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Distributed Systems

Chapter 4 Coordination and Agreement

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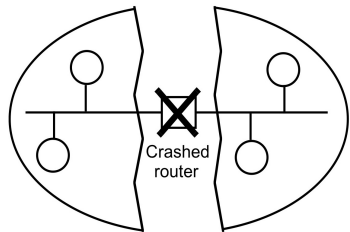
13. May 2013

4.1: Introduction

- Coordination in the absence of master-slave relationship
- Failures and how to deal with it
- Distributed mutual exclusion
- Agreement is a complex problem
- Multicast communication
- Byzantine agreement

Assumptions

- Channels are reliable
- The network remains connected
- Process failures are not a threat to the communication
- Processes only fail by crashing



Failure Detectors

- Failure detector is a service answer queries about the failures of *other* processes
- Most failure detectors are *unreliable failure detectors*
 - Returning either *suspected* or *unsuspected*
 - *suspected*: some indication of process failure
 - *unsuspected*: no evidence for process failure
- *Reliable failure detector*
 - Returning either *failed* or *unsuspected*
 - *failed*: detector has determined that the process has failed
 - *unsuspected*: no evidence for failure

Example of an unreliable failure detector

- Each process p sends a 'p is here' message to every other process every T seconds
- If the message does not arrive within $T + D$ seconds then the process is reported as *Suspected*

4.2: Distributed Mutual Exclusion

- Problem known from operating systems (there: *critical sections*)
- How to achieve mutual exclusion only with messages

Application-Level Protocol

<code>enter()</code>	enter critical section – block if necessary
<code>resourceAccesses()</code>	access shared resources in critical section
<code>exit()</code>	leave critical section – other processes may enter

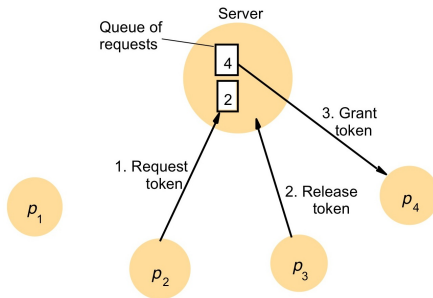
Essential Requirements

ME1: Safety	At most one process may execute the critical section at a time
ME2: Liveness	Requests to enter and exist the critical section eventually succeed
ME3: \rightarrow ordering	requests enter the critical section according to the <i>happened-before</i> relationship

Performance of algorithms for mutual exclusion

- *Bandwidth* consumed: proportional to the number of messages sent in each *entry* and *exit* operation
- *Client delay* at each *entry* and *exit* operation
- *Throughput* rate of several processes entering the critical section
- Throughput is measured by the *synchronization delay* between one process exiting the critical section and the next process entering it
- short *synchronization delay* correspond to high *throughput*

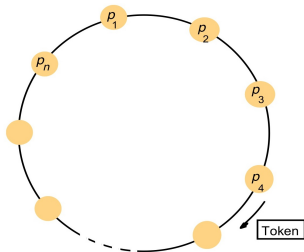
Central Server Algorithm



from *Distributed Systems – Concepts and Design*, Coulouris, Dollimore, Kindberg

- Simplest solution
- Request are handled by queues
- Performance
 - Entering the critical section: two messages (*request*, *grant*)
 - Leaving the critical section: one message (*release*)
- Server is performance bottleneck

Ring Based Algorithm



from *Distributed Systems – Concepts and Design*,

Coulouris, Dollimore, Kindberg

- Simplest distributed solution
- Arrange processes as ring (not related to physical network)
- A token (permission to enter critical section) is passed around
- Conditions ME1 (safety) and ME2 (liveness) are met
- ME3: → ordering is not fulfilled
- Continuous consumption of bandwidth
- Synchronisation delay is between 1 and n messages.

