

Wireless Sensor Networks

22nd Lecture

24.01.2007

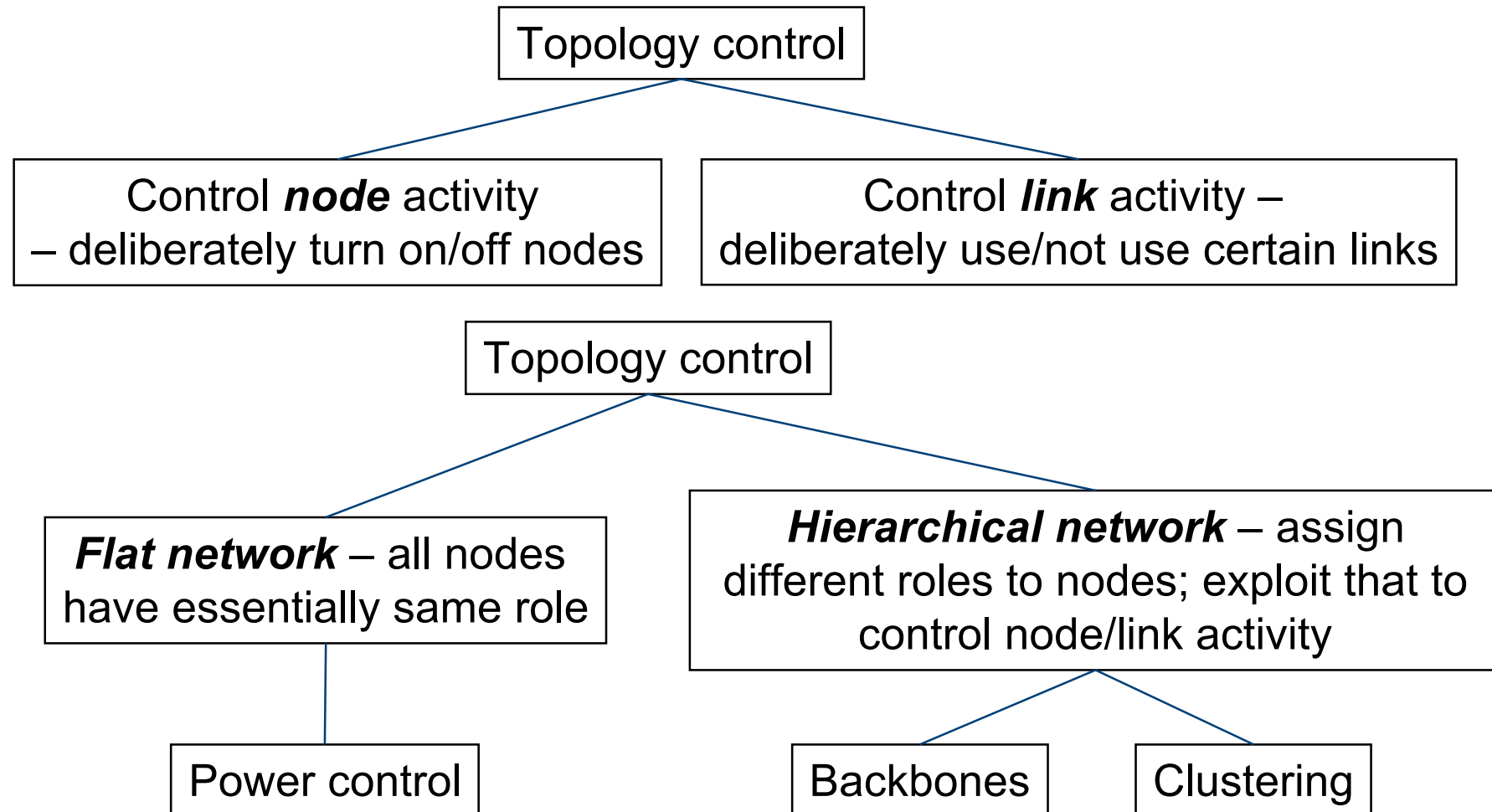


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Options for topology control





Power control – magic numbers?

