University of Freiburg, Germany Department of Computer Science

Distributed Systems

Chapter 4 Coordination and Agreement

Christian Schindelhauer

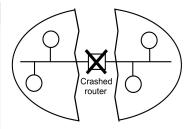
13. May 2013

4.1: Introduction

- Coordination in the absence of master-slave relationship
- Failures and how to deal with it
- Distributed mutual exclusion
- Agreement is a complex problem
- Multicast communication
- Byzantine agreement

Assumptions

- Channels are reliable
- The network remains connected
- Process failures are not a threat to the communication
- Processes only fail by crashing



Failure Detectors

- Failure detector is a service answer queries about the failures of *other* processes
- Most failure detectors are unreliable failure detectors
 - Returning either suspected or unsuspected
 - suspected: some indication of process failure
 - unsuspected: no evidence for process failure
- Reliable failure detector
 - Returning either *failed* or *unsuspected*
 - failed: detector has determined that the process has failed
 - unsuspected: no evidence for failure

Example of an unreliable failure detector

- Each process p sends a 'p is here' message to every other process every T seconds
- If the message does not arrive within T + D seconds then the process is reported as *Suspected*

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4.2: Distributed Mutual Exclusion

- Problem known from operating systems (there: *critical sections*)
- How to achieve mutual exclusion only with messages

Application-Level Protocol

enter()enter critical section – block if necessaryresourceAccesses()access shared resources in critical sectionexit()leave critical section – other processes may enter

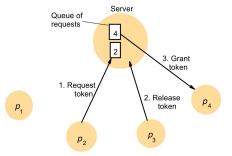
Essential Requirements

ME1: Safety	At most one process may execute the critical section at a
	time
ME2: Liveness	Requests to enter and exist the critical section eventually
	succeed
ME3: \rightarrow ordering	requests enter the critical section according to the
	happened-before relationship

Performance of algorithms for mutual exclusion

- Bandwidth consumed: proportional to the number of messages sent in each entry and exit operation
- Client delay at each entry and exit operation
- Throughput rate of several processes entering the critical section
- Throughput is measured by the synchronization delay between one process exiting the critical section and the next process entering it
- short synchronization delay correspond to high throughput

Central Server Algorithm

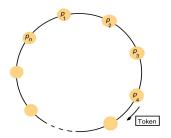


from Distributed Systems - Concepts and Design, Coulouris, Dollimore, Kindberg

- Simplest solution
- Request are handled by queues
- Performance
 - Entering the critical section: two messages (request, grant)
 - Leaving the critical section: one message (release)
- Server is performance bottleneck

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Ring Based Algorithm



from Distributed Systems – Concepts and Design, Coulouris, Dollimore, Kindberg

- Simplest distributed solution
- Arrange processes as ring (not related to physical network)
- A token (permission to enter critical section) is passed around
- Conditions ME1 (safety) and ME2 (liveness) are met
- $\blacksquare ME3: \rightarrow ordering is not fulfilled$
- Continuous consumption of bandwidth
- Synchronisation delay is between 1 and *n* messages.

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The Algorithm of Ricart and Agrawala

- Mutual exclusion between *n* peer processes p_1, p_2, \ldots, p_n which
 - have unique numeric identifiers
 - possess communication channels to one another
 - keep Lamport clocks attached to the messages
- Process states
 - released: outside the critical section
 - wanted: wanting to enter critical section
 - held: being in the critical section
- Each process released immediately answers a request to enter the critical section
- The process with held does not reply to requests until it is finished
- If more than one process requests the entry, the first one collecting the n-1 replies is allowed to enter the critical section.
- If the Lamport clocks of the latest messages do not differ, the numeric ID is used to break the tie.

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The Algorithm of Ricart and Agrawala

```
On initialization

state := RELEASED;

To enter the section

state := WANTED;

Multicast request to all processes;

T := request's timestamp;

Wait until (number of replies received = (N - 1));

state := HELD;
```

```
On receipt of a request <T_i, p_i > at p_j (i \neq j)

if (state = HELD or (state = WANTED and (T, p_j) < (T_i, p_i)))

then

queue request from p_i without replying;

else

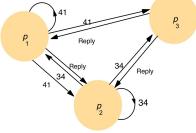
reply immediately to p_i;

end if

To exit the critical section

state := RELEASED;

reply to any queued requests;
```



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from Distributed Systems - Concepts and Design, Coulouris, Dollimore, Kindberg

