



Wireless Sensor Networks

1. Basics

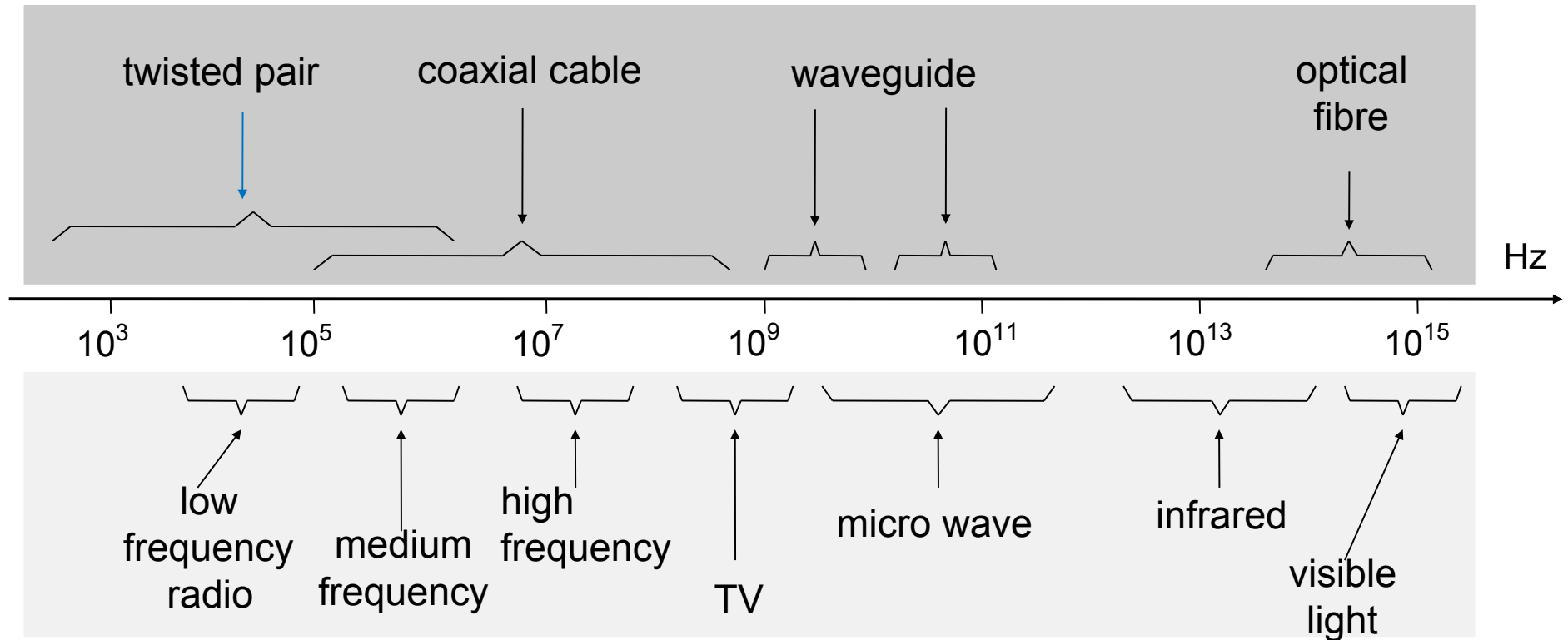
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- Moving particles with electric charge cause electromagnetic waves
 - frequency f : number of oscillations per second
 - unit: Hertz
 - wavelength λ : distance (in meters) between two wave maxima
 - antennas can create and receive electromagnetic waves
 - the transmission speed of electromagnetic waves in vacuum is constant
 - speed of light $c \approx 3 \cdot 10^8$ m/s
- Relation between wavelength, frequency and speed of light:

$$\lambda \cdot f = c$$

Electromagnetic Spectrum

guided media



unguided media

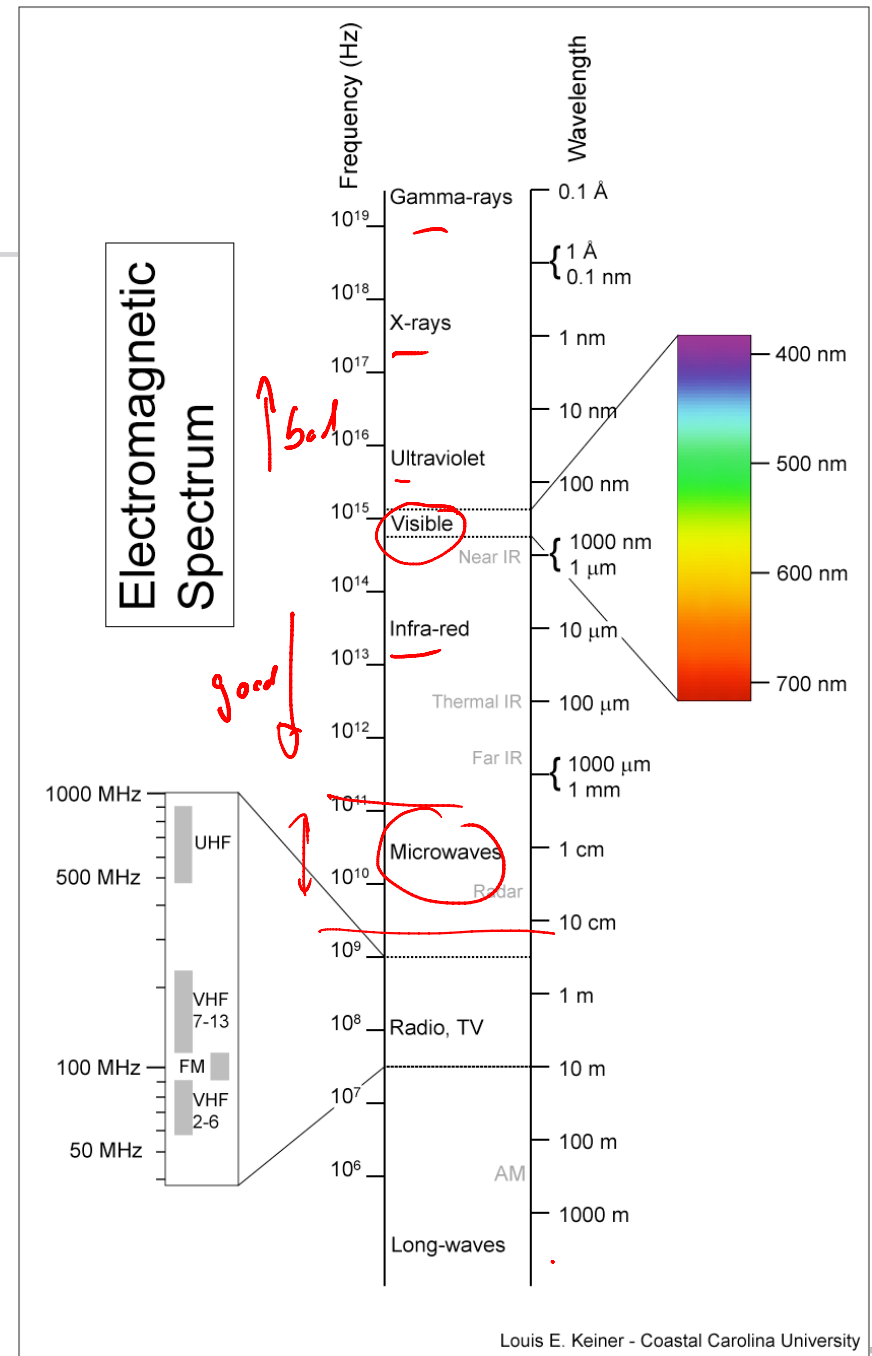
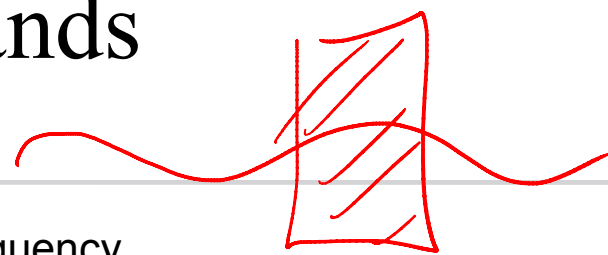
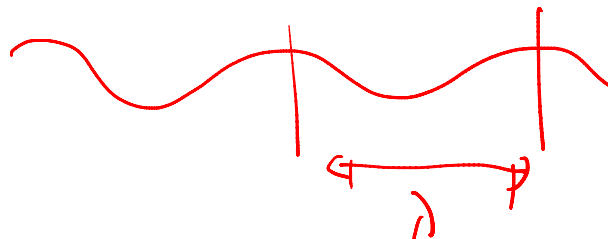
Bands

