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Algorithms for Radio Networks

Multiplexing

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Multiple Use of the Medium

➤ Spatial Multiplexing

- Parallel and exclusive use of transmission channels
 - e.g. Extra lines / cells / directional antenna

➤ Frequency division multiplexing

- Multiple signals to be transmitted in a frequency range of bundled;
- In radio transmission, different frequencies are assigned to different stations.

➤ Time division multiplexing

- Delayed transmission of multiple signals

➤ Code division multiplexing

- Coding of the signal into orthogonal codes, which can now be broadcast simultaneously on one frequency
- Decoding with overlay also possible

➤ Multiple-Input Multiple-Output

- Sending and receiving antennas by several
- Using the spatial and temporal information about location of several waves
 - e.g. 802.11n

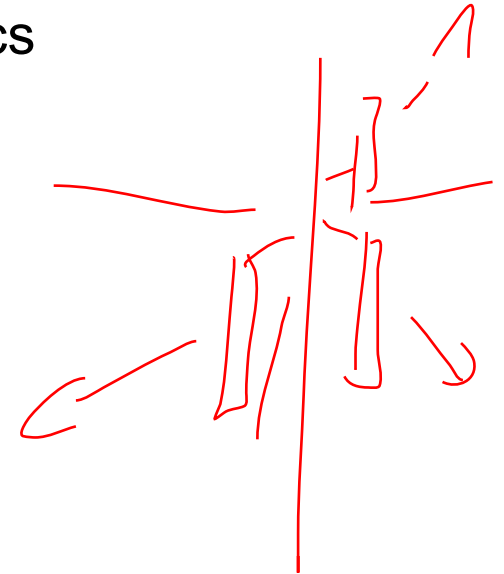
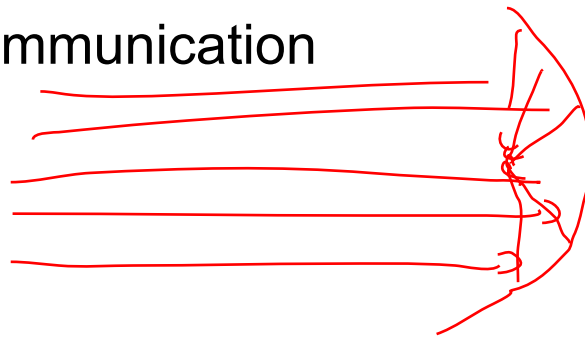
→ Polarization

Space



► Spatial distribution (space multiplexing)

- Utilization of distance loss for the parallel operation of different radio cells → cellular networks
- Using directional antennas for communications directed requested
- GSM antennas with directional characteristics
- Radio with a satellite dish
- laser communications
- infrared communication



Frequency Multiplexing

Bluetooth 7g

- ▶ **Allocation of bandwidth in frequency sections**
- ▶ **Spread of the channels and hopping**
 - Direct Sequence Spread Spectrum (DSSS)
 - Xor a signal with a pseudo-random number sequence at the transmitter and receiver (Relates to code-division multiplexing)
 - Other signals appear as background noise
- ▶ **Frequency Hopping Spread Spectrum (FHSS)**
 - Frequency change by pseudo-random numbers
 - two versions
 - Quick change (almost hopping): Multiple frequencies per user data bits
 - Slowly changing (slow hopping): Multiple user bits per frequency

Time Multiplexing

- **Temporal distribution of sender-/receiver channel**
- **Participants receive exclusive periods (slots) on the media**
- **Accurate synchronization necessary**
- **Coordination necessary, or rigid division**

Direct Sequence Spread Spectrum

- A chip is a bit sequence (given by $\{-1, +1\}$), which encode a smaller set of symbols
- E.g. Transmission signal: $0 = (+1, +1, -1)$, $1 = (-1, -1, +1)$

0	1	0	1
+1 +1 -1	-1 +1 +1	+1 +1 -1	-1 -1 +1

- Coding by calculating the inner product $c_i s_i$ of the received signal and the chip $c_0 = -c_1$:

$$\sum_{i=1}^m c_{0,i} s_i \quad \sum_{i=1}^m c_{1,i} s_i$$

- In the case of a superimposed signal, the original signal can be decoded by filter
- DSSS is used by GPS, WLAN, UMTS, ZigBee, Wireless USB based on the Barker code

- Here for all $v < m$

$$\left| \sum_{i=1}^{N-v} a_i a_{i+v} \right| \leq 1$$

- Barker Code für 11Bit: +1 +1 +1 -1 -1 -1 +1 -1 -1 +1 -1

Code Division Multiple Access (CDMA)

- ▶ **CDMA (Code Division Multiple Access)**
 - e.g. GSM (Global System for Mobile Communication)
 - or UMTS (Universal Mobile Telecommunications System)
- ▶ **Uses chip-sequence with**
 - $C_i \in \{-1, +1\}^m$
 - $-C_i = (-C_{i,1}, -C_{i,2}, \dots, -C_{i,m})$
- ▶ **so that the normalized inner product for all $i \neq j$ the result is 0.**

$$C_i \bullet C_j = \frac{1}{m} C_i \cdot (C_j)^T = \frac{1}{m} \sum_{k=1}^m C_{i,k} C_{j,k} = 0 .$$

- ▶ **Synchronized recipients get a linear combination of A and B**
- ▶ **Multiplying by the desired chip sequence yields the desired message.**

CDMA: Example 1

- ▶ **Sender A:**
 - $0 = (-1, -1)$
 - $1 = (+1, +1)$
- ▶ **Sender B:**
 - $0 = (-1, +1)$
 - $1 = (+1, -1)$
- ▶ **A sends 0, B sends 0:**
 - Result: $(-2, 0)$
- ▶ **C receives $(-2, 0)$:**
 - Decoding of A: $(-2, 0) \cdot (-1, -1) = (-2)(-1) + 0(-1) = 2$
 - A has therefor sent 0 because result is positive

CDMA: Example 2

- ▶ **Sample-code:**
 - Code $C_A = (+1, +1, +1, +1)$
 - Code $C_B = (+1, +1, -1, -1)$
 - Code $C_C = (+1, -1, +1, -1)$
- ▶ **A sends Bit 0, B sends Bit 1, C sends nothing**
 - $V = C_1 + (-C_2) = (0, 0, 2, 2)$
- ▶ **Decoding for A: $V \cdot C_1 = (0, 0, 2, 2) \cdot (+1, +1, +1, +1) = 4/4 = 1$**
 - results in Bit 0
- ▶ **Decoding for B: $V \cdot C_2 = (0, 0, 2, 2) \cdot (+1, +1, -1, -1) = -4/4 = -1$**
 - results in Bit 1
- ▶ **Decoding for C: $V \cdot C_3 = (0, 0, 2, 2) \cdot (+1, -1, +1, -1) = 0$**
 - results in: no Signal.



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