The Algorithm of Ricart and Agrawala

- Mutual exclusion between n peer processes p_1, p_2, \dots, p_n which
 - have unique numeric identifiers
 - possess communication channels to one another
 - keep Lamport clocks attached to the messages
- Process states
 - released: outside the critical section
 - wanted: wanting to enter critical section
 - held: being in the critical section
- Each process released immediately answers a request to enter the critical section
- The process with held does not reply to requests until it is finished
- If more than one process requests the entry, the first one collecting the $n - 1$ replies is allowed to enter the critical section.
- If the Lamport clocks of the latest messages do not differ, the numeric ID is used to break the tie.

The Algorithm of Ricart and Agrawala

On initialization

state := RELEASED;

To enter the section

state := WANTED;

Multicast *request* to all processes;

T := request's timestamp;

Wait until (number of replies received = $(N - 1)$);

state := HELD;

request processing deferred here

On receipt of a request $\langle T_i, p_i \rangle$ at p_j ($i \neq j$)

if (*state* = HELD or (*state* = WANTED and $(T, p_j) < (T_i, p_i)$))

then

 queue *request* from p_i without replying;

else

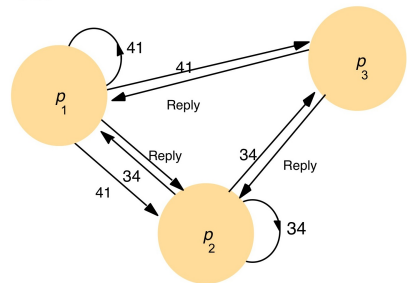
 reply immediately to p_i ;

end if

To exit the critical section

state := RELEASED;

reply to any queued requests;

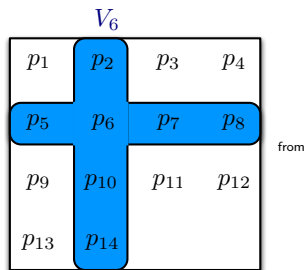


The Algorithm of Ricart and Agrawala

- Mutual exclusion properties
 - ME1 (safety): processes in state `held` prevent other ones from entering the CS
 - ME2 (liveness): follows from the ordering
 - ME3 (ordering): follows from the use of Lamport clocks
- Cost of gaining access: $2(n - 1)$ messages
 - $n - 1$ for multicast of request
 - $n - 1$ for replies
- Client delay for requesting entry: a round-trip message
- Synchronization delay is one message transmission time

Maekawa's Voting algorithm

- Reduce the number of messages by asking a subset
- For each process p_i choose a *voting set* V_i such that
 - 1 $p_i \in V_i$
 - 2 $V_i \cap V_j \neq \emptyset$ for all i, j
 - 3 $|V_i| = k$ for all i (fairness)
 - 4 Each process occurs in at most m voting sets
- Minimal choice of $\max\{m, k\}$ is $k, m \in \Theta(\sqrt{n})$.
- The optimal solution can be approximated by placing all nodes in a square matrix and choosing the row and column as voting set.



Distributed Systems – Concepts and Design, Coulouris, Dollimore, Kindberg

Maekawa's Voting algorithm

On initialization

state := RELEASED;

voted := FALSE;

For p_i *to enter the critical section*

state := WANTED;

Multicast *request* to all processes in V_i ;

Wait until (number of replies received = K);

state := HELD;

On receipt of a request from p_i *at* p_j

if (*state* = HELD or *voted* = TRUE)

then

 queue *request* from p_i without replying;

else

 send *reply* to p_i ;

voted := TRUE;

end if

For p_i *to exit the critical section*

state := RELEASED;

Multicast *release* to all processes in V_i ;

On receipt of a release from p_i *at* p_j

if (queue of requests is non-empty)

then

 remove head of queue – from p_k , say;

 send *reply* to p_k ;

voted := TRUE;

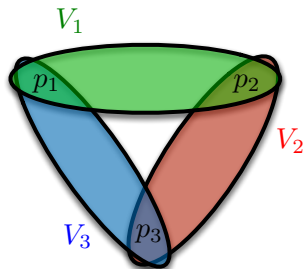
else

voted := FALSE;

end if

Maekawa's Voting algorithm

- Mutual exclusion properties
 - ME1 (safety): follows from the intersections of V_i and V_j
 - ME2 (liveness): not guaranteed.
- Sanders improved this algorithm to achieve ME2 and ME3 (not presented here)
- Cost
 - $2k$ per entry to the critical section
 - k for exit
 - $O(\sqrt{n})$ messages
- Client delay for requesting entry: a round-trip message
- Synchronization delay is a round-trip message