- LF Low Frequency
- MF Medium Frequency
- HF High Frequency
- VHF Very High Frequency
- UHF Ultra High Frequency
- UV Ultra Violet light

$$\lambda \cdot f = c$$


$$c = \frac{\lambda}{t}$$

$$f = \frac{1}{t}$$



Louis E. Keiner - Coastal Carolina University

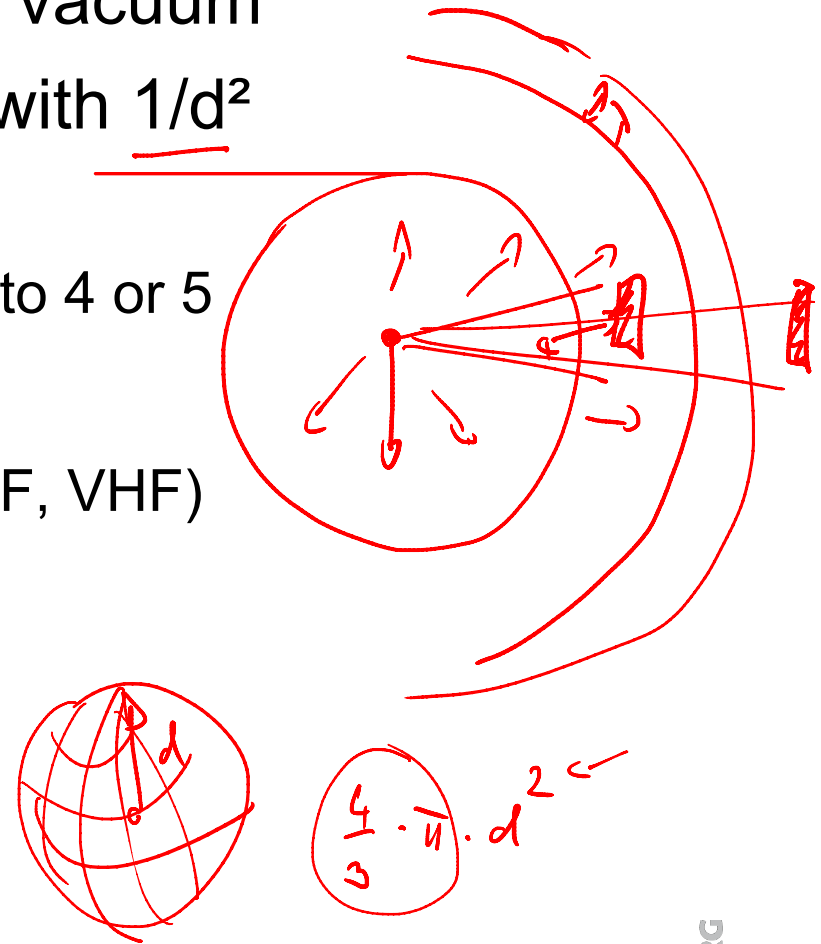
Bands for Wireless Networks

- VHF/UHF for mobile radio
 - antenna length
- SHF for point-to-point radio systems, satellite communication
- Wireless LAN: UHF to SHF
 - planned EHF
- Visible light 
 - communication by laser
- Infrared
 - remote controls
 - LAN in closed rooms