The Algorithm of Ricart and Agrawala

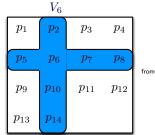
Mutual exclusion properties

- ME1 (safety): processes in state held prevent other ones from entering the CS
- ME2 (liveness): follows from the ordering
- ME3 (ordering): follows from the use of Lamport clocks
- Cost of gaining access: 2(n-1) messages
 - n-1 for multicast of request
 - n − 1 for replies
- Client delay for requesting entry: a round-trip message
- Synchronization delay is one message transmission time

Maekawa's Voting algorithm

- Reduce the number of messages by asking a subset
- For each process p_i choose a voting setV_i such that
 - 1 $p_i \in V_i$
 - 2 $V_i \cap V_j \neq \emptyset$ for all i, j
 - $|V_i| = k \text{ for all } i \text{ (fairness)}$
 - 4 Each process occurs in at most *m* voting sets
- Minimal choice of max $\{m, k\}$ is $k, m \in \Theta(\sqrt{n})$.
- The optimal solution can be approximated by placing all nodes in a square matrix and choosing the row and column as voting set.

Distributed Systems - Concepts and Design, Coulouris, Dollimore, Kindberg



Maekawa's Voting algorithm

On initialization *state* := RELEASED: *voted* := FALSE: For p_i to enter the critical section *state* := WANTED; Multicast *request* to all processes in V_i ; *Wait until* (number of replies received = K); state := HELD; On receipt of a request from p_i at p_i *if* (*state* = HELD *or voted* = TRUE) then queue *request* from p_i without replying; else send *reply* to p_i ; *voted* := TRUE; end if

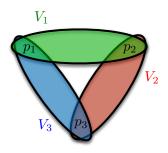
For p_i to exit the critical section state := RELEASED; Multicast release to all processes in V_i ; On receipt of a release from p_i at p_j if (queue of requests is non-empty) then remove head of queue – from p_k , say; send reply to p_k ; voted := TRUE; else voted := FALSE; end if

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Maekawa's Voting algorithm

- Mutual exclusion properties
 - ME1 (safety): follows from the intersections of V_i and V_j
 - ME2 (liveness): not guaranteed.
- Sanders improved this algorithm to achieve ME2 and ME3 (not presented here)
- Cost
 - 2k per entry to the critical section
 - k for exit
 - $O(\sqrt{n})$ messages
- Client delay for requesting entry: a round-trip message
- Synchronization delay is a round-trip message



Mutual Exclusion

Fault Tolerance

- What happens when messages are lost
- What happens when process crashes
- All of the above algorithms presented fail
- We will revisit this problem

4.3: Elections

Election Algorithm

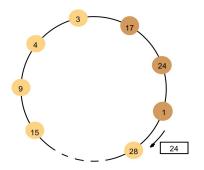
- An algorithm for choosing a unique process from a set of processes p_1, \ldots, p_n .
- A process calls the election if it initiates a run of an election algorithm
- Several elections could run in parallel where subset of processes are *participants* or *non-participants*.
- We assume processes have numeric IDs and that wlog. the process with the highest will be chosen.

Requirements

E1: Safety	During the run each participant has either $elected_i = \bot$ or
	elected _i = P , where P is the non-crashed process with the
	largest ID
E2: Liveness	All participating processes p_i eventually set elected _i $\neq \perp$
	or crash.

Ring-Based Election: Algorithm of Chang and Roberts

- Each process p_i has a communication channel to the next process in the ring p_{(i+1) mod n}
- Messages are sent clockwise
- Assumption: no failures occur
- Non-participants are marked
- When a process receives an election message, it compares the identifier
 - If the arrived ID is greater, it forwards it
 - if the arrived ID is smaller and the process participates, it replaces it with its ID
 - if the arrived ID equals the process ID, the process is elected and sends an elected message around (with its ID).