- **Question: What is a good power level for a node to ensure “nice” properties of the resulting graph?**
- **Idea: Controlling transmission power corresponds to controlling the number of neighbors for a given node**
- **Is there an “optimal” number of neighbors a node should have?**
 - Is there a “magic number” that is good irrespective of the actual graph/network under consideration?
- **Historically, $k=6$ or $k=8$ had been suggested as such “magic numbers”**
 - However, they optimize progress per hop – they do *not* guarantee connectivity of the graph!!
 - Needs deeper analysis



Controlling transmission range

- Assume all nodes have identical transmission range $r=r(|V|)$, network covers area A , V nodes, uniformly distr.
- Fact: Probability of connectivity goes to zero if:

$$r(|V|) \leq \sqrt{\frac{(1-\epsilon)A \log |V|}{\pi|V|}}, \text{ for any } \epsilon > 0$$

- Fact: Probability of connectivity goes to 1 for

$$r(|V|) \geq \sqrt{\frac{A(\log |V| + \gamma|V|)}{\pi|V|}}$$

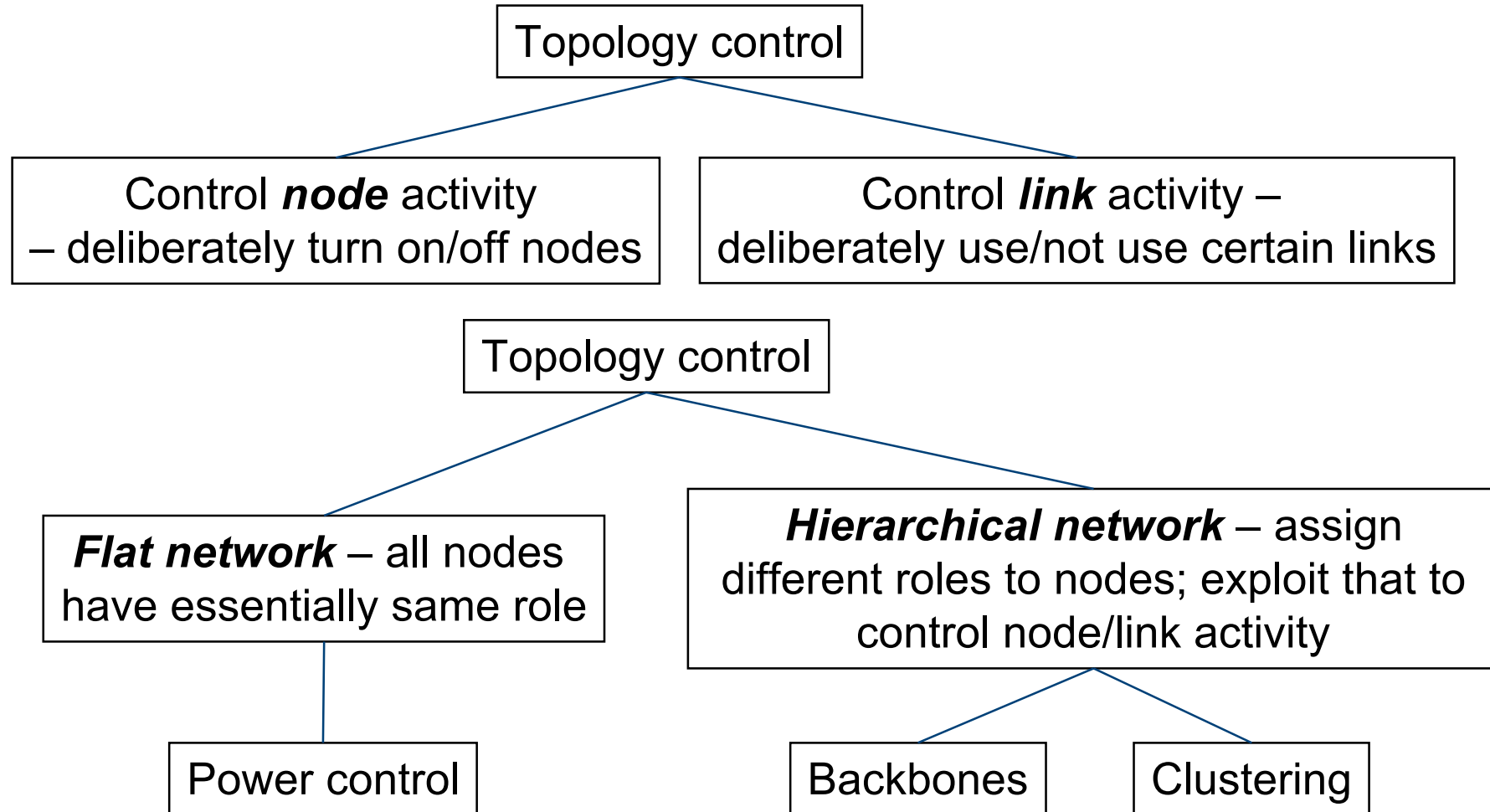
if and only if $\gamma|V| \rightarrow \infty$ with $|V|$