Mutual Exclusion

Fault Tolerance

- What happens when messages are lost
 - What happens when process crashes
-
- All of the above algorithms presented fail
 - We will revisit this problem

4.3: Elections

Election Algorithm

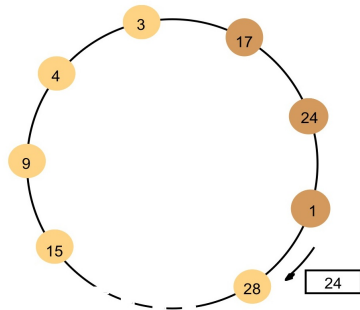
- An algorithm for choosing a unique process from a set of processes p_1, \dots, p_n .
- A process *calls the election* if it initiates a run of an election algorithm
- Several elections could run in parallel where subset of processes are *participants* or *non-participants*.
- We assume processes have numeric IDs and that wlog. the process with the highest will be chosen.

Requirements

- E1: Safety During the run each participant has either $\text{elected}_i = \perp$ or $\text{elected}_i = P$, where P is the non-crashed process with the largest ID
- E2: Liveness All participating processes p_i eventually set $\text{elected}_i \neq \perp$ or crash.

Ring-Based Election: Algorithm of Chang and Roberts

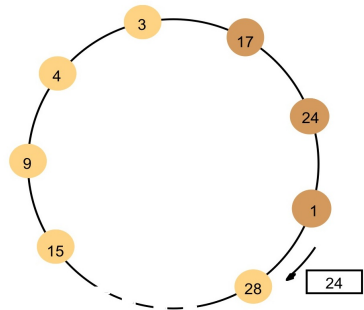
- Each process p_i has a communication channel to the next process in the ring $p_{(i+1) \bmod n}$
- Messages are sent clockwise
- Assumption: no failures occur
- Non-participants are marked
- When a process receives an election message, it compares the identifier
 - If the arrived ID is greater, it forwards it
 - if the arrived ID is smaller and the process participates, it replaces it with its ID
 - if the arrived ID equals the process ID, the process is elected and sends an elected message around (with its ID).



Note: The election was started by process 17.
The highest process identifier encountered so far is 24.
Participant processes are shown darkened

Ring-Based Election: Algorithm of Chang and Roberts

- E1 (Safety): follows directly
- E2 (Liveness): follows in the absence of crashes and communication errors
- Worst-case performance if a single node participates in the process
- Time: $3n - 1$ messages for the election
- Not very practical algorithm fault-prone and high communication overhead
- assumes a-priori knowledge (ring topology)



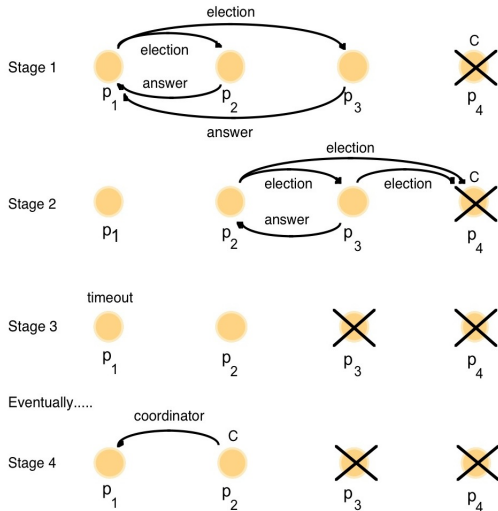
Note: The election was started by process 17.
The highest process identifier encountered so far is 24.
Participant processes are shown darkened