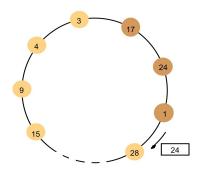


Note: The election was started by process 17. The highest process identifier encountered so far is 24. Participant processes are shown darkened

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Ring-Based Election: Algorithm of Chang and Roberts

- E1 (Safety): follows directly
- E2 (Liveness): follows in the absence of crashes and communication errors
- Worst-case performance if a single node participates in the process
- Time: 3*n* − 1 messages for the election
- Not very practical algorithm fault-prone and high communication overhead
- assumes a-priori knowledge (ring topology)



Note: The election was started by process 17. The highest process identifier encountered so far is 24. Participant processes are shown darkened

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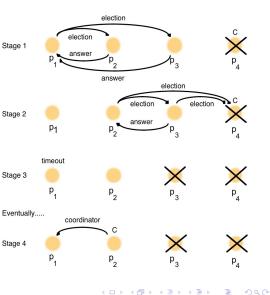
The Bully Algorithm of Garcia & Molina

- The distributed system is assumed to be synchronous
 - \blacksquare i.e. after a timeout period ${\cal T}$ a missing answer is interpreted as crash
 - reliable failure detector
 - fail-stop model
- Message types
 - election: Announces an election
 - answer: Answers election message (contains ID)
 - coordinator: Announces the identity of the elected process
- Any process may trigger an *election*
- Every process receiving an *election* messages sends an *answer* and starts a new one (if it has not started one before).
- If a process knows it has the highest ID (based on the answers) it sends the coordinator message to all processes
- If answers of lower IDs fail to arrive within time *T* the sender considers itself a coordinator and sends the *coordinator* message

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The Bully Algorithm of Garcia & Molina

- If a process receives an election message it sends back an answer messages and begins another election — if it has not begun an election
- If a process knows it has the highest ID it sends the coordinator message
- New arriving processes with higher ID ", bully" existing cordinators



The Bully Algorithm of Garcia & Molina

- E2: liveness condition is guaranteed if messages are transmitted reliably
- E1: safety condition: Not guaranteed if processes are replaced by processes with the same identifier
- different conclusions on which is the coordinator process
- E1 not guaranteed if the timeout value is too small
- In the worst case the algorithm needs $O(n^2)$ messages for *n* processes

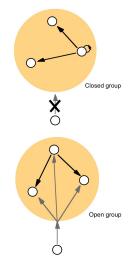
4.4: Multicast communication

- With a single call of multicast(g, m) a process sends a message to all members of the group g
- Using *deliver(m)*, received messages are delivered on participating processes
- Efficiency
 - Number of messages, transmission time
- Delivery guarantees
 - ordering
 - receipt
 - e.g. IP Multicast does not guarantee ordering of success

4.4: Multicast communication

System Model

- multicast(g, m): sends the message m to all members of group g
 - deliver(m): delivers a message to the process (message has been received by lower level)
 - sender(m): sender of a message m (within the message header)
 - group(m): group of a message m (within the message header)
- Allowed senders
 - closed group: senders must be members of a group
 - open group: any process can send a message to the group





Basic Multicast

- *B*-multicast(g, m): for each process $p \in g$, send(p, m)
- *B*-deliver(*m*): if message *m* is received at *p* return the message *m*

Ack Implosion

- if too many processes participate
- if send uses acknowledgments, some of them could be dropped
- then the messages could be retransmitted
- further *acks* are lost due to full buffers etc.



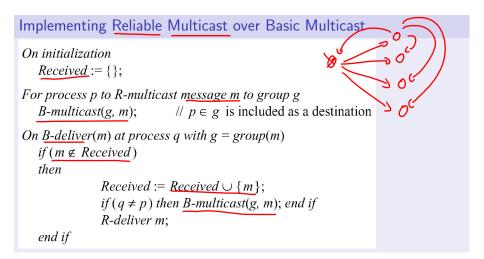


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Reliable Multicast

- Safety: Integrity
 - Every message is delivered at most once
 - Receiver of m is a member of group(m)
 - Sender has initiated a *multicast*(g, m)
- Liveness: Validity
 - If a correct process multicasts a messages then it eventually delivers m (to itself)
- Agreement

If a correct process delivers m then all other processes eventually deliver m



Each message needs to be sent |g| times!