Propagation Performance

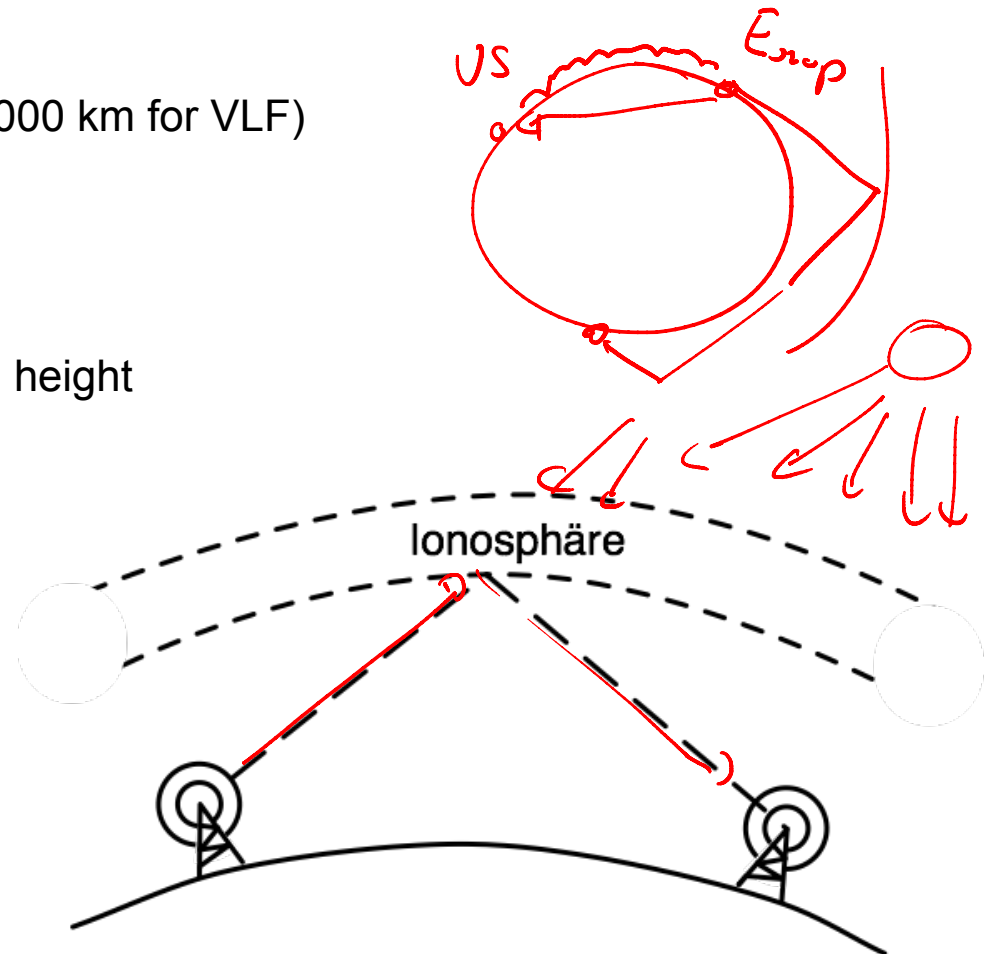
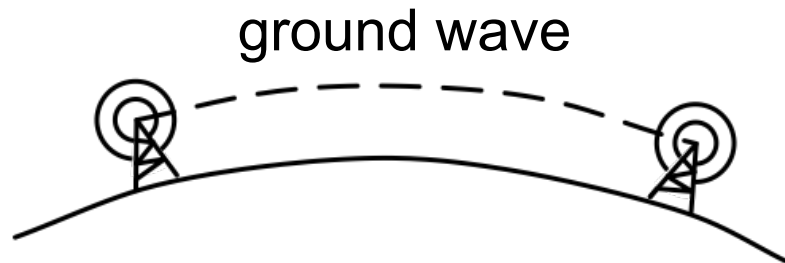


- Straight-lined propagation in vacuum
- Received power decreases with $1/d^2$
 - in theory
 - in practice higher exponents up to 4 or 5
- Reduction because of
 - attenuation in air (in particular HF, VHF)
 - shadowing and mountain effect
 - reflection
 - diffusion at small obstacles
 - diffraction



Frequency Dependent Behavior

- VLF, LF, MF
 - follow the curvature of the earth (up to 1000 km for VLF)
 - permeate buildings
- HF, VHF
 - absorbed by the ground
 - reflected by the ionosphere 100-500 km height
- Over 100 MHz
 - straight-line propagation
 - marginal penetration of buildings
 - good focus
- Over 8 GHz absorption by rainfall

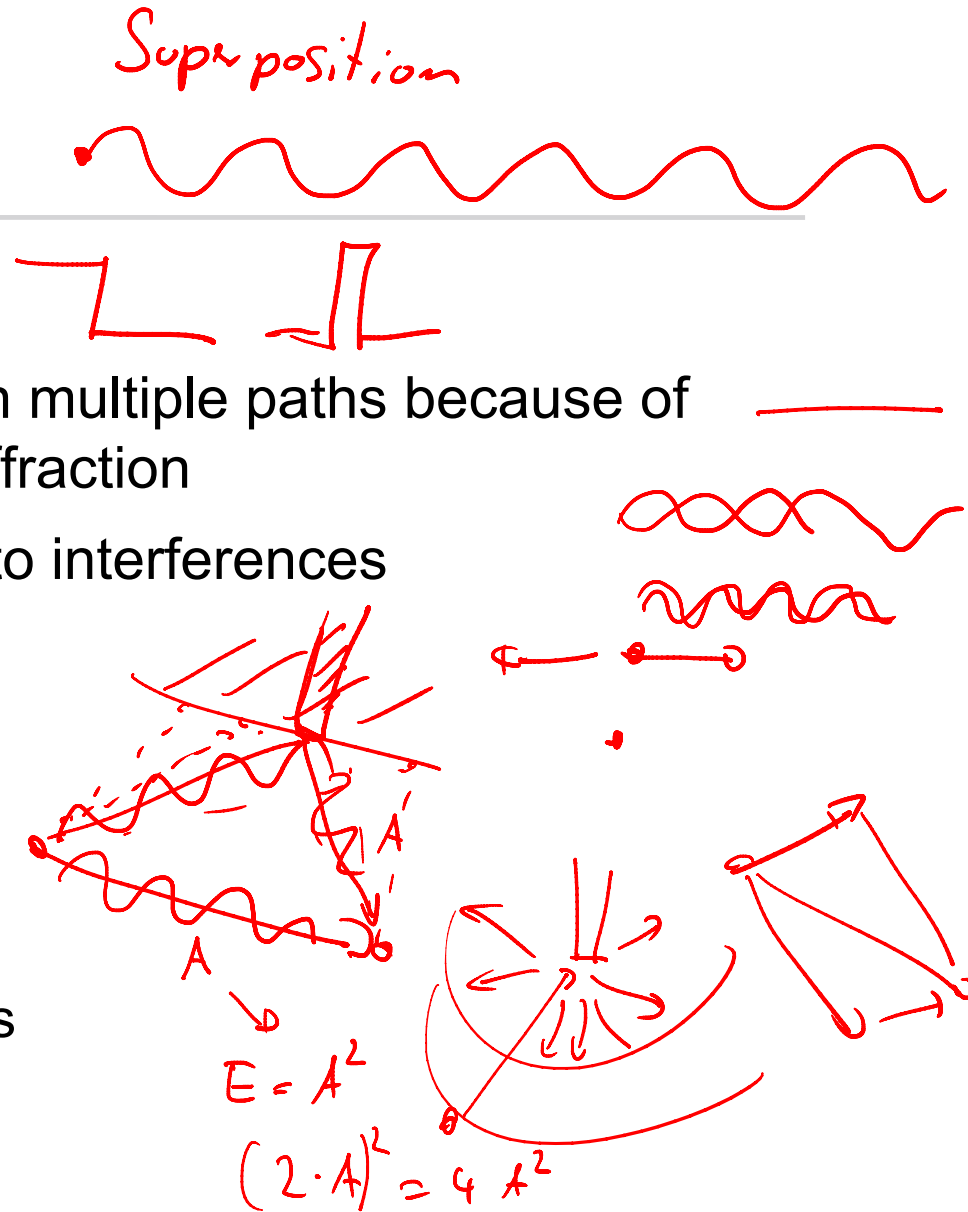


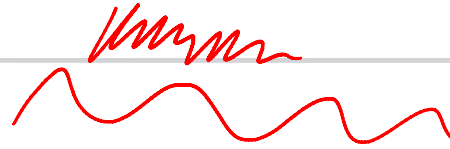
■ Multiple Path Fading

- Signal arrives at receiver on multiple paths because of reflection, diffusion, and diffraction
- Signal time variation leads to interferences
 - decoding faults
 - attenuation