The Bully Algorithm of Garcia & Molina

- The distributed system is assumed to be synchronous
 - i.e. after a timeout period T a missing answer is interpreted as crash
 - reliable failure detector
 - fail-stop model
- Message types
 - *election*: Announces an election
 - *answer*: Answers *election* message (contains ID)
 - *coordinator*: Announces the identity of the elected process
- Any process may trigger an *election*
- Every process receiving an *election* messages sends an *answer* and starts a new one (if it has not started one before).
- If a process knows it has the highest ID (based on the answers) it sends the *coordinator* message to all processes
- If answers of lower IDs fail to arrive within time T the sender considers itself a coordinator and sends the *coordinator* message

The Bully Algorithm of Garcia & Molina

- If a process receives an *election* message it sends back an *answer* messages and begins another election — if it has not begun an election
- If a process knows it has the highest ID it sends the *coordinator* message
- New arriving processes with higher ID „bully“ existing coordinators



The Bully Algorithm of Garcia & Molina

- E2: liveness condition is guaranteed if messages are transmitted reliably
- E1: safety condition: Not guaranteed if processes are replaced by processes with the same identifier
- different conclusions on which is the coordinator process
- E1 not guaranteed if the timeout value is too small
- In the worst case the algorithm needs $O(n^2)$ messages for n processes

4.4: Multicast communication

- With a single call of $multicast(g, m)$ a process sends a message to all members of the group g
- Using $deliver(m)$, received messages are delivered on participating processes
- *Efficiency*
 - Number of messages, transmission time
- *Delivery guarantees*
 - ordering
 - receipt
 - e.g. IP Multicast does not guarantee ordering of success

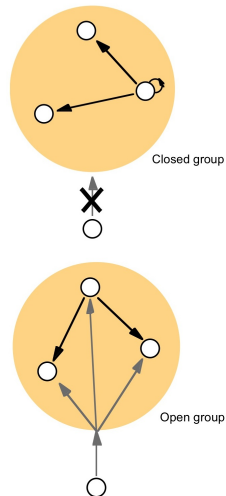
4.4: Multicast communication

■ System Model

- $multicast(g, m)$: sends the message m to all members of group g
- $deliver(m)$: delivers a message to the process (message has been received by lower level)
- $sender(m)$: sender of a message m (within the message header)
- $group(m)$: group of a message m (within the message header)

■ Allowed senders

- closed group: senders must be members of a group
- open group: any process can send a message to the group



Basic Multicast

- $B\text{-multicast}(g, m)$: for each process $p \in g$, $send(p, m)$
- $B\text{-deliver}(m)$: if message m is received at p return the message m

Ack Implosion

- if too many processes participate
- if $send$ uses acknowledgments, some of them could be dropped
- then the messages could be retransmitted
- further $acks$ are lost due to full buffers etc.

Reliable Multicast

- *Safety: Integrity*
 - Every message is delivered at most once
 - Receiver of m is a member of $group(m)$
 - Sender has initiated a $multicast(g, m)$
- *Liveness: Validity*
 - If a correct process multicasts a messages then it eventually delivers m (to itself)
- *Agreement*
 - If a correct process delivers m then all other processes eventually deliver m

Implementing Reliable Multicast over Basic Multicast

On initialization

Received := {};

For process p to R-multicast message m to group g

B-multicast(g, m); // $p \in g$ is included as a destination

On B-deliver(m) at process q with g = group(m)

if (m \notin Received)

then

Received := Received \cup {m};

if (q \neq p) then B-multicast(g, m); end if

R-deliver m;

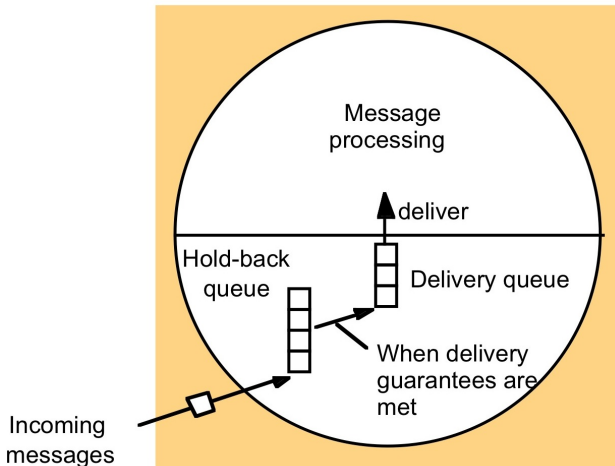
end if

Each message needs to be sent $|g|$ times!