Christian Schindelhauer

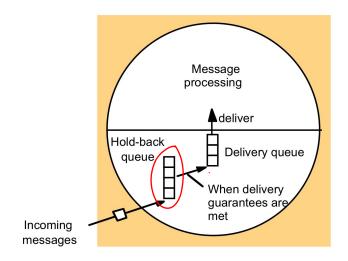
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Implementing Reliable Multicast over IP Multicast

- *R-multicast(g, m)* for sending process p
 - Sender increments a (sending) sequence number S_{g}^{p} for group g after each messages 2
 - Sequence number sent with message
 - Acknowledgements of all received messages with $\langle q, R_g^q \rangle$ are piggybacked with message
 - Negative Acknowledgments: by received sequence number R_{e}^{q} causes retransmission of message
- *R-deliver(g)* for receiving process *q*
 - (R^q_r) 's the sequence number of the latest message it has delivered.
 - it is sent with each acknowledgment and allows the sender (and all receivers) to learn about missing messages
 - Process q delivers a message m (with piggybacked S) only if $S = R_{e}^{q} + 1$.
 - messages with $S > R_{\sigma}^{q} + 1$ are kept in a hold-back queue
 - messages with $S < R_{e}^{\bullet} + 1$ are erased
 - After delivery $R_{\sigma}^q := R_{\sigma}^q + 1$

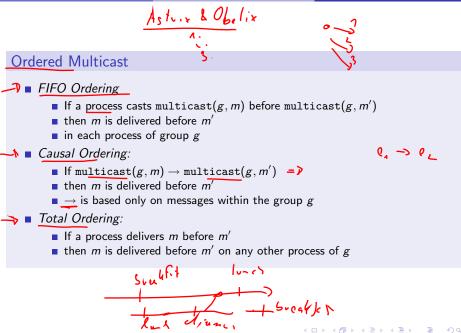
Image: A match a ma

Hold-Back Queue for Arriving Multicast Messages

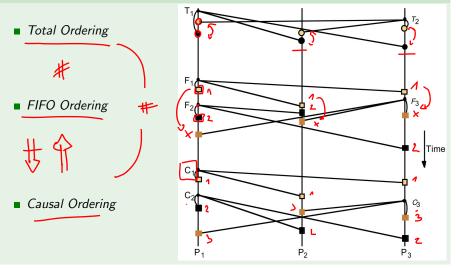


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Total, FIFO and Causal Ordering



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TCPI



- Use sequence numbers for each message

 - R_g^p for the last message delivered to process p of group g
- Multiast over IP Multicast satisfies FIFO ordering
- Essential components for FIFO ordering:
 - Sender piggybacks S^p_g on the message
 - <u>Receiver</u> checks wether received message satisfies $S = R_g^q + 1$
 - and delivers *m* and sets $\underline{R_g^q} := R_g^q + 1$.
 - if $S > R_g^q + 1$ it puts *m* into the hold-back queue
- In combination of a reliable multicast we obtain a reliable FIFO ordering multicast algorithm

Implementing Total Ordering Multicast with a Sequencer

- 1. Algorithm for group member p
- A sequencer is an extra process taking care about ordering
- A sender process sends message with unique ID i to sequencer.
- Sequencer marks message with ordering and multicasts the message

On initialization: $r_g := 0;$

To TO-multicast message m to group g B-multicast($g \cup \{sequencer(g)\}, \le m, i >$);

On <u>B-deliver($\leq m, i \geq$)</u> with g = group(m)Place $\leq m, i \geq$ in hold-back queue;

- On B-deliver($m_{order} = \leq \text{``order''}, i, S >$) with $g = group(m_{order})$ wait until $\leq m, i >$ in hold-back queue and $S = r_g$; TO-deliver m; // (after deleting it from the hold-back queue) $r_g = S + 1$;
- 2. Algorithm for sequencer of g On initialization: $s_g := 0$; On B-deliver($\leq m, i >$) with g = group(m)B-multicast(g, < 'order'', $i, s_g >$); $s_g := s_g + 1$;



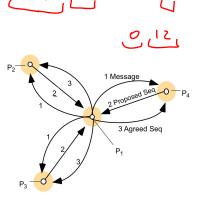
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Implementing Total Ordering Multicast using ISIS

- Used in the ISIS toolkit of Birman & Joseph
- Each participating process proposes a sequence number for a messages
 - All proposed message numbers are unique
 - The sender chooses the maximum of all proposals and sends this information (piggybacked with the next messages)
 - This agreed sequence number defines the ordering of the hold-back-queue
 - The smallest elements of the hold-back queue can be delivered as the first element
- Does not imply causal nor FIFO ordering



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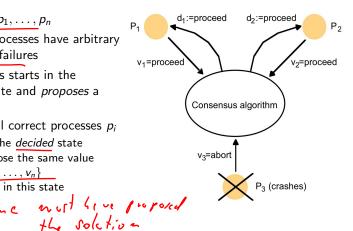
Implementing Causal Ordering