■ Mobility problems

- Fast fading
 - different transmission paths
 - different phasing
- Slow fading
 - increase of distance between sender and receiver





- Noise
 - inaccuracies and heat development in electrical components
 - modeled by normal distribution
- Interference from other transmitters
 - in the same spectrum
 - or in neighbored spectrum
 - e.g. because of bad filters
- Effect
 - Signal is disrupted

Signal Interference Noise Ratio

- reception energy = transmission energy ~~·~~ path loss
 - path loss $\sim 1/d^\alpha$
 $\alpha \in [2,5]$
- Signal to Interference and Noise Ratio = SINR
 - S = (desired) Signal energy
 - I = energy of Interfering signals
 - N = Noise
- Necessary condition for reception

SINR

$$\text{SINR} = \frac{S}{I+N} \geq \text{Threshold}$$

▶ Attenuation

- Received signal power depends on the distance d between sender and receiver

▶ Friis transmission equation

- distance: R
- wavelength: λ
- P_r : energy at receiver antenna
- P_t : energy at sender antenna
- G_t : sender antenna gain
- G_r : receiver antenna gain

$$\frac{P_r}{P_t} = G_t G_r \left(\frac{\lambda}{4\pi R} \right)^2$$

$$P_r(d) = P_r(d_0) \cdot \left(\frac{d_0}{d} \right)^2$$

Path Loss Exponent

$$\sim \frac{1}{d^5}$$

■ Measurements

- α path loss exponent
- shadowing variance σ^2
- reference path loss at 1m distance

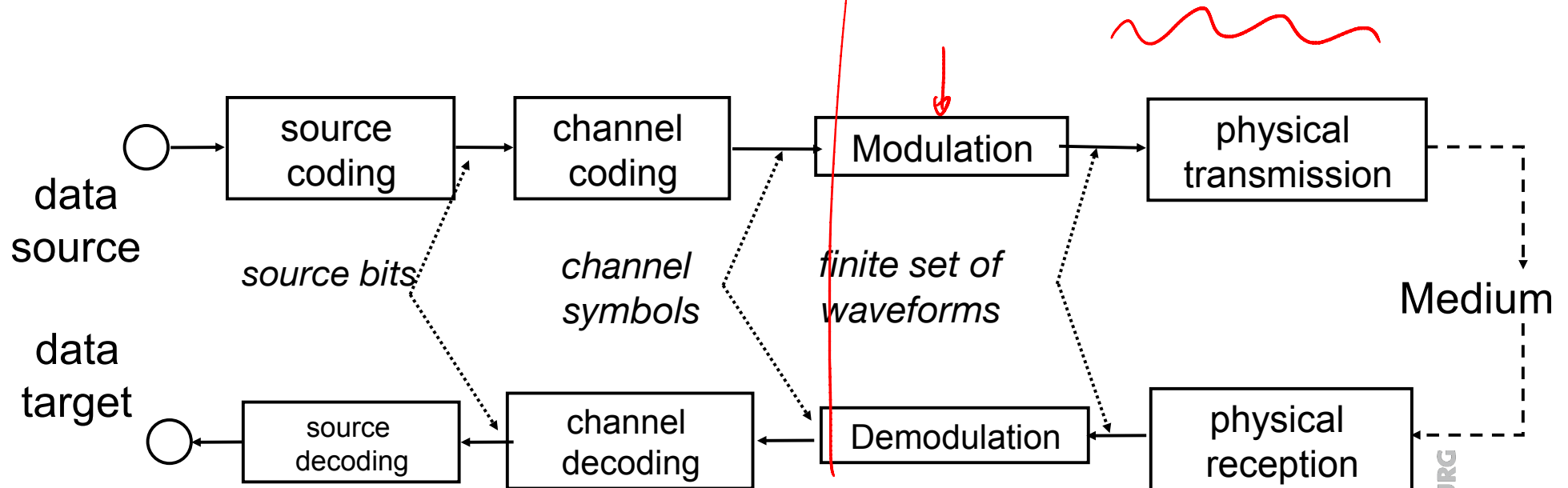
Location	Average of γ	Average of σ^2 [dB]	Range of PL(1m) [dB]
Engineering Building	1.9	5.7	[-50.5, -39.0]
Apartment Hallway	<u>2.0</u>	8.0	[-38.2, -35.0]
Parking Structure	3.0	7.9	[-36.0, -32.7]
One-sided Corridor	1.9	8.0	[-44.2, -33.5]
One-sided patio	3.2	3.7	[-39.0, -34.2]
Concrete canyon	2.7	10.2	[-48.7, -44.0]
Plant fence	4.9	9.4	[-38.2, -34.5]
Small boulders	3.5	12.8	[-41.5, -37.2]
Sandy flat beach	4.2	4.0	[-40.8, -37.5]
Dense bamboo	<u>5.0</u>	11.6	[-38.2, -35.2]
Dry tall underbrush	3.6	8.4	[-36.4, -33.2]

Karl, Willig, Protocols and Architectures for Wireless Sensor Networks, Wiley, 2005

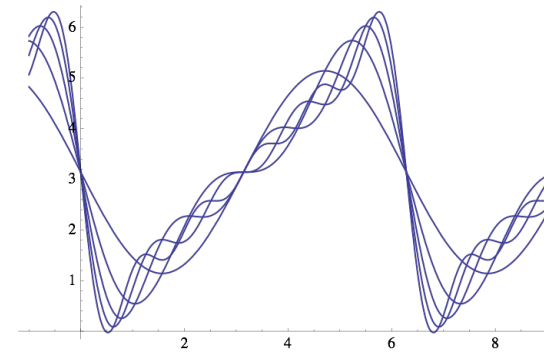
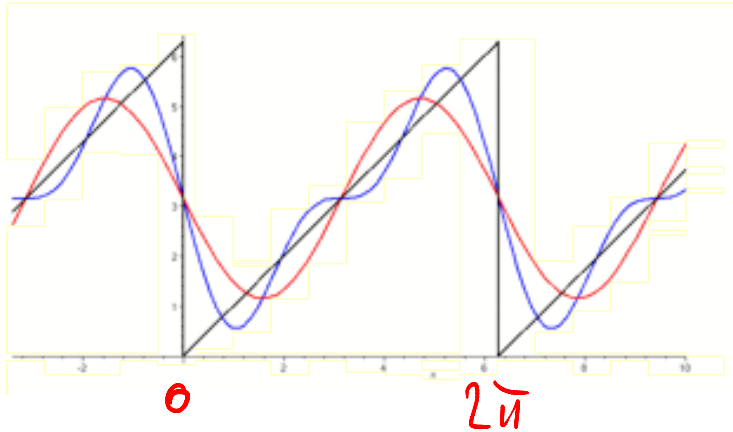
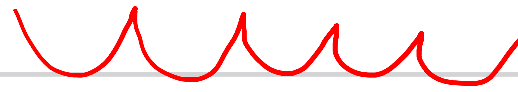
Structure of a *Broadband* Digital transmission