- Fact (uniform node distribution, density ρ):

$$P(G \text{ is } k\text{-connected}) \approx \left(1 - \sum_{l=0}^{k-1} \frac{(\rho\pi r^2)^l}{l!} e^{-\rho\pi r^2} \right)$$



Options for topology control





Hierarchical networks – backbones

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- **Idea: Select some nodes from the network/graph to form a *backbone***
 - A connected, minimal, dominating set (MDS or MCDS)
 - Dominating nodes control their neighbors
 - Protocols like routing are confronted with a simple topology – from a simple node, route to the backbone, routing in backbone is simple (few nodes)
- **Dominating Set:**
 - Given an undirected graph $G=(V,E)$
 - Find a minimal subset $W \subseteq V$ such that for all $u \in V$ there exists $v \in W$ with $\{u,v\} \in E$
- **Problem: MDS is an NP-hard problem**
 - Hard to approximate, and even approximations need quite a few messages
 - Polynomial approximable within $c \log n$ for some $c > 0$ only if $P=NP$
 - Polynomial approximable within a factor of $1 + \log n$.

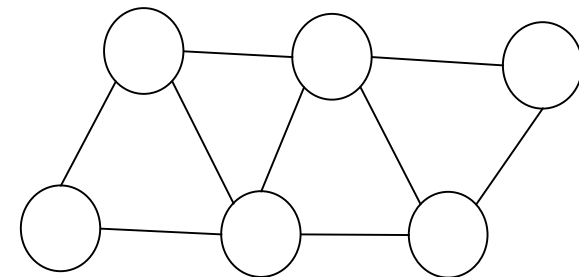


Backbone by growing a tree

➤ Construct the backbone as a tree, grown iteratively

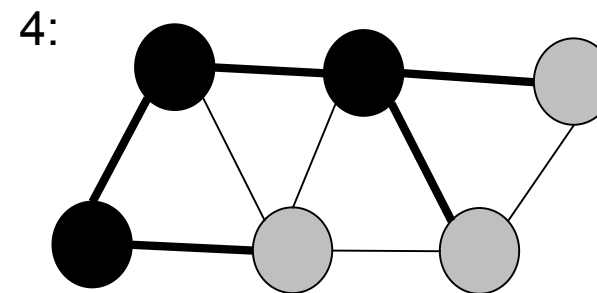
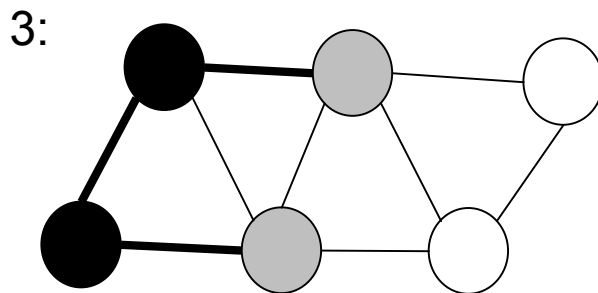
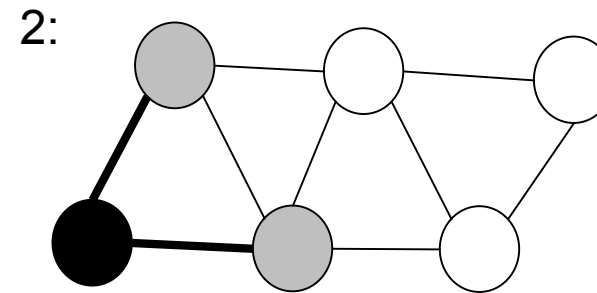
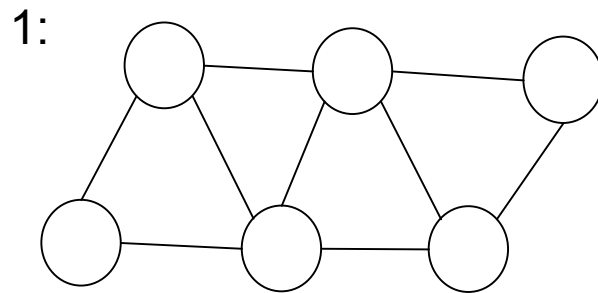
```
initialize all nodes' color to white
pick an arbitrary node and color it grey

while (there are white nodes) {
  pick a grey node v that has white neighbors
  color the grey node v black
  foreach white neighbor u of v {
    color u grey
    add (v,u) to tree T
  }
}
```





