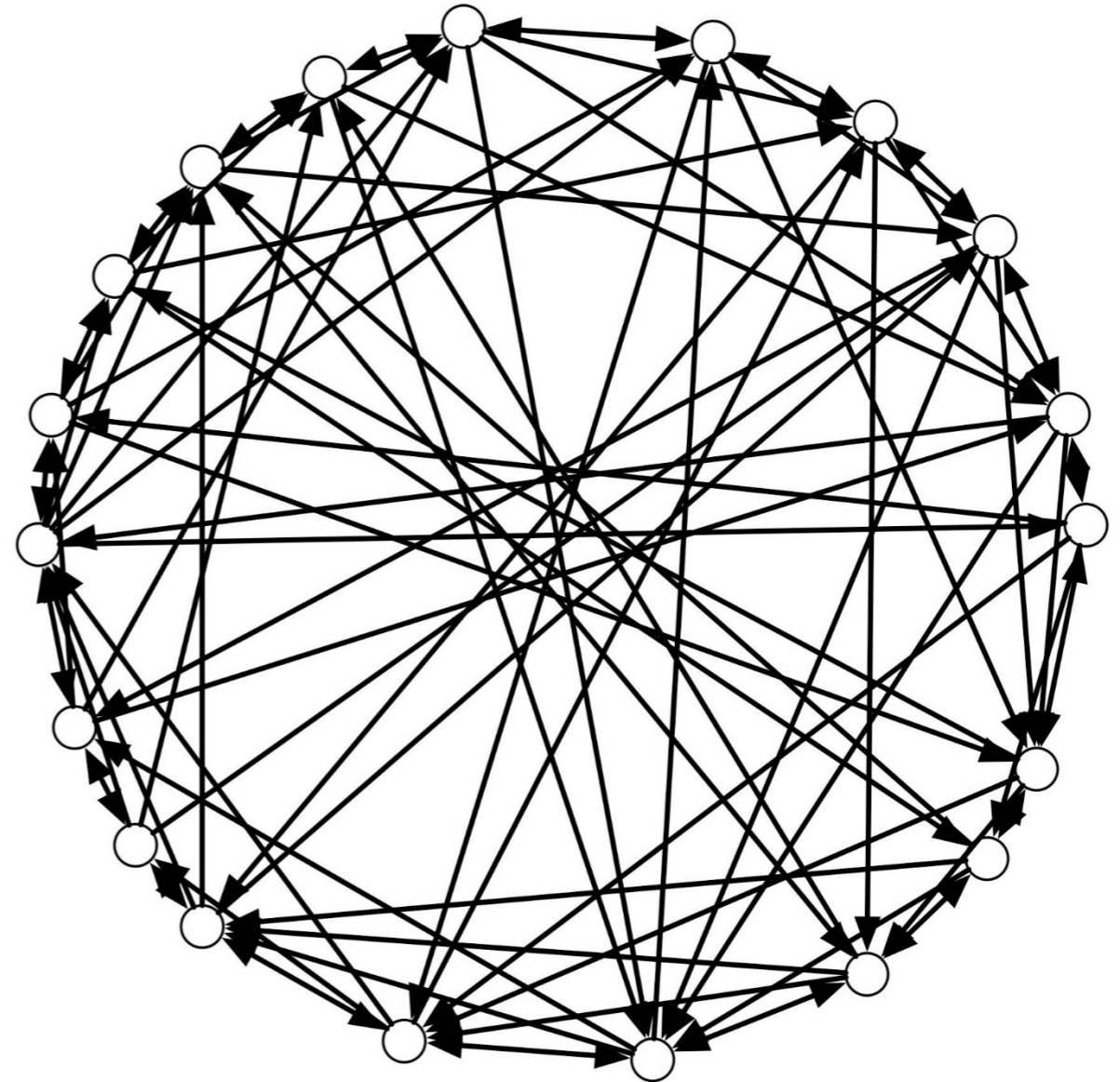
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From Cuckoo Hashing  
Rasmus Pagh, Flemming Friche Rodler  
2004