- Uses vector clocks to keep causal ordering (piggybacked to messages)
- Vector clock
 V^g_i[i] counts all
 multicast
 messages of
 process i in
 group g

 hold-back queue reflects vector clocks Algorithm for group member p_i (i = 1, 2..., N)On initialization $V_i^g[j] := 0$ (j = 1, 2..., N); To CO-multicast message m to group g $V_i^g[i] := V_i^g[i] + 1$; B-multicast(g, $\langle V_i^g, m \rangle$); On B-deliver($\langle V_j^g, m \rangle$) from p_j , with g = group(m)place $\langle V_j^g, m \rangle$ in hold-back queue; wait until $V_i^g[j] = V_i^g[j] + 1$ and $V_j^g[k] \leq V_i^g[k]$ $(k \neq j)$; CO-deliver m; // after removing it from the hold-back queue $V_i^g[j] := V_i^g[j] + 1$;

4.5: Consensus

- *n* processes p_1, \ldots, p_n
- at most f processes have arbitrary (Byzantine) failures
- Every process starts in the undecidedstate and proposes a value vi
- Eventually all correct processes p_i
 - choose the decided state
 - and choose the same value $d_i \in \{v_1,\ldots,v_n\}$
 - and stay in this state

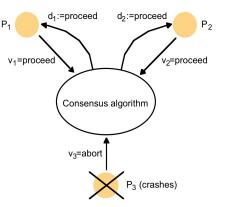


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Consensus Problem

- Termination: Eventually each correct process p_i is decided by setting variable d_i
- Agreement: The decision value d_i of all correct processes is the same
- Integrity: If all correct process proposed the same value v, then d_i = v for all correct p_i
- Possible decision functions: majority, minimum, maximum, ...
- Byzantine failures can cause irritating and adversarial messages
- System crashes may not be detected

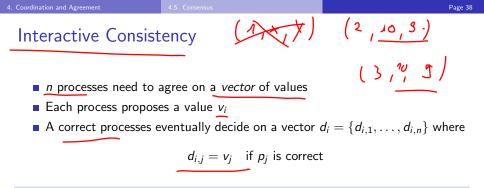


Byzantine Generals Problem

- n generals have to agree on attack or retreat
- one of them is the commander and issues the order
- at most <u>f</u> generals are traitors (possibly also the commander) and have adversarial behavior
- all correct generals have eventually to agree on the commander decision if he acts correctly

Consensus Problem

- Termination: Eventually each correct process p_i is decided by setting variable d_i
- Agreement: The decision value d_i of all correct processes is the same
- Integrity: If the commander is correct then all correct processes choose the commander's proposal



Interactive Consistency

- Termination: Eventually each correct process p_i is decided by setting variable d_i
- Agreement: The decision value d_i of all correct processes is the same

• Integrity: If the p_j is correct then all correct processes p_i set $d_{i,j} = v_j$

The Relationship between Consensus Problems

Assume solutions to Consensus (C), Byzantine generals (BG), interactive consistency (IC)

- $C_i(v_1, \ldots, v_n)$ = consensus decision value of p_i for proposals v_i
 - $BG_i(j, v) = BG$ decision value of p_i for commander p_j proposal v_j
- $IC_i(v_1, ..., v_n)[j] = j$ -th position of interactive consistency decision vector of p_i for proposals v_i

Solving IC from BG

In parallel *n* Byzantine generals problems are solved

• each process p_j acts as commander once

 $IC_i(v_1,\ldots,v_n)[j] = BG_i(j,v)$

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- \blacksquare majority returns the most often parameter or \bot if no such value exists
- for all $i = 1, \ldots, n$

$$C_i(v_1,\ldots,v_n) = majority(IC_i(v_1,\ldots,v_n)[1],\ldots,IC_i(v_1,\ldots,v_n)[n])$$

Solving BG from C

- The commander p_j sends its proposed value to itself and each other process
- All processes run consenus with the values v_1, \ldots, v_n received from the commander
- for all $i = 1, \ldots, n$

$$BG_i(j, v) = C_i(v_1, \ldots, v_n)$$

Consensus in a Synchronous System

- Assume that there are no arbitrary (Byzantine) errors
- Given a synchronous distributed systems (fail-stop model)
- Use basic multicast for f + 1 rounds
- Multicast all known values of all participants
- Values^r_i denotes the set of proposed variables at the beginning of round r
- Reduce communication overhead by multicasting only freshly arrived variables Values^r_i - Values^{r-1}
- Choose the minimum of all known values as final value