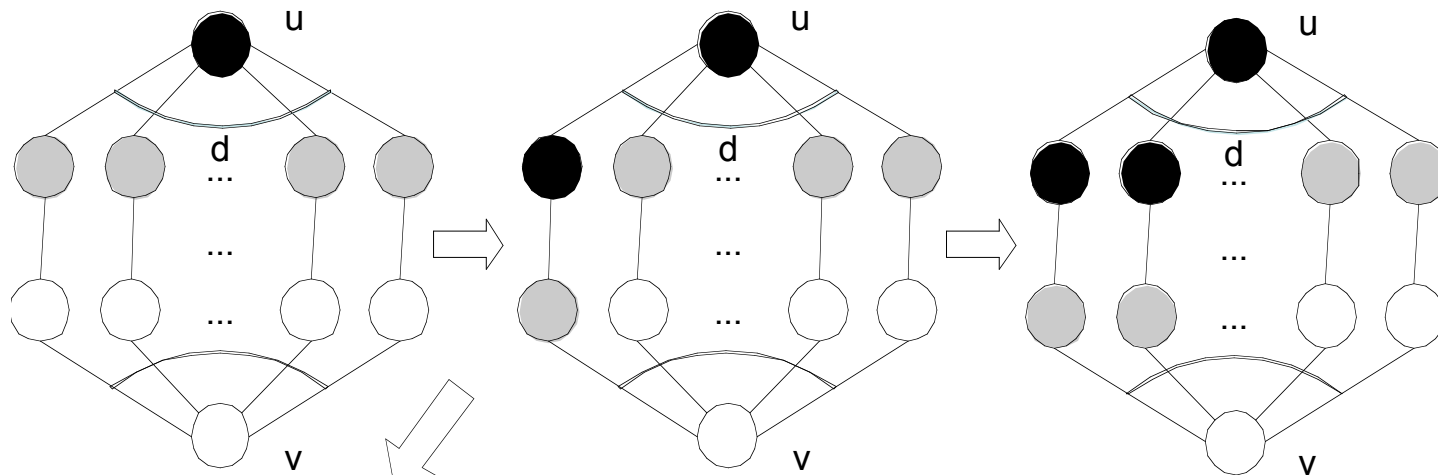
Backbone by growing a tree – Example





Problem: Which gray node to pick?

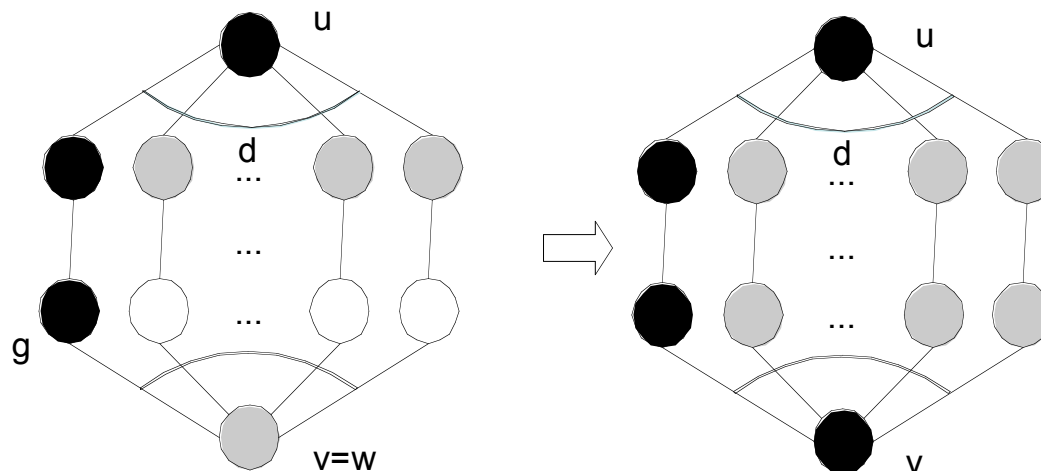
- When blindly picking any gray node to turn black
 - resulting tree can be very bad