Implementing Reliable Multicast over IP Multicast

- R -multicast(g, m) for sending process p
 - Sender increments a (sending) sequence number S_g^p for group g after each messages
 - Sequence number sent with message
 - Acknowledgements of all received messages with $\langle q, R_g^q \rangle$ are piggybacked with message
 - Negative Acknowledgments: by received sequence number R_g^q causes retransmission of message
- R -deliver(g) for receiving process q
 - R_g^q is the sequence number of the latest message it has delivered.
 - it is sent with each acknowledgment and allows the sender (and all receivers) to learn about missing messages
 - Process q *delivers* a message m (with piggybacked S) only if $S = R_g^q + 1$.
 - messages with $S > R_g^q + 1$ are kept in a hold-back queue
 - messages with $S < R_g^q + 1$ are erased
 - After delivery $R_g^q := R_g^q + 1$

Hold-Back Queue for Arriving Multicast Messages



Ordered Multicast

■ *FIFO Ordering*

- If a process casts $\text{multicast}(g, m)$ before $\text{multicast}(g, m')$
- then m is delivered before m'
- in each process of group g

■ *Causal Ordering:*

- If $\text{multicast}(g, m) \rightarrow \text{multicast}(g, m')$
- then m is delivered before m'
- \rightarrow is based only on messages within the group g

■ *Total Ordering:*

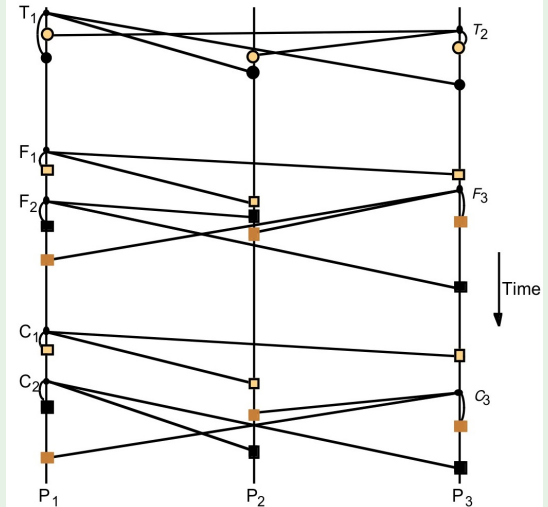
- If a process delivers m before m'
- then m is delivered before m' on any other process of g

Total, FIFO and Causal Ordering

■ *Total Ordering*

■ *FIFO Ordering*

■ *Causal Ordering*



Bulletin Board

Bulletin board: *os.interesting*

Item	From	Subject
23	A.Hanlon	Mach
24	G.Joseph	Microkernels
25	A.Hanlon	Re: Microkernels
26	T.L'Heureux	RPC performance
27	M.Walker	Re: Mach
end		

- *FIFO Ordering*
- *Causal Ordering*
- *Total Ordering*

Implementing FIFO Ordering Multicast

- Use sequence numbers for each message
 - S_g^p for each sender process p and group g
 - R_g^p for the last message delivered to process p of group g
- Multicast over IP Multicast satisfies FIFO ordering
- Essential components for FIFO ordering:
 - Sender piggybacks S_g^p on the message
 - Receiver checks whether received message satisfies $S = R_g^q + 1$
 - and delivers m and sets $R_g^q := R_g^q + 1$.
 - if $S > R_g^q + 1$ it puts m into the hold-back queue
- In combination of a reliable multicast we obtain a reliable FIFO ordering multicast algorithm

Implementing Total Ordering Multicast with a Sequencer

- A sequencer is an extra process taking care about ordering
- A sender process sends message with unique ID i to sequencer
- Sequencer marks message with ordering and multicasts the message

1. Algorithm for group member p

On initialization: $r_g := 0$;