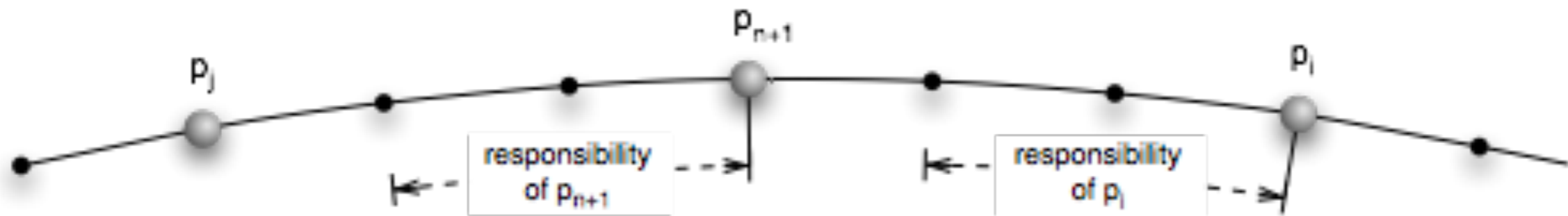
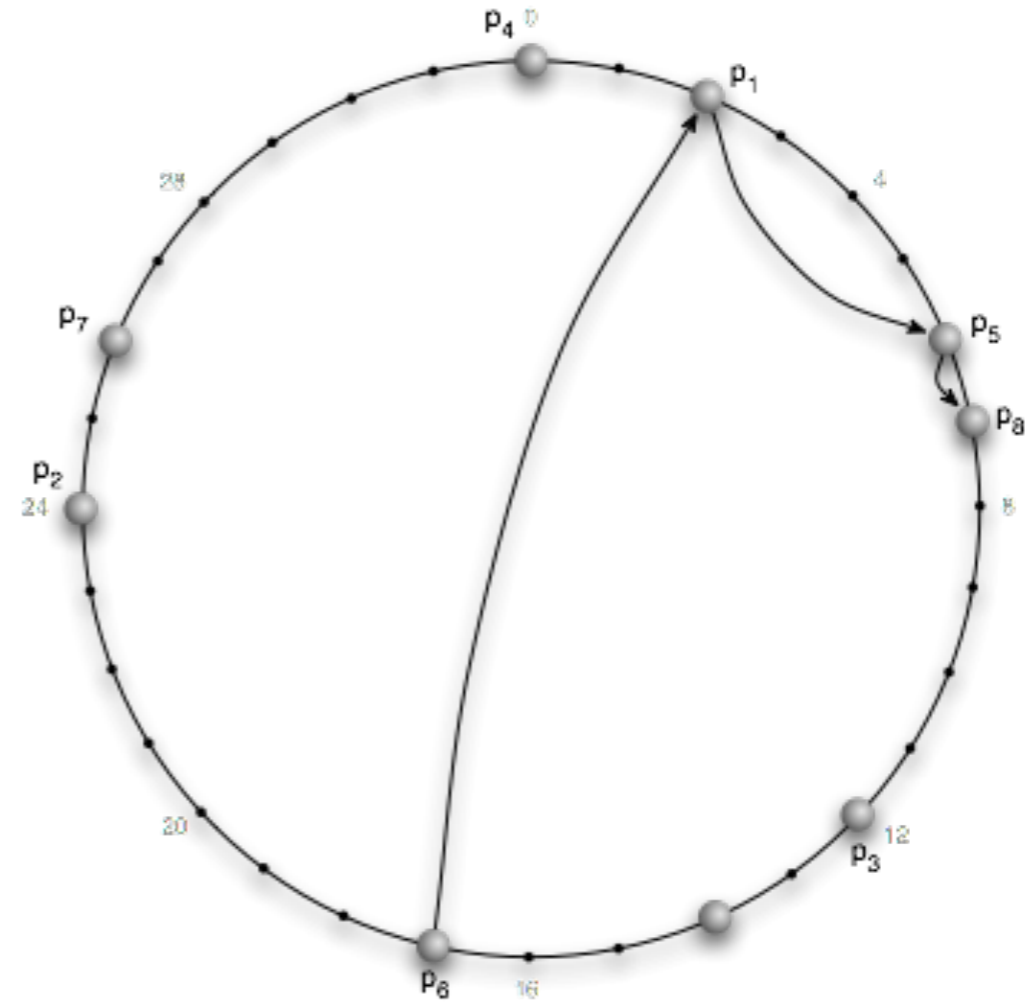
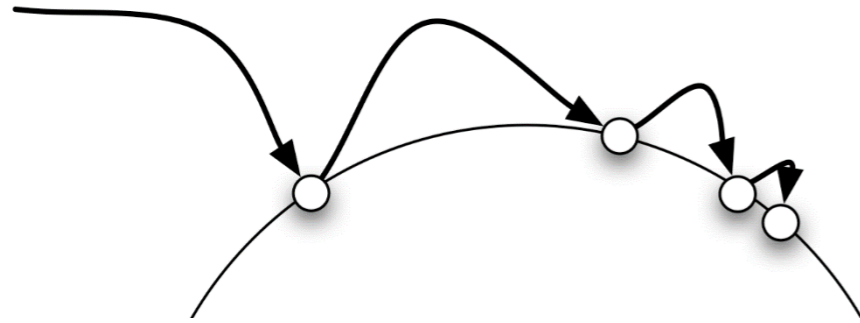
# Efficiency of Cuckoo Hashing

- Theorem
  - Let  $\epsilon > 0$  then if at most  $n$  elements are stored, then Cuckoo Hashing needs a hash space of  $2n + \epsilon$ .
- Three hash functions increase the load factor from 1/2 to 91%
- Insert
  - needs  $O(1)$  steps in the expectation
  - $O(\log n)$  with high probability
- Lookup
  - needs two steps