■ MOdulation/DEModulation

- Translation of the channel symbols by
 - amplitude modulation
 - phase modulation
 - frequency modulation
 - or a combination thereof

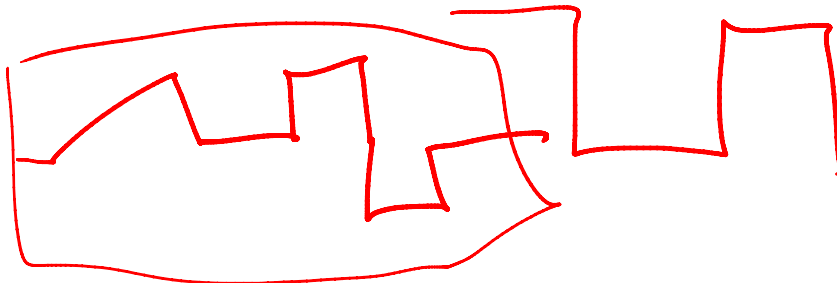
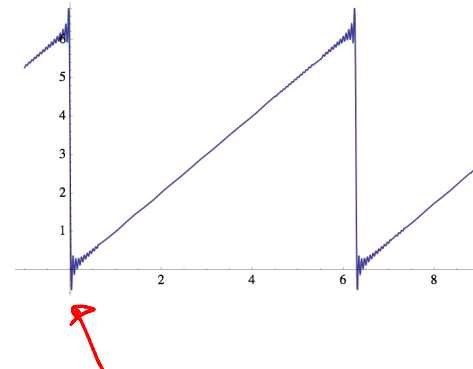


Computation of Fourier Coefficients



$$f(x) = x, \text{ für } 0 < x < 2\pi$$

$$f(x) = \pi - 2 \left(\frac{\sin x}{1} + \frac{\sin 2x}{2} + \frac{\sin 3x}{3} + \dots \right)$$



- Theorem of Fourier for period $T=1/f$:
 - The coefficients c , a_n , b_n are then obtained as follows

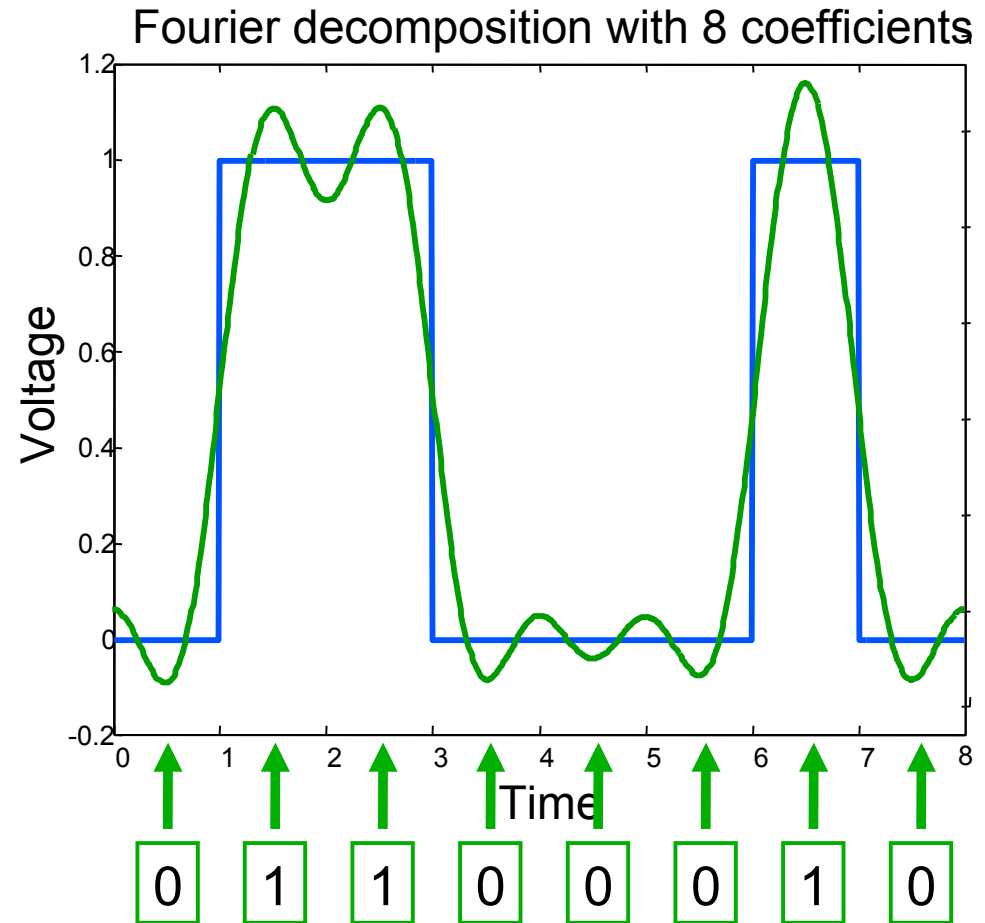
$$g(t) = \frac{a_0}{2} + \sum_{k=1}^{\infty} a_k \cos(2\pi k f t) + b_k \sin(2\pi k f t)$$

$$a_k = \frac{2}{T} \int_0^T g(t) \cos(2\pi n f t) dt$$
$$b_k = \frac{2}{T} \int_0^T g(t) \sin(2\pi n f t) dt$$

- The sum of squares of the k -th terms is proportional to the energy consumed in this frequency: $(a_k)^2 + (b_k)^2$