Solution:
Look ahead!

Here,
one step suffices

Look-ahead
using
nodes g
and w





Performance of tree growing with look ahead

- **Dominating set obtained by growing a tree with the look ahead heuristic is at most a factor $2(1+ H(\Delta))$ larger than MDS**
 - $H(\cdot)$ harmonic function, $H(k) = \sum_{i=1}^k 1/i \leq \ln k + 1$
 - Δ is maximum degree of the graph

- **It is automatically connected**

- **Can be implemented in a distributed fashion as well**



Start big, make lean

- **Idea: start with some, possibly large, connected dominating set, reduce it by removing unnecessary nodes**
- **Initial construction for dominating set**
 - All nodes are initially white
 - Mark any node black that has two neighbors that are not neighbors of each other (they might need to be dominated)
 - Black nodes form a connected dominating set (proof by contradiction); shortest path between ANY two nodes only contains black nodes
- **Needed: Pruning heuristics**



Pruning heuristics

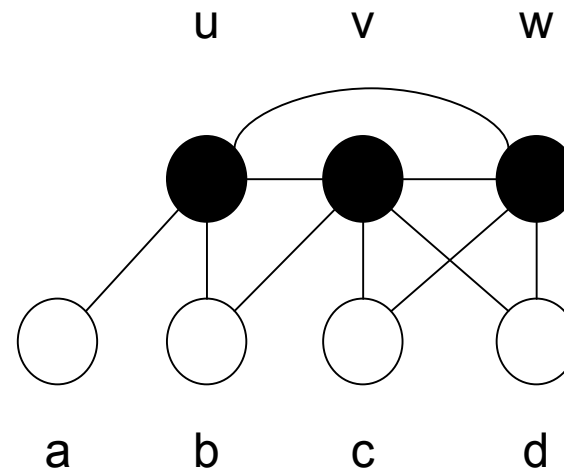
➤ **Heuristic 1: Unmark node v if**

- Node v and its neighborhood are included in the neighborhood of some node marked node u (then u will do the domination for v as well)
- Node v has a smaller unique identifier than u (to break ties)

➤ **Heuristic 2: Unmark node v if**

- Node v's neighborhood is included in the neighborhood of two marked neighbors u and w
- Node v has the smallest identifier of the tree nodes

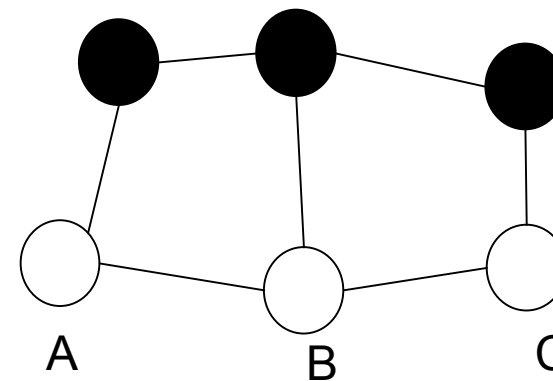
➤ **Nice and easy, but only linear approximation factor**





One more distributed backbone heuristic: Span

- **Construct backbone, but take into account need to carry traffic – preserve capacity**
 - Means: If two paths could operate without interference in the original graph, they should be present in the reduced graph as well
 - Idea: If the stretch factor (induced by the backbone) becomes too large, more nodes are needed in the backbone
- **Rule: Each node observes traffic around itself**
 - If node detects two neighbors that need three hops to communicate with each other, node joins the backbone, shortening the path
 - Contention among potential new backbone nodes handled using random backoff



Thank you

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