- Ion Stoica, Robert Morris, David Karger, M. Frans Kaashoek and Hari Balakrishnan (2001)
- Distributed Hash Table
  - range  $\{0, \dots, 2^m - 1\}$
  - for sufficient large  $m$
- for this work the range is seen as  $[0, 1)$
- Network
  - ring-wise connections
  - shortcuts with exponential increasing distance

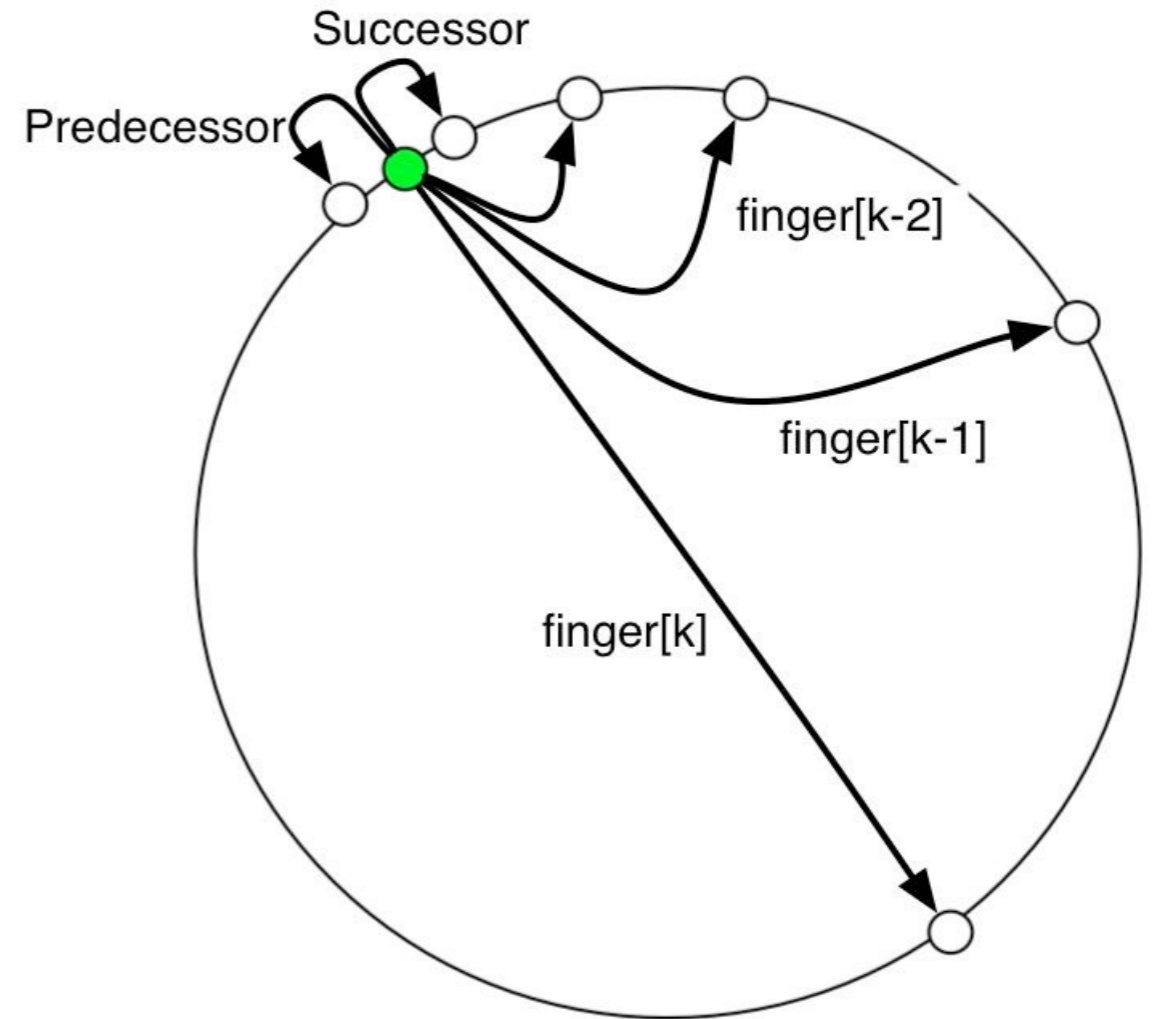


# Lookup in Chord



# Data Structure of Chord

- For each peer
  - successor link on the ring
  - predecessor link on the ring
  - for all  $i \in \{0, \dots, m-1\}$ 
    - $\text{Finger}[i] :=$  the peer following the value  $r_v(b+2^i)s$
- For small  $i$  the finger entries are the same
  - store only different entries
- Chord
  - needs  $O(\log n)$  hops for lookup
  - needs  $O(\log^2 n)$  messages for inserting and erasing of peers