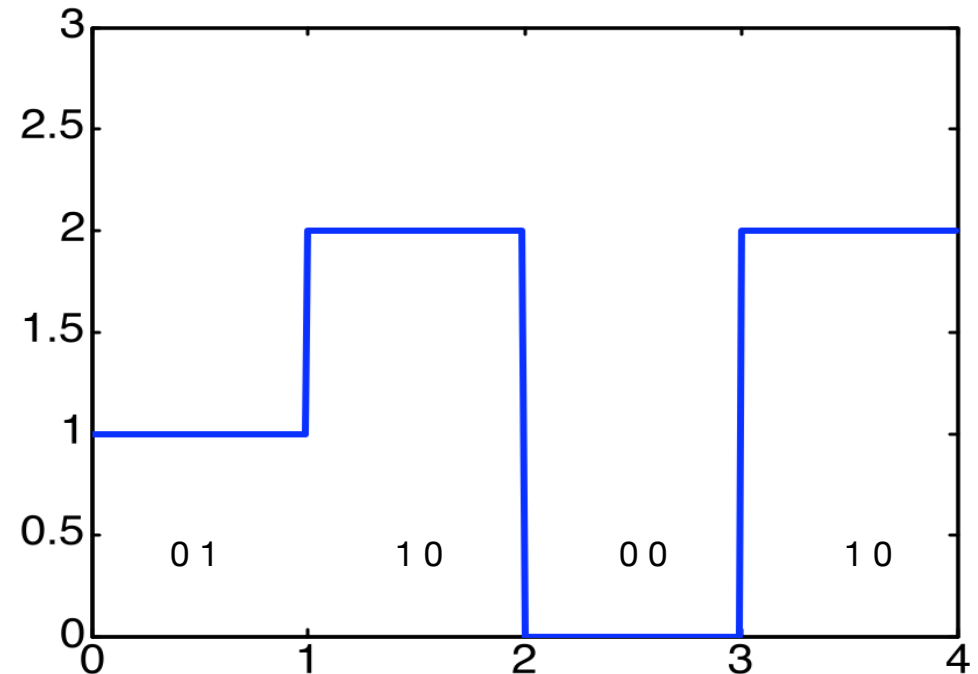
How often do you measure?

- How many measurements are necessary
 - to determine a Fourier transform to the k -th component, exactly?
- Nyquist-Shannon sampling theorem
 - To reconstruct a continuous band-limited signal with a maximum frequency f_{\max} you need at least a sampling frequency of $2 f_{\max}$.



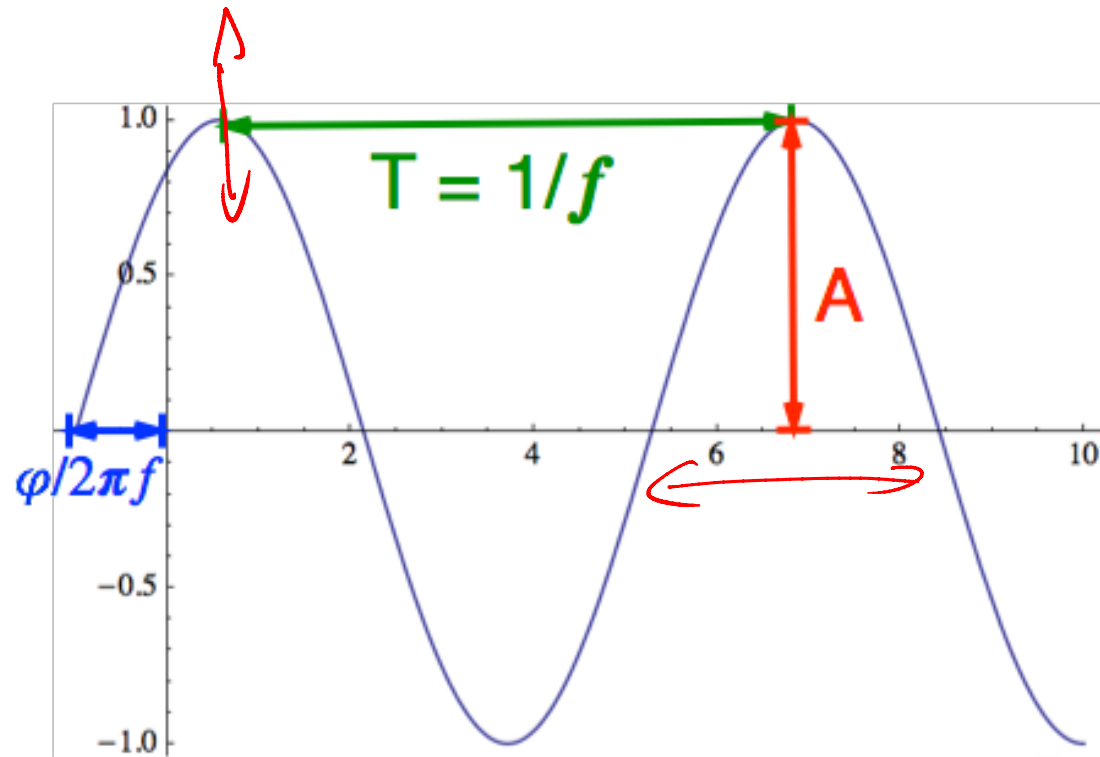
Symbols and Bits

- For data transmission instead of bits can also be used symbols
 - E.g. 4 Symbols: A, B, C, D
 - A = 00, B = 01, C = 10, D = 11
- Symbols
 - Measured in baud
 - Number of symbols per second
- Data rate
 - Measured in bits per second
 - Number of bits per second
- Example
 - 2400 bit/s modem is 600 baud (uses 16 symbols)



- Idea
 - Focusing on the ideal frequency of the medium
 - Using a sine wave as the carrier wave signals
- A sine wave has no information
 - the sine curve continuously (modulated) changes for data transmission,
 - implies spectral widening (more frequencies in the Fourier analysis)
- The following parameters can be changed:
 - Amplitude A
 - Frequency $f=1/T$
 - Phase φ

$$s(t) = A \sin(2\pi f t + \phi)$$

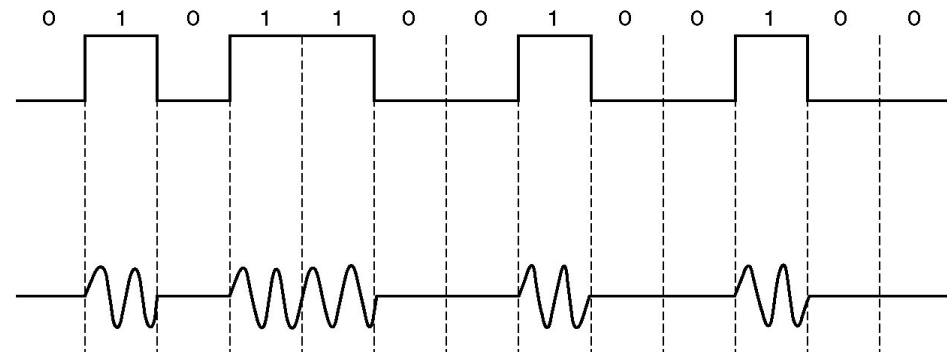
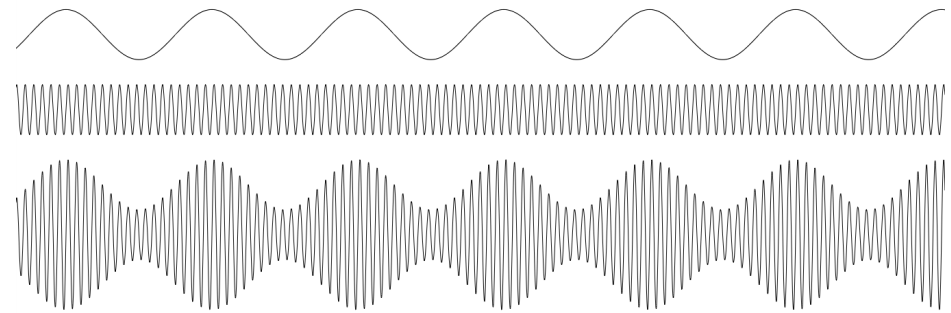