To TO-multicast message m to group g
B-multicast($g \cup \{\text{sequencer}(g)\}$, $\langle m, i \rangle$);

On B-deliver($\langle m, i \rangle$) with $g = \text{group}(m)$
 Place $\langle m, i \rangle$ in hold-back queue;

On B-deliver($m_{\text{order}} = \langle \text{"order"}, i, S \rangle$) with $g = \text{group}(m_{\text{order}})$
 wait until $\langle m, i \rangle$ in hold-back queue and $S = r_g$;
TO-deliver m ; // (after deleting it from the hold-back queue)
 $r_g = S + 1$;

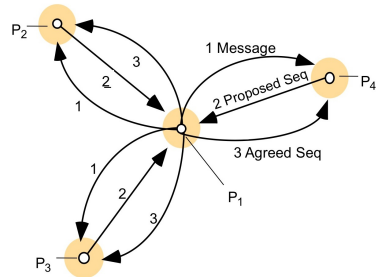
2. Algorithm for sequencer of g

On initialization: $s_g := 0$;

On B-deliver($\langle m, i \rangle$) with $g = \text{group}(m)$
B-multicast(g , $\langle \text{"order"}, i, s_g \rangle$);
 $s_g := s_g + 1$;

Implementing Total Ordering Multicast using ISIS

- Used in the ISIS toolkit of Birman & Joseph
- Each participating process proposes a sequence number for a messages
 - All proposed message numbers are unique
 - The sender chooses the maximum of all proposals and sends this information (piggybacked with the next messages)
 - This agreed sequence number defines the ordering of the hold-back-queue
 - The smallest elements of the hold-back queue can be delivered as the first element
- Does not imply causal nor FIFO ordering



Implementing Causal Ordering

- Uses vector clocks to keep causal ordering (piggybacked to messages)
- Vector clock V_i^g counts all multicast messages of process i in group g
- hold-back queue reflects vector clocks

Algorithm for group member p_i ($i = 1, 2, \dots, N$)

On initialization

$$V_i^g[j] := 0 \quad (j = 1, 2, \dots, N);$$

To CO-multicast message m to group g

$$V_i^g[i] := V_i^g[i] + 1;$$

$$B\text{-multicast}(g, \langle V_i^g, m \rangle);$$

On B-deliver($\langle V_j^g, m \rangle$) from p_j , with $g = \text{group}(m)$

place $\langle V_j^g, m \rangle$ in hold-back queue;

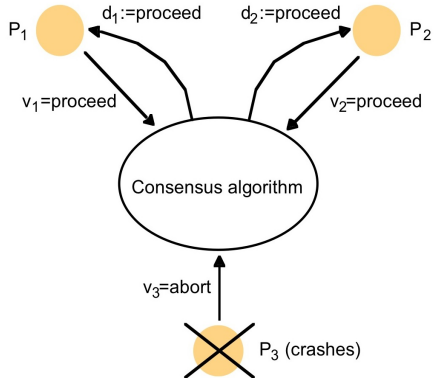
wait until $V_j^g[j] = V_i^g[j] + 1$ and $V_j^g[k] \leq V_i^g[k]$ ($k \neq j$);

CO-deliver m ; // after removing it from the hold-back queue

$$V_i^g[j] := V_i^g[j] + 1;$$

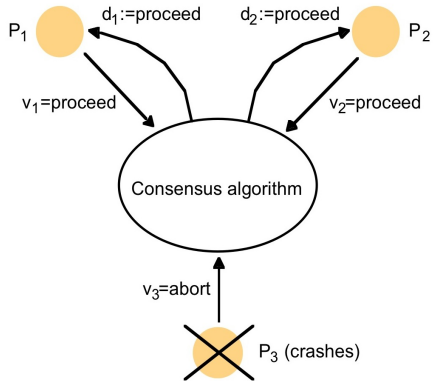
4.5: Consensus

- n processes p_1, \dots, p_n
- at most f processes have arbitrary (Byzantine) failures
- Every process starts in the *undecided* state and *proposes* a value v_i
- Eventually all correct processes p_i
 - choose the *decided* state
 - and choose the same value $d_i \in \{v_1, \dots, v_n\}$
 - and stay in this state