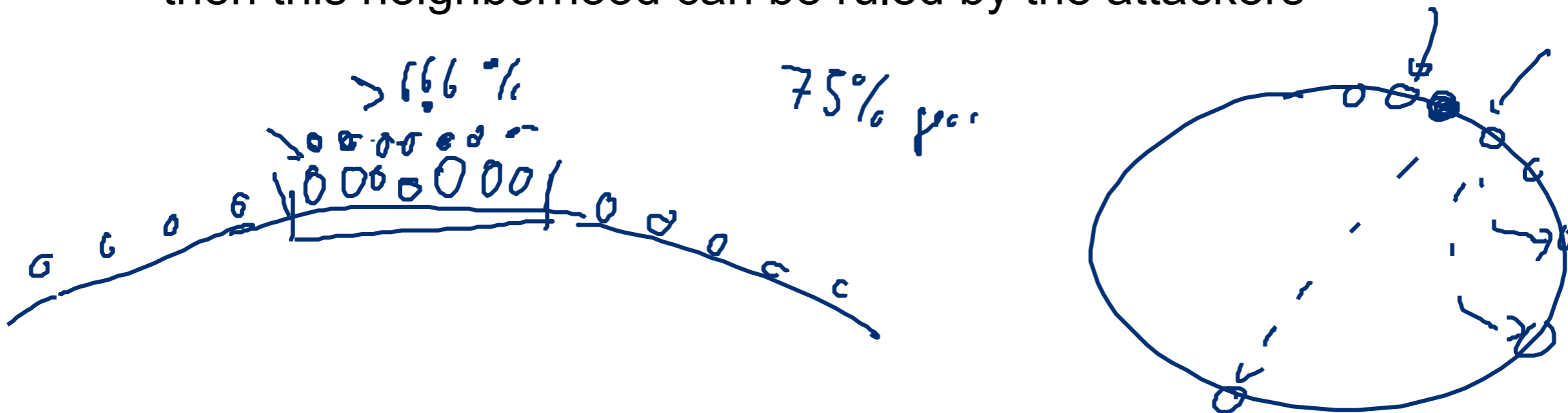


# Cuckoo Hashing for Security

- Given  $n$  honest peers and  $\epsilon n$  dishonest peers
- Goal
  - For any adversarial attack the following properties for every interval  $I \subseteq [0, 1)$  of size at least  $(c \log n)/n$  we have
    - Balancing condition
      - $I$  contains  $\Theta(|I| \cdot n)$  nodes
    - Majority condition
      - the honest nodes in  $I$  are in the majority
- Then all majority decisions of  $O(\log n)$  nodes give a correct result