Amplitude Modulation

- The time-varying signal $s(t)$ is encoded as the amplitude of a sine curve:

$$f_A(t) = s(t) \sin(2\pi ft + \phi)$$

- Analog Signal
- Digital signal
 - amplitude keying
 - special case: symbols 0 or 1
 - on / off keying

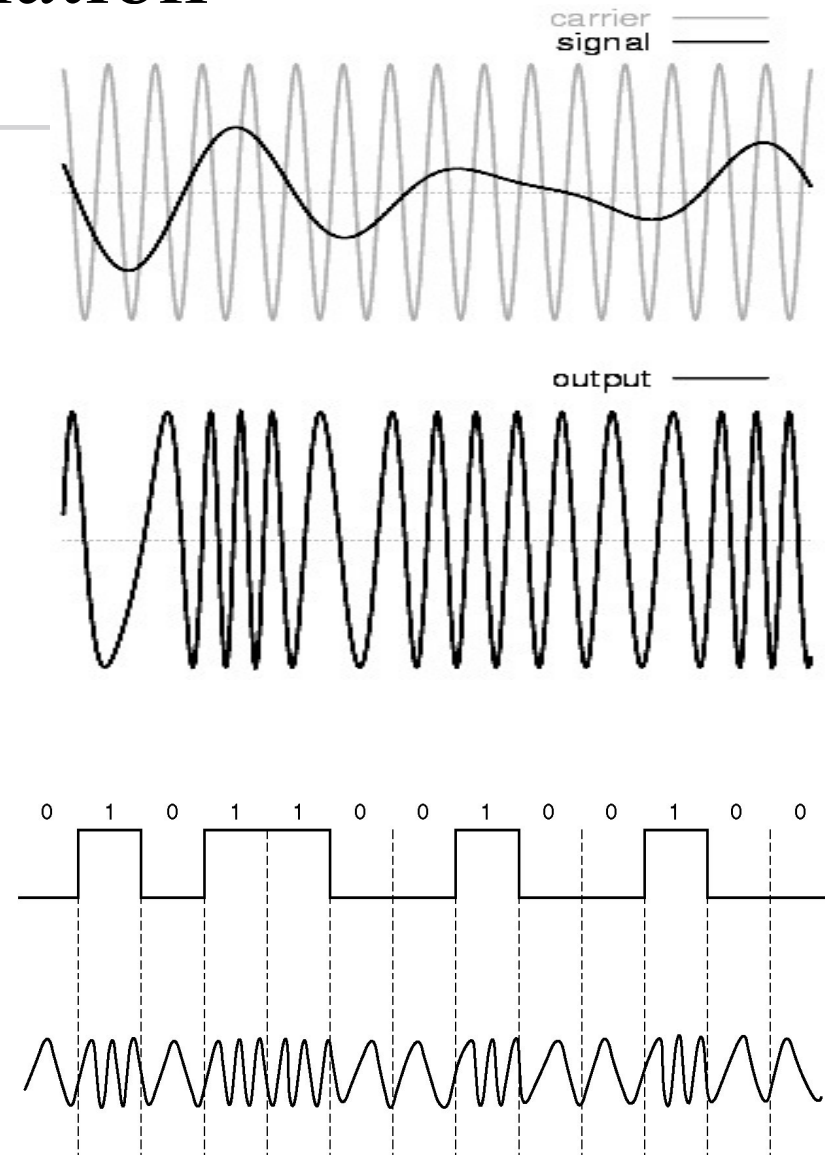


Frequency Modulation

- The time-varying signal $s(t)$ is encoded in the frequency of the sine curve:

$$f_F(t) = a \sin(2\pi s(t)t + \phi)$$

- Analog signal
 - Frequency modulation (FM)
 - Continuous function in time
- Digital signal
 - Frequency Shift Keying (FSK)
 - E.g. frequencies as given by symbols

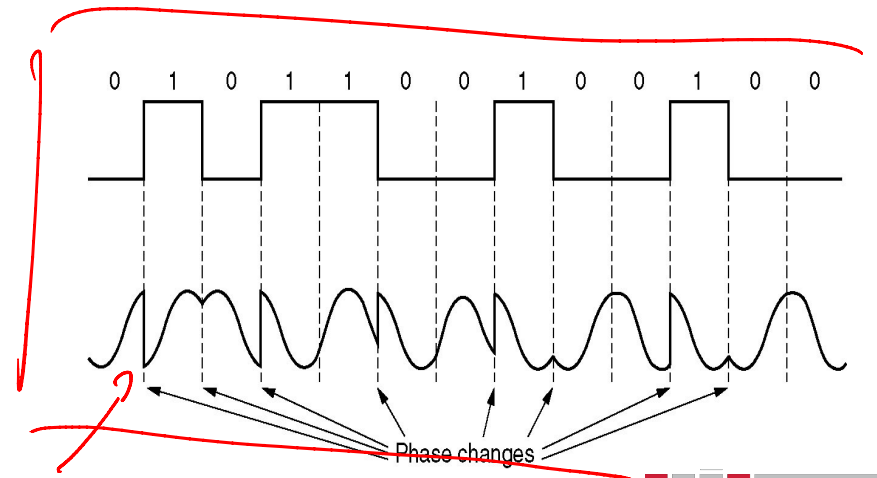
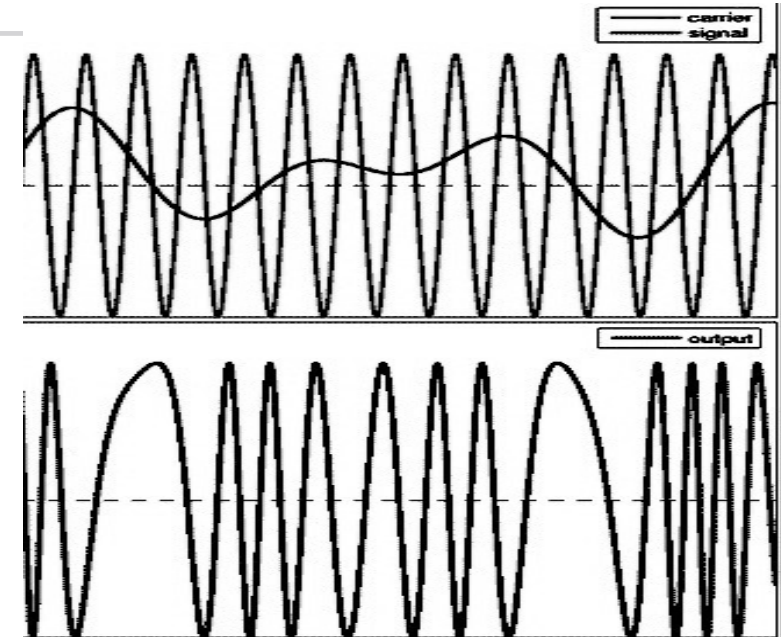
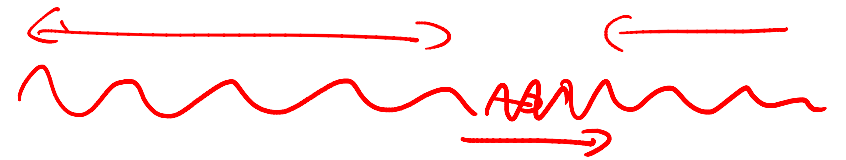