Consensus in a Synchronous System

Algorithm for process $p_i \in g$; algorithm proceeds in f + 1 rounds

```
On initialization
     Values_{i}^{1} := \{v_{i}\}; Values_{i}^{0} = \{\};
In round r (1 \le r \le f + 1)
    B-multicast(g, Values_i^r - Values_i^{r-1}); // Send only values that have not been sent Values_i^{r+1} := Values_i^r;
    while (in round r)
                      On B-deliver(V_j) from some p_j
Values<sub>i</sub><sup>r+1</sup> := Values<sub>i</sub><sup>r+1</sup> \cup V_j;
After (f+1) rounds
    Assign d_i = minimum(Values_i^{f+1});
```

Consensus in a Synchronous System

- There are no arbitrary errors only processes that crash and are correctly detected
- Given a synchronous distributed systems (fail-stop model)
- Correctness
 - Assume that two processes p_i and p_j have different values at round r
 - Then, in round r 1 at least one process p_k has sent different values to p_i and p_j
 - Then, *p_k* has crashed in this round
 - Since the number of crashes is limited to f there are not enough crashes to cover each of the f + 1 rounds

Byzantine Generals Problem in a Synchronous System

- Assume that there are Byzantine errors
- Given a synchronous distributed system
 - crashes are detected
 - other wrong behavior can not detected, e.g. strange messages
- The messages are not (digitally) signed $i_{i} i_{i} ? = NPL$
- at most f faulty processes

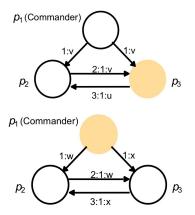
Impossibility of a solution of the Byzantine generals problem [Lamport, Shostak, Pease 1982]

- The byzantine generals problem cannot be solved for n = 3 and f = 1.
- The byzantine generals problem cannot be solved for $n \le 3f$.

Byzantine Generals Problem in a Synchronous System

Impossibility of a solution of the Byzantine generals problem for n = 3

- The byzantine generals problem with arbitrary failures cannot be solved for n = 3 and f = 1 in a synchronous system.
 - a faulty commander sending different values to his generals
 - cannot be distinguished from a faulty general forwarding wrong values



Solution of the Byzantine Generals Problem

- Assume that there are **Byzantine** errors
- Given a synchronous distributed system
- messages are not (digitally) signed
- at most f faulty processes

Solution of the Byzantine generals problem [Pease, Shostak, Lamport 1980]

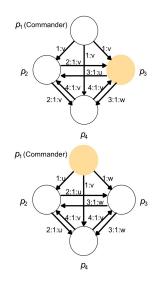
- The byzantine generals problem can be solved for n = 4 and f = 1.
- The byzantine generals problem can be solved for $n \ge 3f + 1$.

Solution for Four Generals and One Faulty Process

• The byzantine generals problem can be solved for $n \ge 4$ and f = 1.

Algorithm of Pease et al.

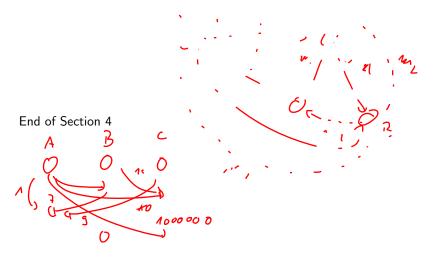
- The commander sends a value to all other generals (lieutenants)
- 2 All lieutenants send the received value to all other lieutenants
- 3 The commander chooses its value; the lieutenants compute the majority of all received values
- Since <u>n ≥ 4 the majority function always can</u> be computed if at most one process is faulty
- If the commander crashes very early then all lieutenants agree on \perp



More About the Byzantine Generals Problems

• For f > 1 the algorithm can be used recursively

- Complexity: f + 1 rounds and $O(n^{f+1})$ messages
- The time complexity of f + 1 rounds is optimal
- With the help of signed messages
 - any number of faulty generals f < n can be dealt with
 - with signed messages the Byzantine Generals problem can be solved in f + 1 rounds with $O(n^2)$ messages [Dolev & Strong 1983]
- For asynchronous systems with crash failures
 - No algorithm can reach consensus even if only **one processor** is faulty [Fischer, Lynch, Paterson 1985]
 - Each algorithm that tries to reach consensus can be confronted with a faulty process which influences the result if it continues (instead of crashing)



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