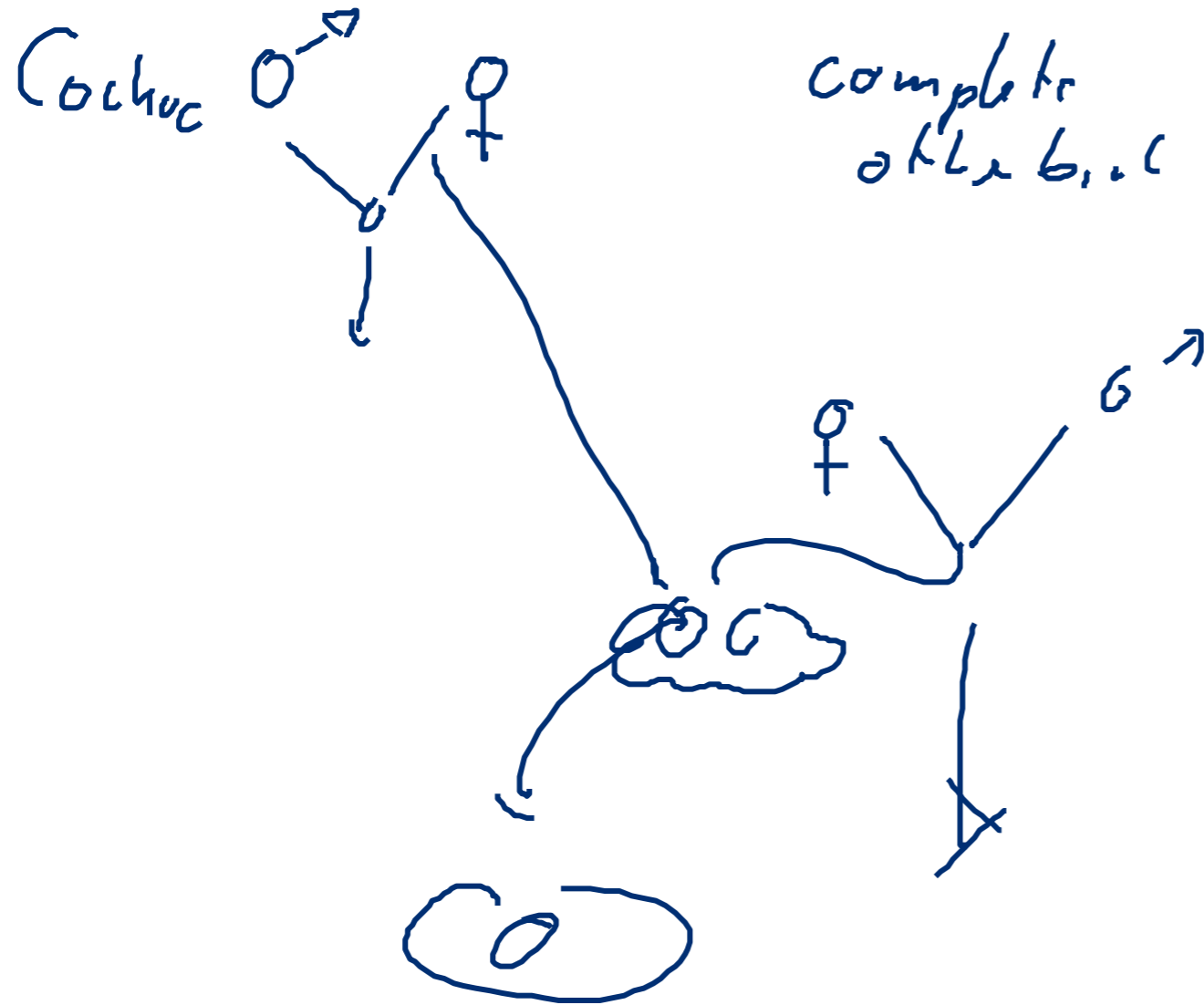


- Secure hash functions for positions in the Chord
  - if one position is used
  - then in an  $O(\log n)$  neighborhood more than half is honest
  - if more than half of all peers are honest
- Rejoin attacks
  - use a small number of attackers
  - check out new addresses until attackers fall in one interval
  - then this neighborhood can be ruled by the attackers