Phase Modulation

- The time-varying signal $s(t)$ is encoded in the phase of the sine curve:

$$f_P(t) = a \sin(2\pi ft + s(t))$$

- Analog signal
 - phase modulation (PM)
 - very unfavorable properties
 - es not used
- Digital signal
 - phase-shift keying (PSK)
 - e.g. given by symbols as phases



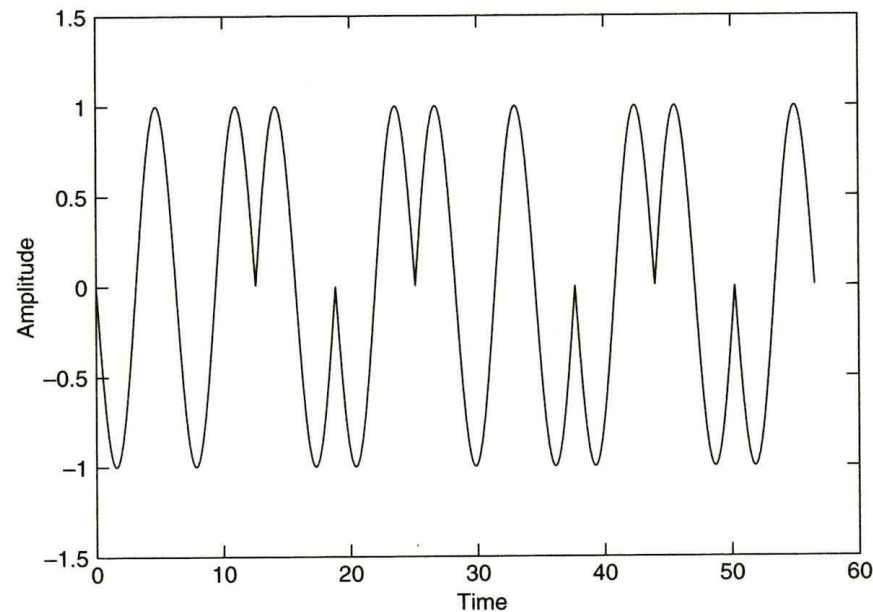
- For a station there are two options
 - digital transmission
 - finite set of discrete signals
 - e.g. finite amount of voltage sizes / voltages
 - analog transmission
 - Infinite (continuous) set of signals
 - E.g. Current or voltage signal corresponding to the wire
- Advantage of digital signals:
 - There is the possibility of receiving inaccuracies to repair and reconstruct the original signal
 - Any errors that occur in the analog transmission may increase further

Phase Shift Keying (PSK)

- For phase signals $\phi_i(t)$

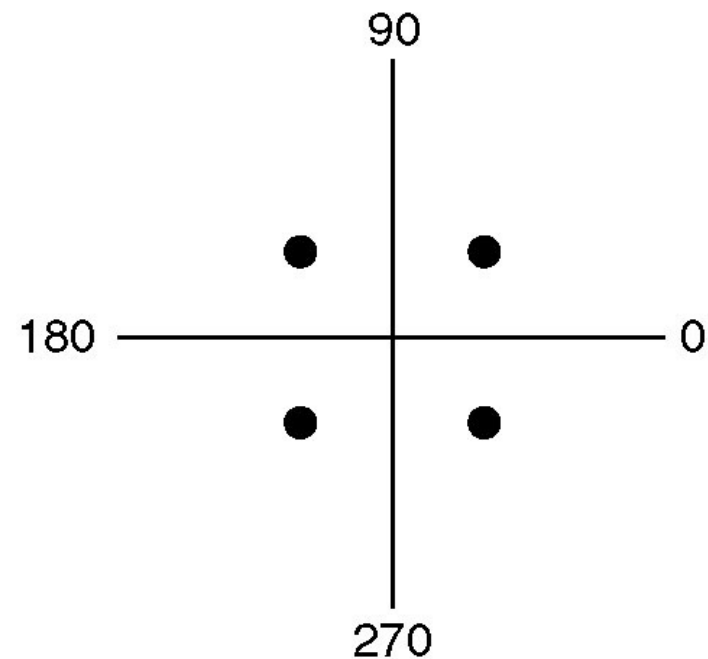
$$s_i(t) = \sqrt{\frac{2E}{T}} \cdot \sin(\omega_0 t + \phi_i(t))$$

- Example:

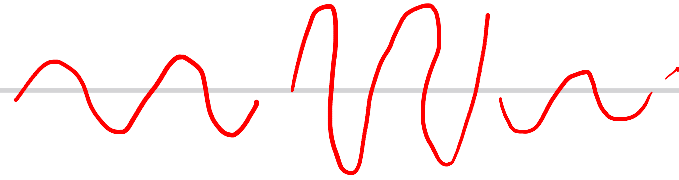


PSK with Different Symbols

- Phase shifts can be detected by the receiver very well
- Encoding various Symbols very simple
 - Using phase shift e.g. $\pi / 4$, $3/4\pi$, $5/4\pi$, $7/4\pi$
 - rarely: phase shift 0 (because of synchronization)
 - For four symbols, the data rate is twice as large as the symbol rate
- This method is called Quadrature Phase Shift Keying (QPSK)



Amplitude and Phase Modulation



- Amplitude and phase modulation can be successfully combined
 - Example: 16-QAM (Quadrature Amplitude Modulation)
 - uses 16 different combinations of phases and amplitudes for each symbol
 - Each symbol encodes four bits ($2^4 = 16$)
 - The data rate is four times as large as the symbol rate