Consensus Problem

- **Termination:** Eventually each correct process p_i is *decided* by setting variable d_i
 - **Agreement:** The decision value d_i of all correct processes is the same
 - **Integrity:** If all correct process proposed the same value v , then $d_i = v$ for all correct p_i
-
- Possible decision functions: *majority, minimum, maximum, ...*
 - Byzantine failures can cause irritating and adversarial messages
 - System crashes may not be detected



Byzantine Generals Problem

- n generals have to agree on attack or retreat
- one of them is the commander and issues the order
- at most f generals are traitors (possibly also the commander) and have adversarial behavior
- all correct generals have eventually to agree on the commander decision if he acts correctly

Consensus Problem

- *Termination*: Eventually each correct process p_i is *decided* by setting variable d_i
- *Agreement*: The decision value d_i of all correct processes is the same
- *Integrity*: If the commander is correct then all correct processes choose the commander's proposal

Interactive Consistency

- n processes need to agree on a *vector* of values
- Each process proposes a value v_i
- A correct processes eventually decide on a vector $d_i = \{d_{i,1}, \dots, d_{i,n}\}$ where

$$d_{i,j} = v_j \quad \text{if } p_j \text{ is correct}$$

Interactive Consistency

- *Termination*: Eventually each correct process p_i is *decided* by setting variable d_i
- *Agreement*: The decision value d_i of all correct processes is the same
- *Integrity*: If the p_j is correct then all correct processes p_i set $d_{i,j} = v_j$

The Relationship between Consensus Problems

Assume solutions to Consensus (C), Byzantine generals (BG), interactive consistency (IC)

$C_i(v_1, \dots, v_n)$ = consensus decision value of p_i for proposals v_i

$BG_i(j, v)$ = BG decision value of p_i for commander p_j proposal v_j

$IC_i(v_1, \dots, v_n)[j]$ = j -th position of interactive consistency decision vector of p_i for proposals v_i

Solving IC from BG

- In parallel n Byzantine generals problems are solved
- each process p_j acts as commander once

$$IC_i(v_1, \dots, v_n)[j] = BG_i(j, v)$$

The Relationship between Consensus Problems

Solving C from IC

- *majority* returns the most often parameter or \perp if no such value exists
- for all $i = 1, \dots, n$

$$C_i(v_1, \dots, v_n) = \text{majority}(IC_i(v_1, \dots, v_n)[1], \dots, IC_i(v_1, \dots, v_n)[n])$$

Solving BG from C

- The commander p_j sends its proposed value to itself and each other process
- All processes run consensus with the values v_1, \dots, v_n received from the commander
- for all $i = 1, \dots, n$

$$BG_i(j, v) = C_i(v_1, \dots, v_n)$$

Consensus in a Synchronous System

- Assume that there are no arbitrary (Byzantine) errors
- Given a synchronous distributed systems (fail-stop model)
- Use basic multicast for $f + 1$ rounds
- Multicast all known values of all participants
- $Values_i^r$ denotes the set of proposed variables at the beginning of round r
- Reduce communication overhead by multicasting only freshly arrived variables $Values_i^r - Values_i^{r-1}$
- Choose the minimum of all known values as final value

Consensus in a Synchronous System

Algorithm for process $p_i \in g$; algorithm proceeds in $f + 1$ rounds

On initialization

$$Values_i^1 := \{v_i\}; Values_i^0 = \{\};$$

In round r ($1 \leq r \leq f + 1$)

$$B\text{-multicast}(g, Values_i^r - Values_i^{r-1}); // \text{ Send only values that have not been sent}$$

$$Values_i^{r+1} := Values_i^r;$$

while (in round r)

{

$$\begin{aligned} & \text{On } B\text{-deliver}(V_j) \text{ from some } p_j \\ & Values_i^{r+1} := Values_i^{r+1} \cup V_j; \end{aligned}$$