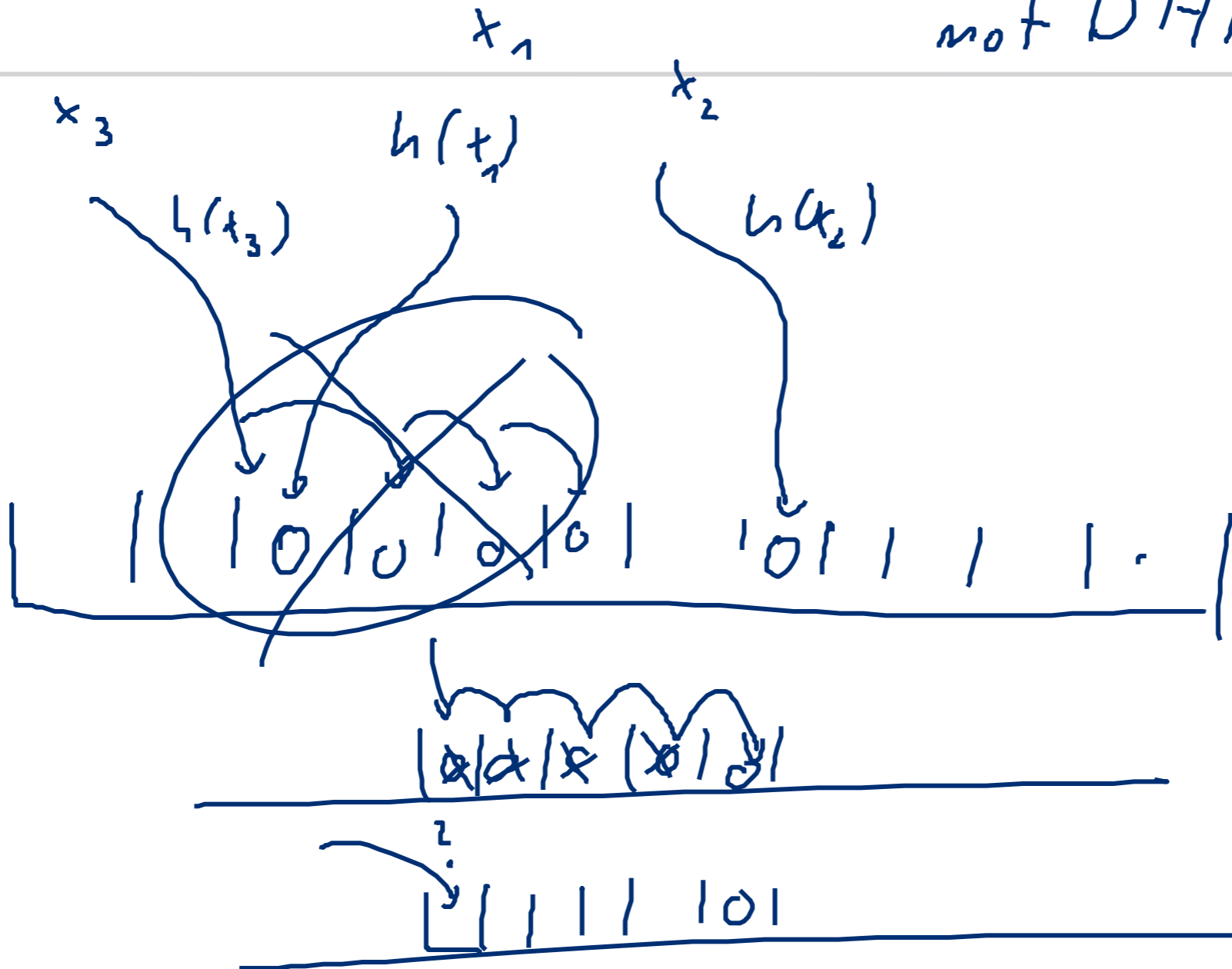


Cuckoo

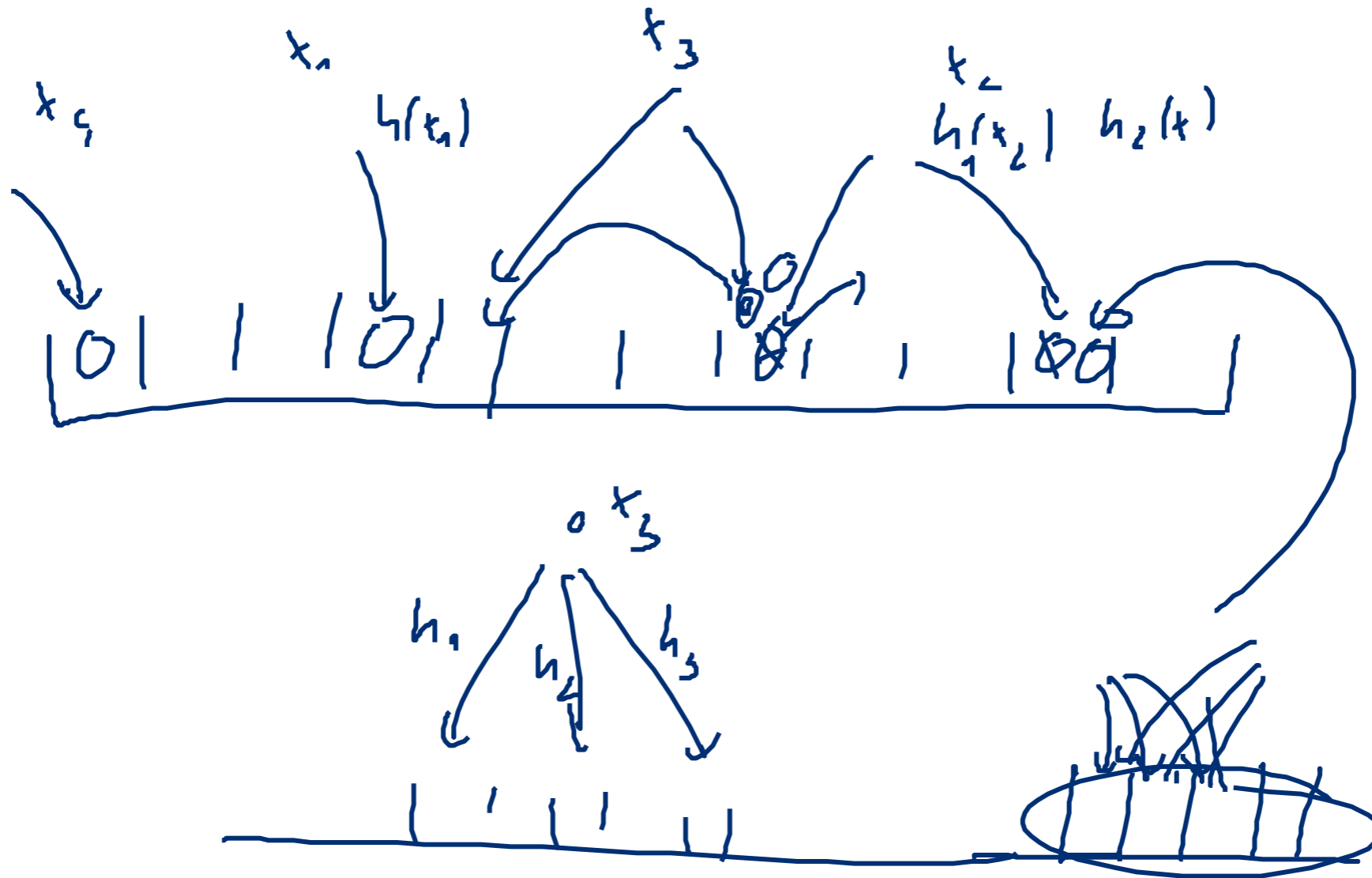
Kuckuck



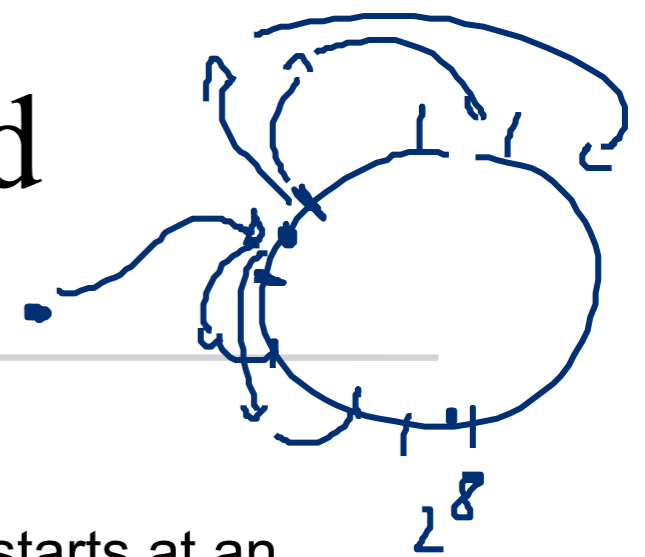
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# Cuckoo Hashing



# The Cuckoo Rule for Chord



## ■ Notation

- a region is an interval of size  $1/2^r$  in  $[0, 1)$  for some integer  $r$  that starts at an integer multiple of  $1/2^r$
- There are exactly  $2^r$  regions
- A  $k$ -region is a region of size (closest from above to)  $k/n$ , and for any point  $x \in [0, 1)$
- the  $k$ -region  $R_k(x)$  is the unique  $k$ -region containing  $x$ .

## ■ Cuckoo rule

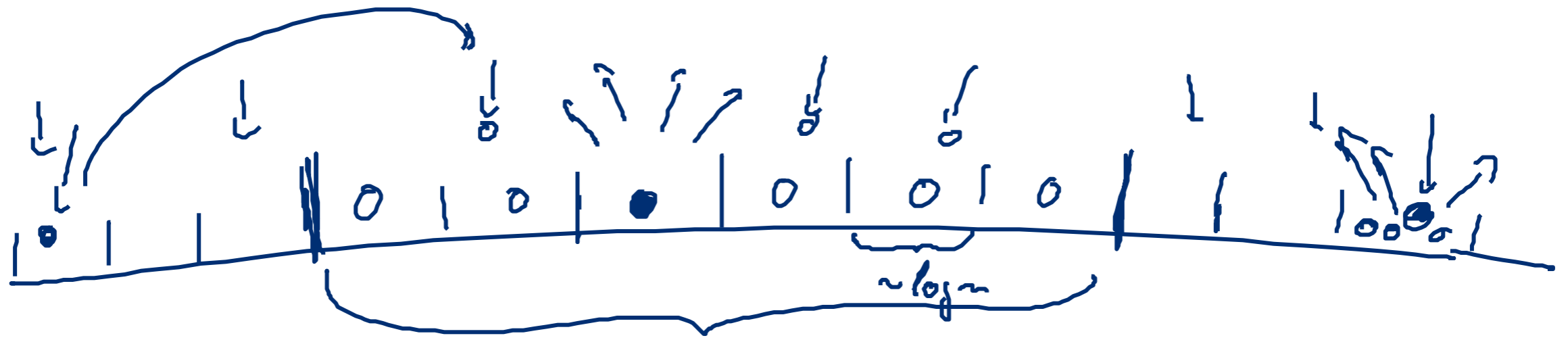
- If a new node  $v$  wants to join the system, pick a random  $x \in [0, 1)$ .
- Place  $v$  into  $x$  and move all nodes in  $R_k(x)$  to points in  $[0, 1)$  chosen uniformly at random
  - (without replacing any further nodes).

## ■ Theorem

- For any constants  $\epsilon$  and  $k$  with  $\epsilon < 1 - 1/k$ , the cuckoo rule with parameter  $k$  satisfies the balancing and majority conditions for a polynomial number of rounds, with high probability, for any adversarial strategy within our model.
- The inequality  $\epsilon < 1 - 1/k$  is sharp

- Data storage
  - each data item is stored in the  $O(\log^3 n)$  neighborhood as copies
- Primitives
  - robust hash functions
    - safe against attacks
  - majority decisions of each operation
  - use multiple routes for targeting location

$$\left[ \begin{array}{c} \frac{1}{16} \quad \frac{15}{16} \quad \frac{1}{16} \\ \sum_{i=1}^m \left( \frac{15}{16} \right)^{i-1} \cdot 16^i \cdot i \rightarrow 16 \end{array} \right]$$



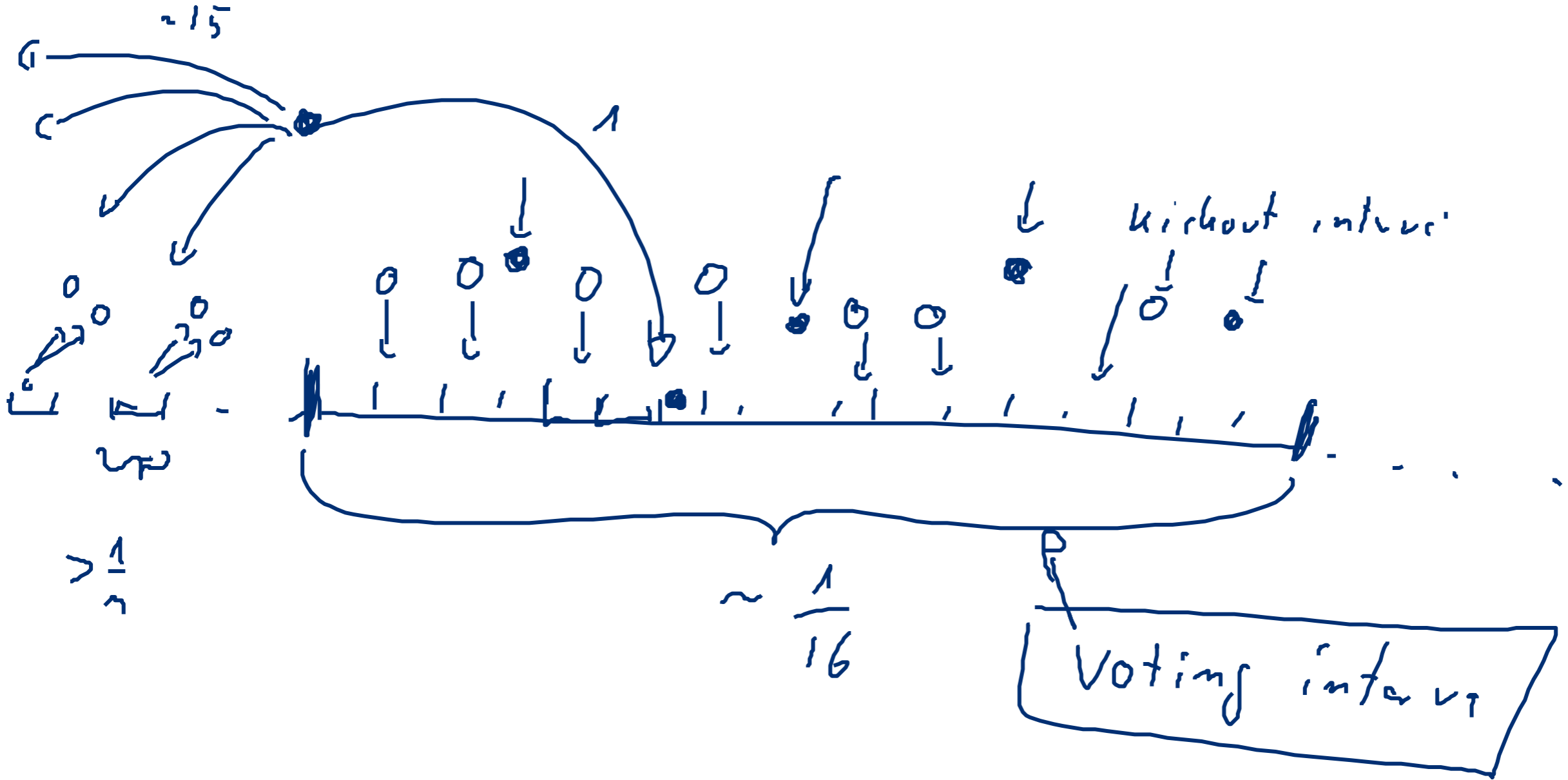
$$m \sim \log_2^2 m$$

$$\frac{2^4}{m} \approx \frac{1}{16}$$

→ Cherno Sf

# accesses,  $\frac{m}{2^4}$  misses.







- Lookup
  - works correctly with high probability
  - can be performed with  $O(\log^5 n)$  messages
- Inserting of data
  - works in „polylogarithmic time“
  - needs  $O(\log^5 n)$  messages
- Copies stored of each data:  $O(\log^3 n)$

$$\log_2^5 1000$$

$$\approx 10^5 = 100,000$$

- Advantage
  - Cuckoo Chord is safe against adversarial attacks
  - Cuckoo rule is simple and effective
- Disadvantage
  - Computation of secure hash function is complex
  - Considerate overhead for communication
- Theoretical breakthrough
- Little impact to the practical world



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