}

After $(f + 1)$ rounds

$$\text{Assign } d_i = \text{minimum}(Values_i^{f+1});$$

Consensus in a Synchronous System

- There are no arbitrary errors only processes that crash and are correctly detected
- Given a synchronous distributed systems (fail-stop model)
- Correctness
 - Assume that two processes p_i and p_j have different values at round r
 - Then, in round $r - 1$ at least one process p_k has sent different values to p_i and p_j
 - Then, p_k has crashed in this round
 - Since the number of crashes is limited to f there are not enough crashes to cover each of the $f + 1$ rounds

Byzantine Generals Problem in a Synchronous System

- Assume that there are **Byzantine** errors
- Given a synchronous distributed system
 - crashes are detected
 - other wrong behavior can not detected, e.g. strange messages
- messages are not (digitally) signed
- at most f faulty processes

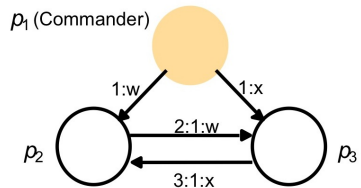
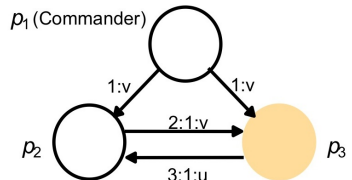
Impossibility of a solution of the Byzantine generals problem [Lamport, Shostak, Pease 1982]

- The byzantine generals problem cannot be solved for $n = 3$ and $f = 1$.
- The byzantine generals problem cannot be solved for $n \leq 3f$.

Byzantine Generals Problem in a Synchronous System

Impossibility of a solution of the Byzantine generals problem for $n = 3$

- The byzantine generals problem with arbitrary failures cannot be solved for $n = 3$ and $f = 1$ in a synchronous system.
 - a faulty commander sending different values to his generals
 - cannot be distinguished from a faulty general forwarding wrong values



Solution of the Byzantine Generals Problem

- Assume that there are **Byzantine** errors
- Given a synchronous distributed system
- messages are not (digitally) signed
- at most f faulty processes

Solution of the Byzantine generals problem [Pease, Shostak, Lamport 1980]

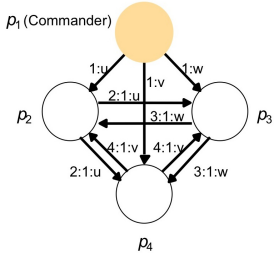
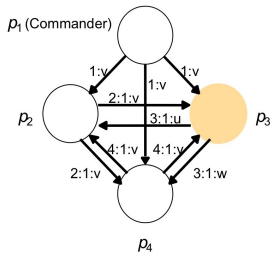
- The byzantine generals problem **can** be solved for $n = 4$ and $f = 1$.
- The byzantine generals problem **can** be solved for $n \geq 3f + 1$.

Solution for Four Generals and One Faulty Process

- The byzantine generals problem can be solved for $n \geq 4$ and $f = 1$.

Algorithm of Pease et al.

- 1 The commander sends a value to all other generals (lieutenants)
- 2 All lieutenants send the received value to all other lieutenants
- 3 The commander chooses its value; the lieutenants compute the majority of all received values



- Since $n \geq 4$ the majority function always can be computed if at most one process is faulty
- If the commander crashes very early then all lieutenants agree on \perp

More About the Byzantine Generals Problems

- For $f > 1$ the algorithm can be used recursively
 - Complexity: $f + 1$ rounds and $O(n^{f+1})$ messages
 - The time complexity of $f + 1$ rounds is optimal
- With the help of signed messages
 - any number of faulty generals $f < n$ can be dealt with
 - with signed messages the Byzantine Generals problem can be solved in $f + 1$ rounds with $O(n^2)$ messages [Dolev & Strong 1983]
- For asynchronous systems with crash failures
 - No algorithm can reach consensus even if only **one processor** is faulty [Fischer, Lynch, Paterson 1985]
 - Each algorithm that tries to reach consensus can be confronted with a faulty process which influences the result if it continues (instead of crashing)

End of Section 4